

# Bayesian Analysis of Electron Kinetic Profiles.

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\* See the Appendix of F. Romanelli et al., Fusion Energy Conference 2008 (Proc. 22nd Int. FEC Geneva) IAEA

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Overall Idea: Add  $n_e$ ,  $T_e$  diagnostics to Bayesian Analysis

- Polarimetry

  - [ Relativistic Model Testing ]

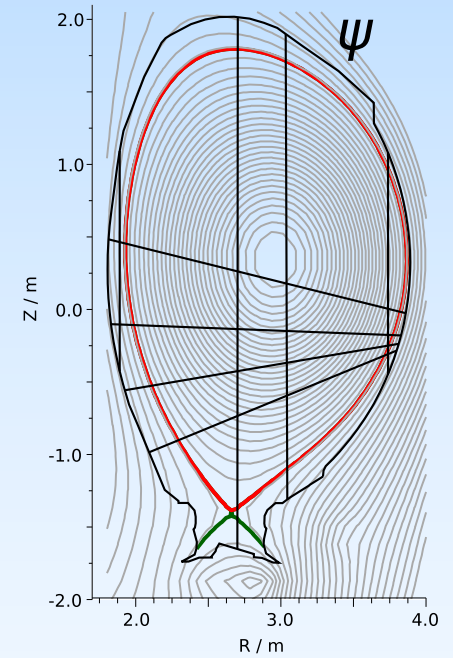
- Core LIDAR

- Edge LIDAR

- Equilibrium

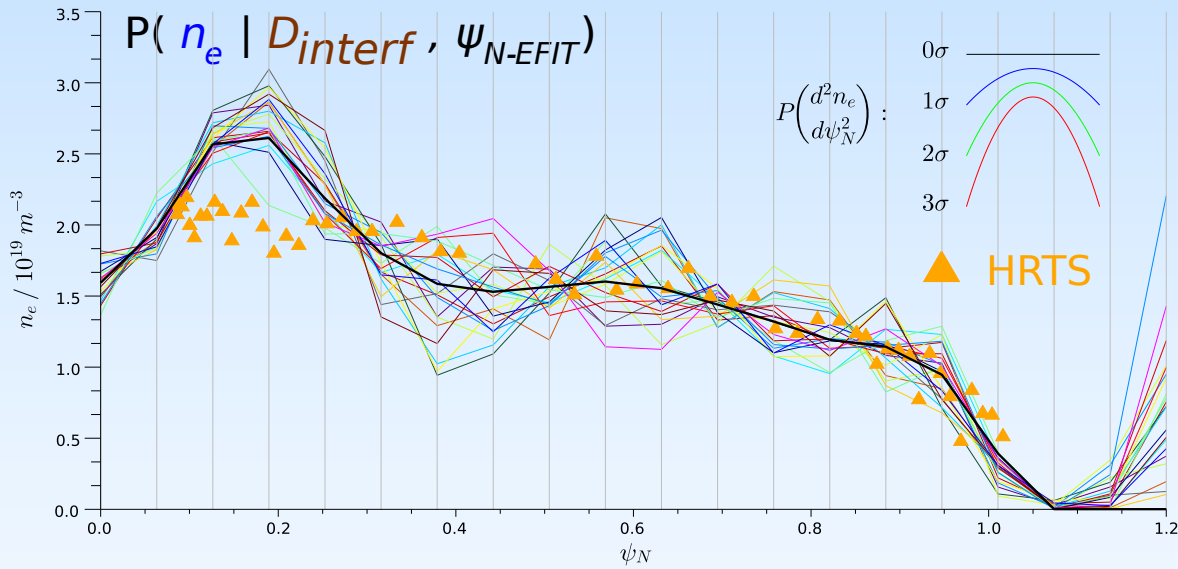
## Interferometry + Current Tomography I

Invert interferometry data to  $n_e(\psi_N)$  using weak smoothing prior based on magnetics only EFIT flux surfaces

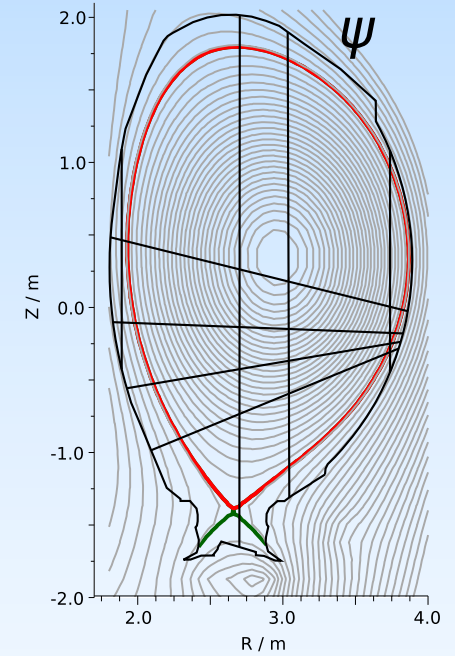


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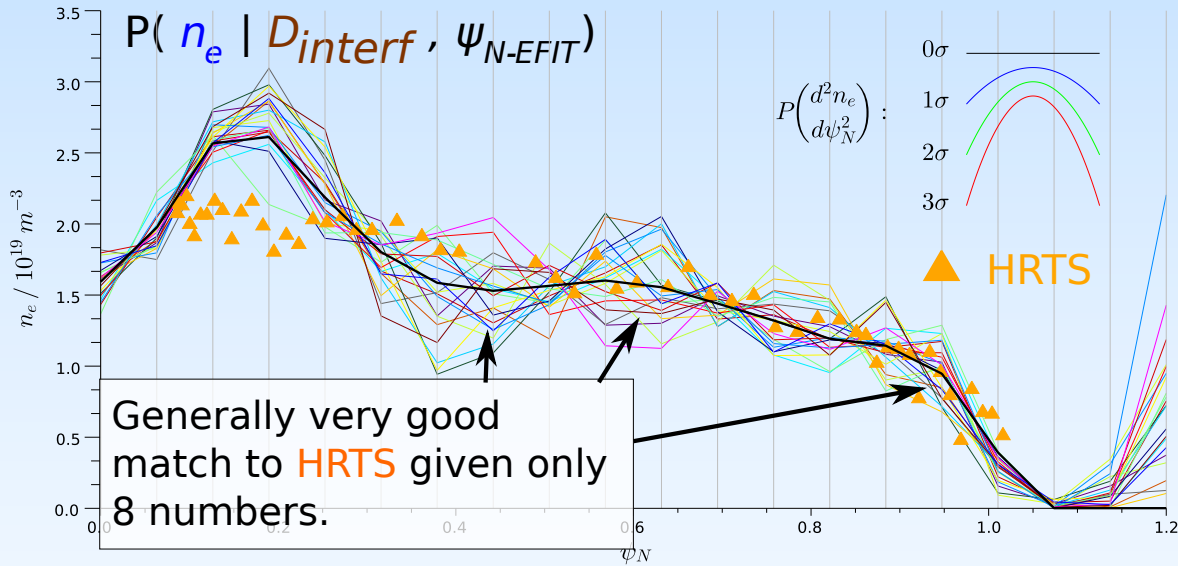
78625  
Ohmic  
(recovery pulse)



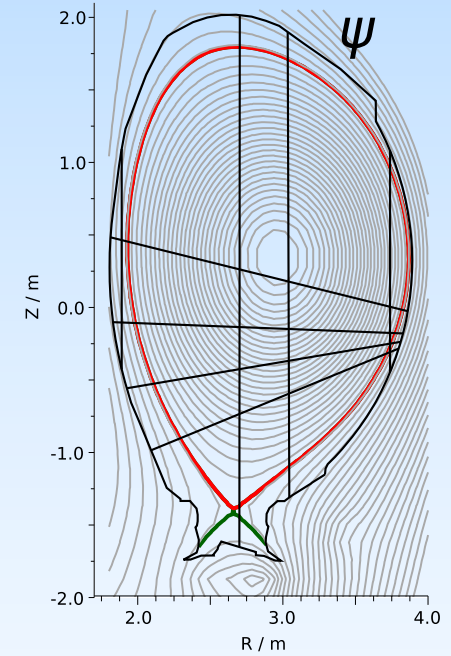


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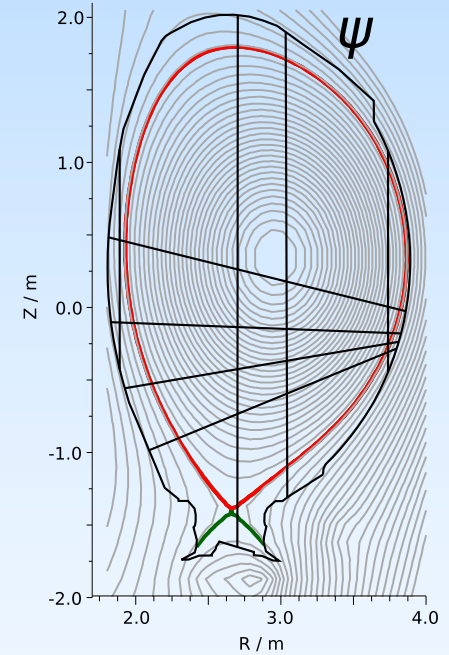
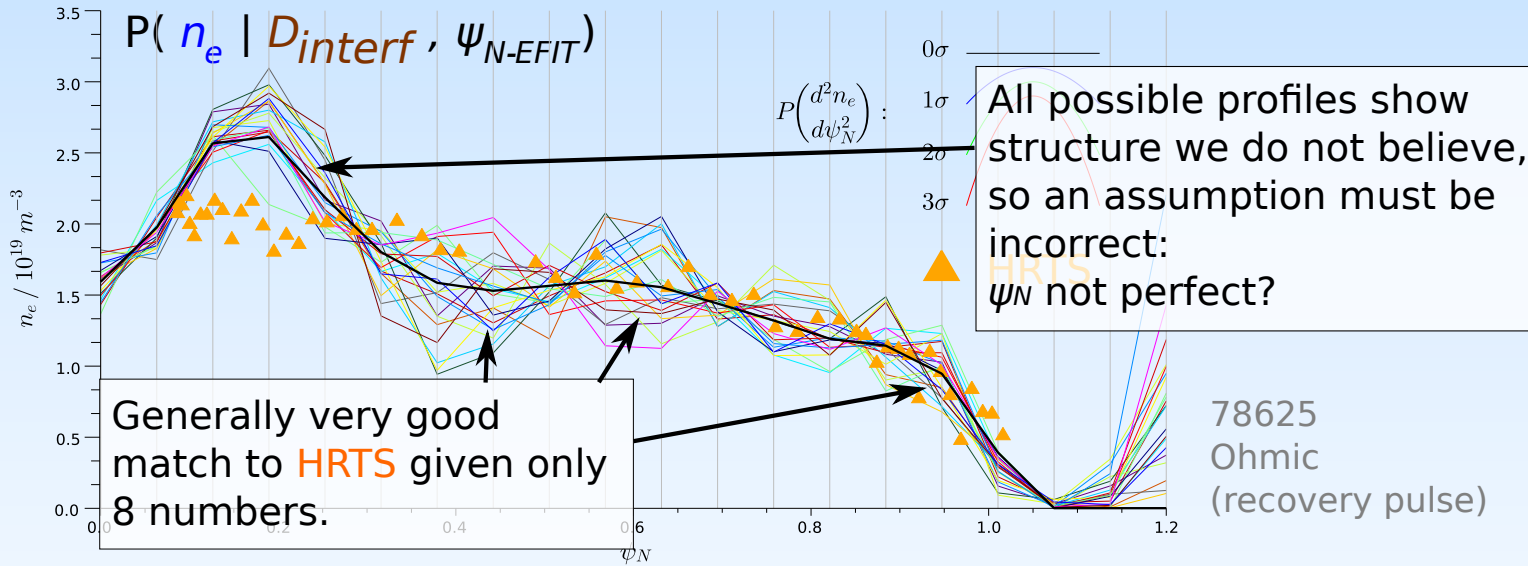


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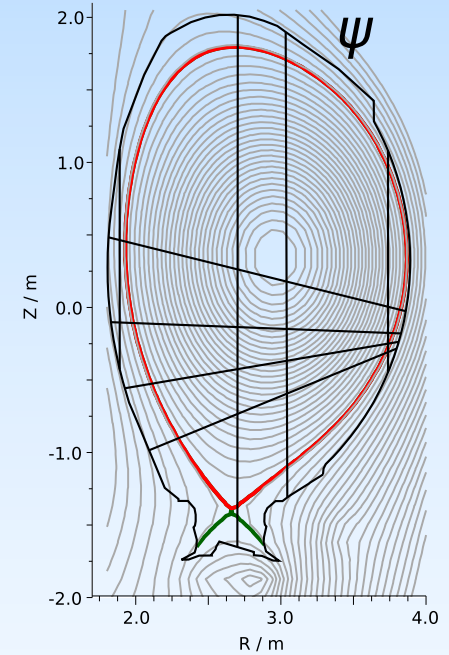
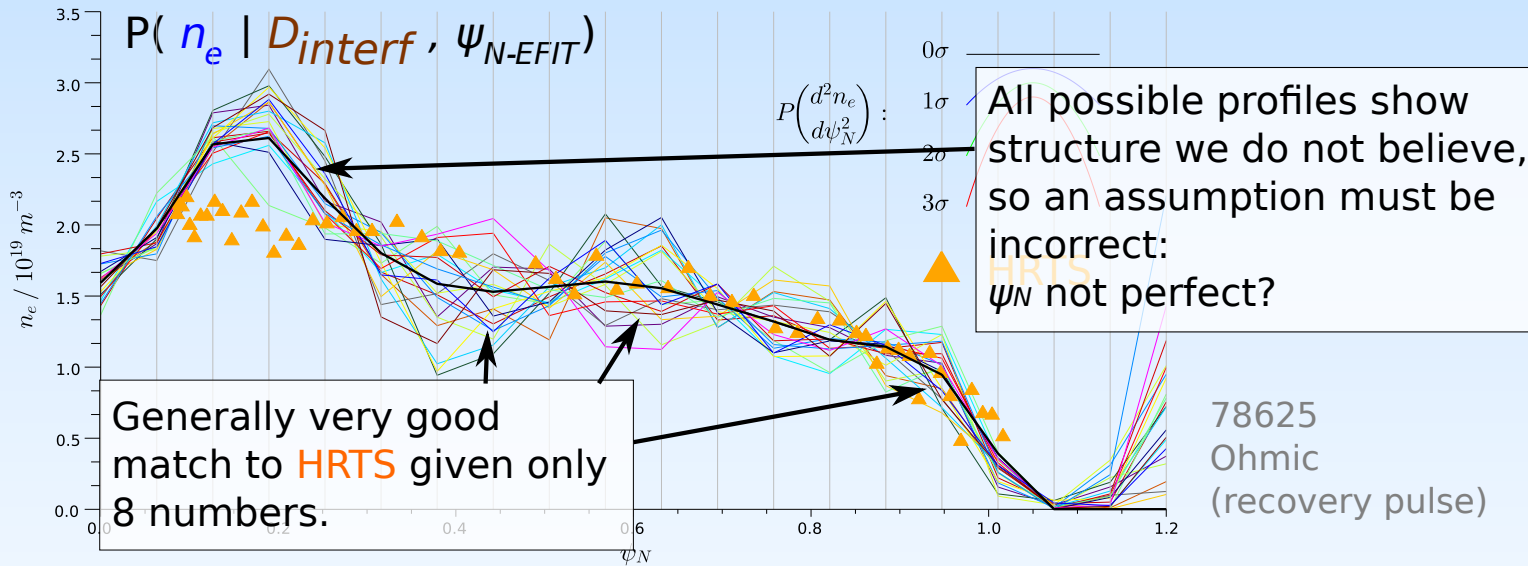
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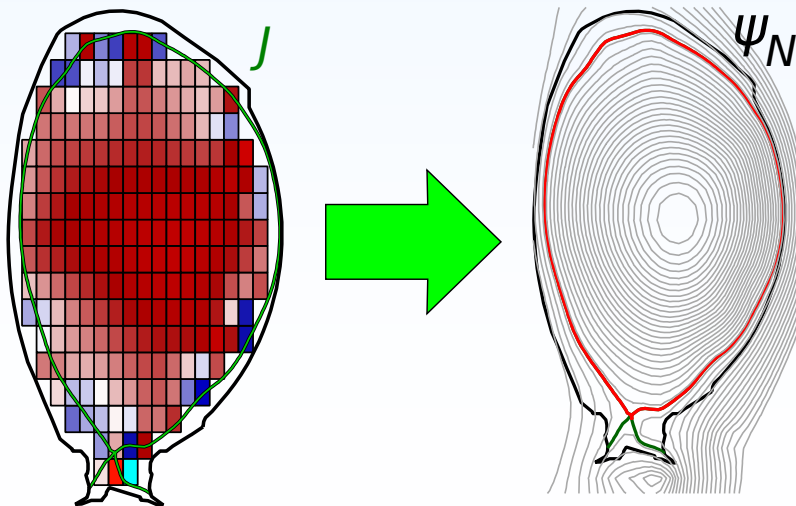


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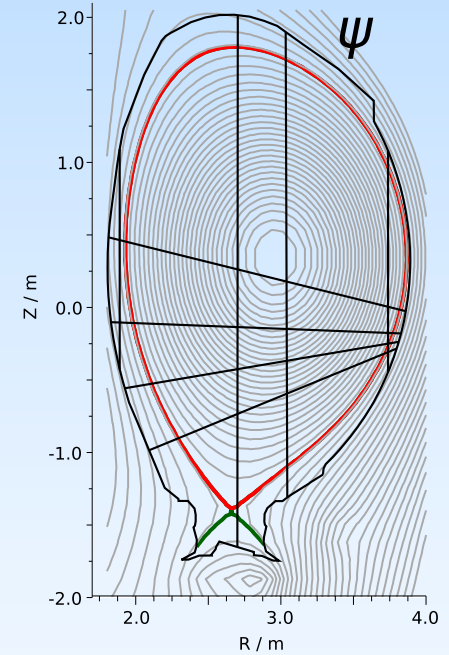
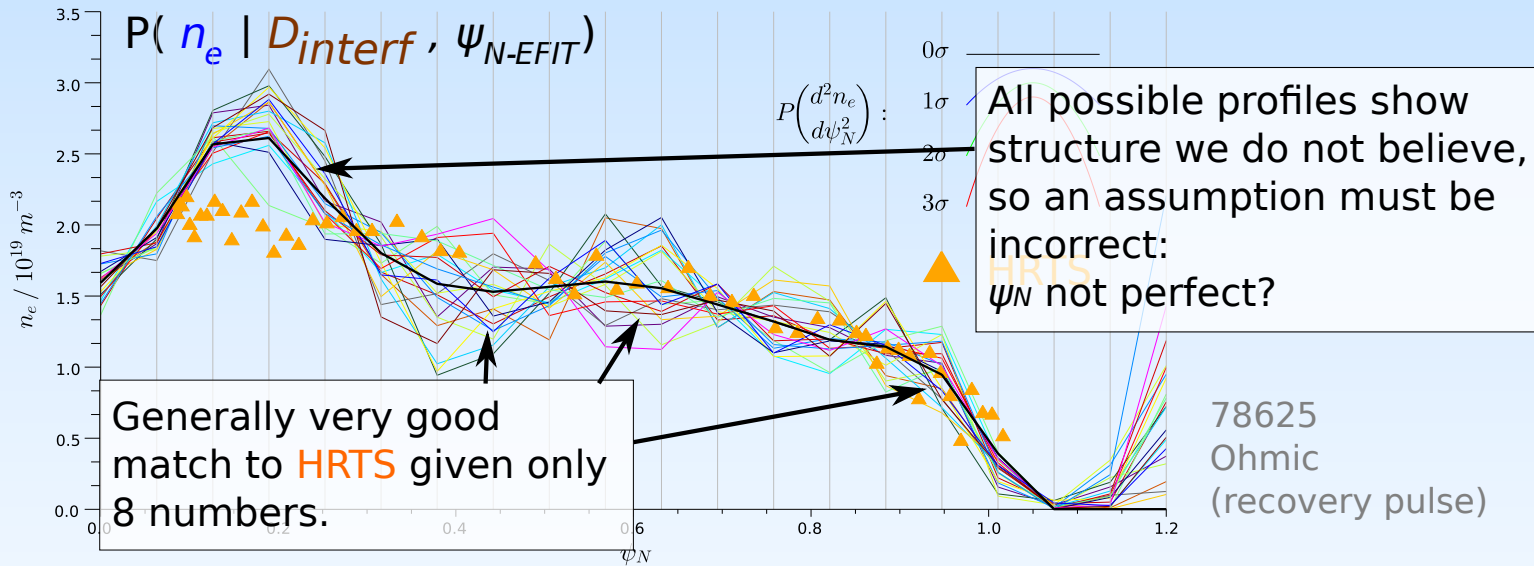
Instead, calculate  $\psi_N$  from toroidal currents  $J$ , include magnetics diagnostics and invert to full posterior: Finds combinations of  $J$  and  $n_e$  that are consistent with both interferometry and magnetics (and with  $n_e$  and  $J$  priors).



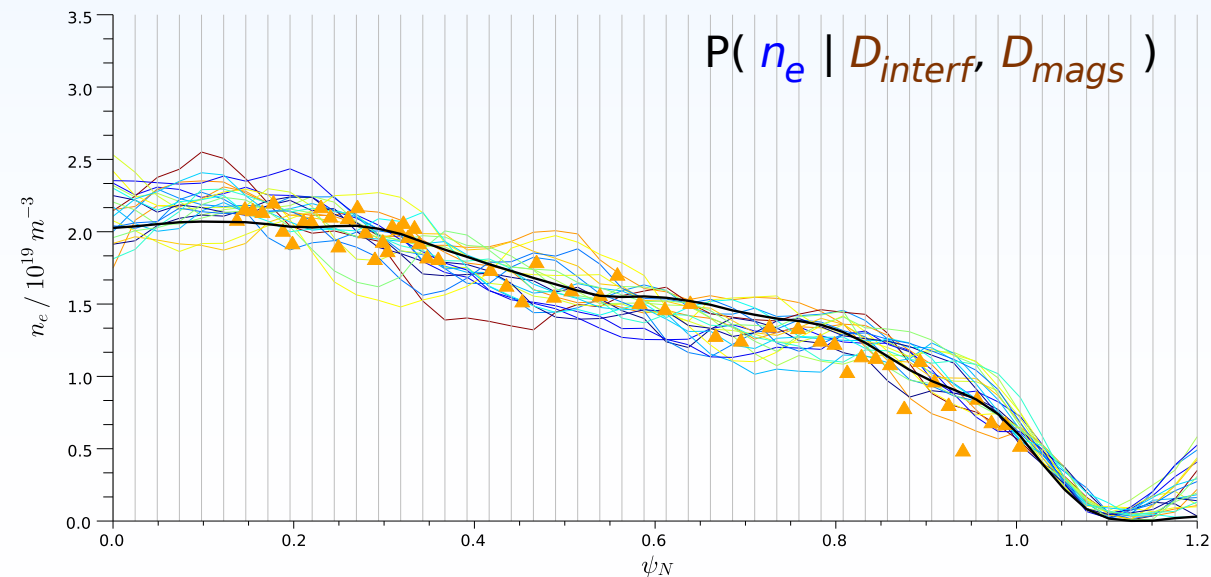
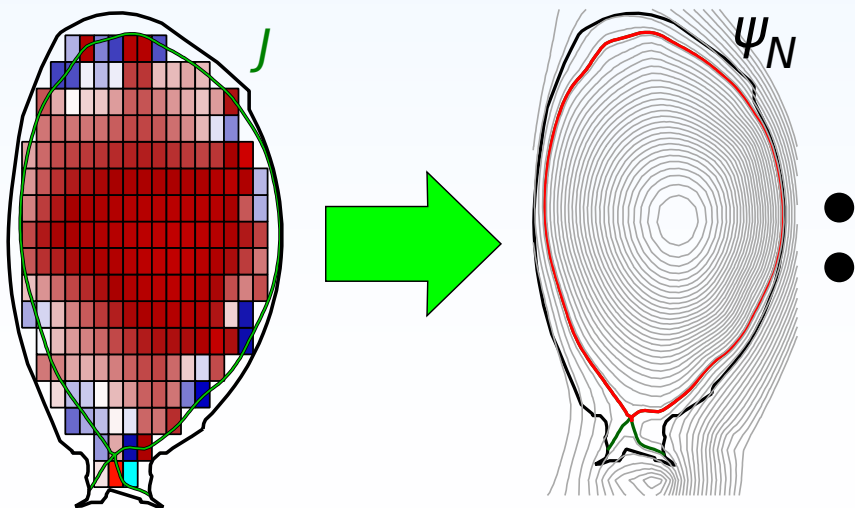


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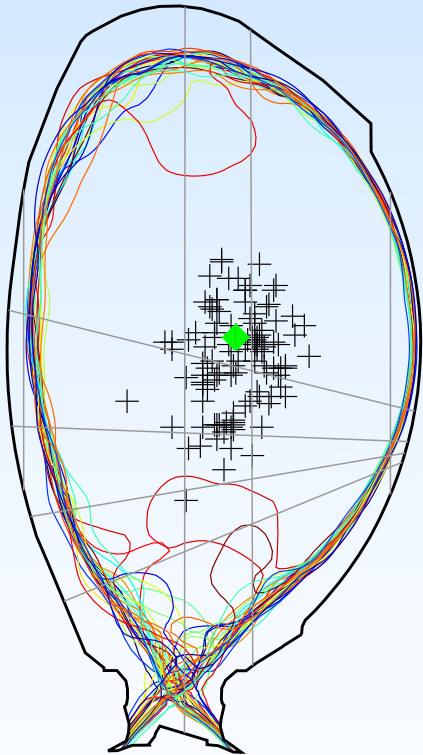
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Magnetics  
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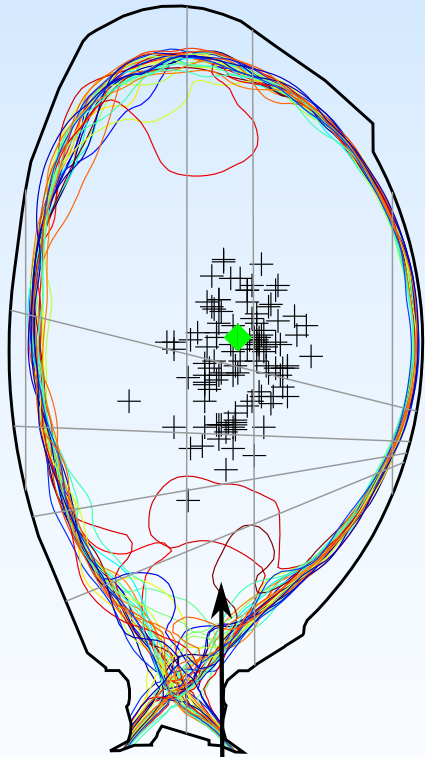


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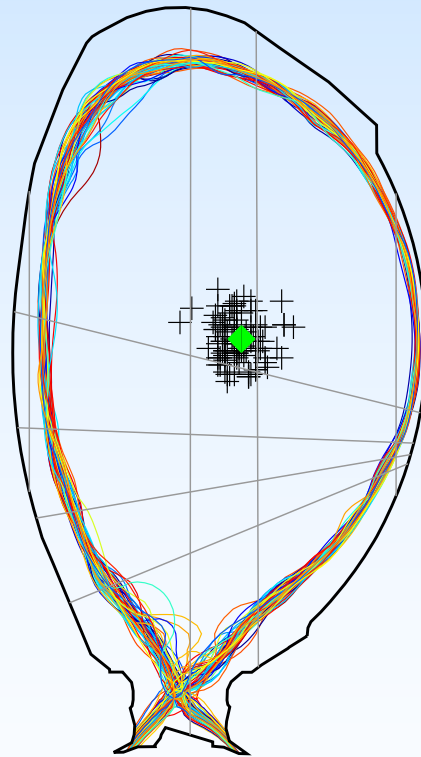
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Magnetics + Weak CAR prior  
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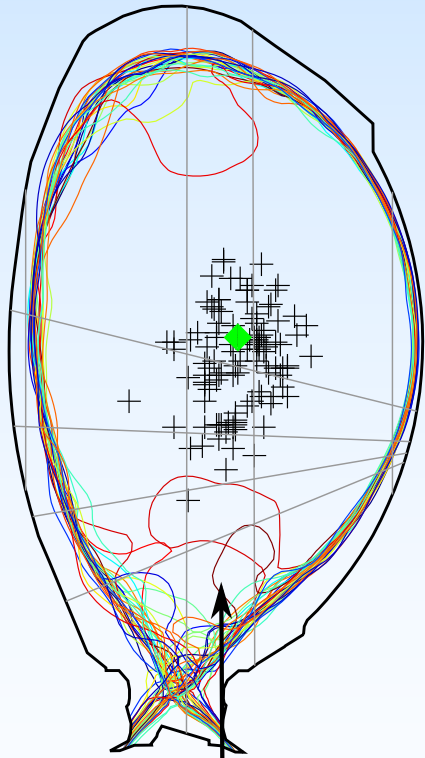
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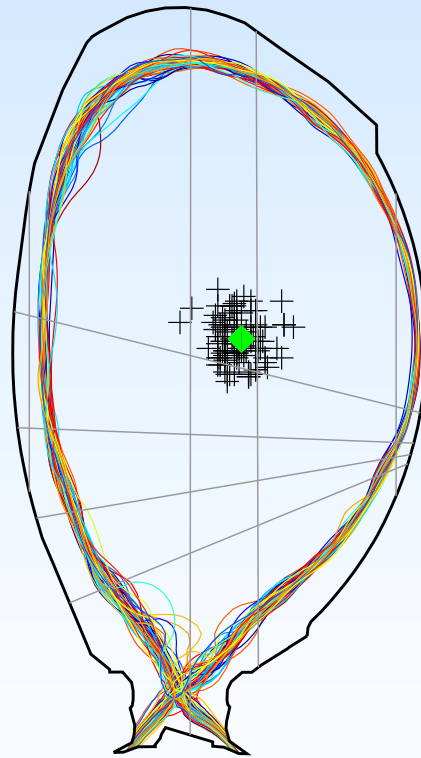
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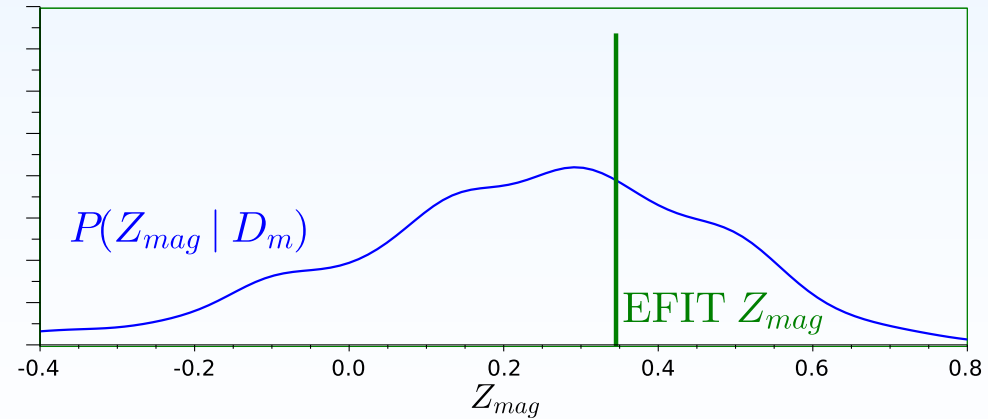
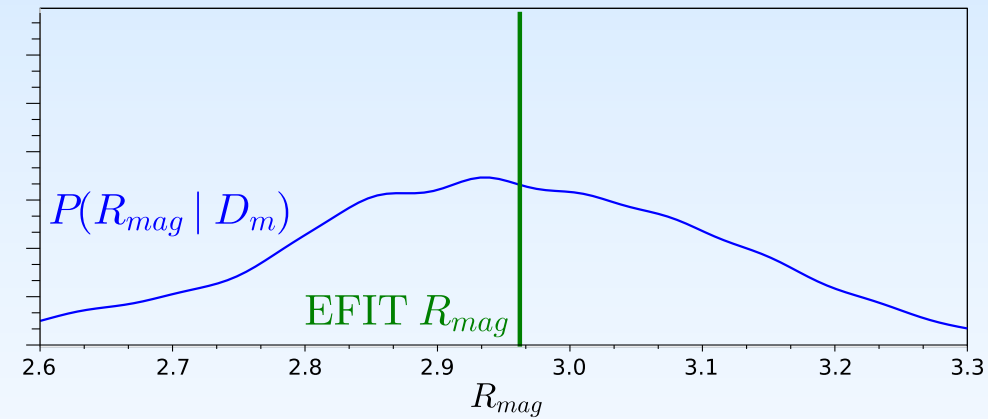
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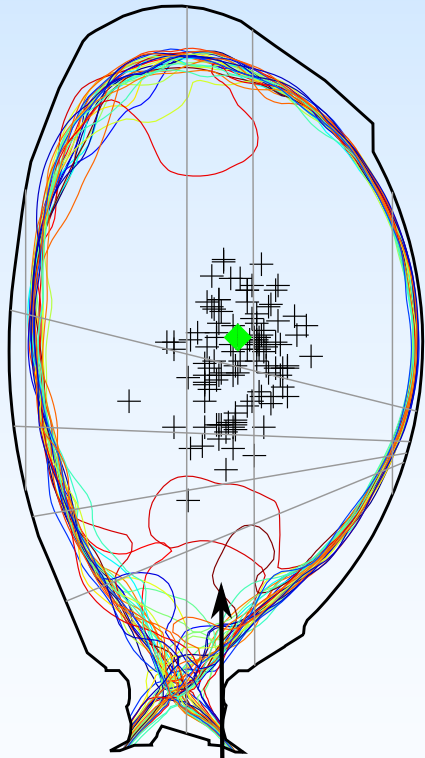
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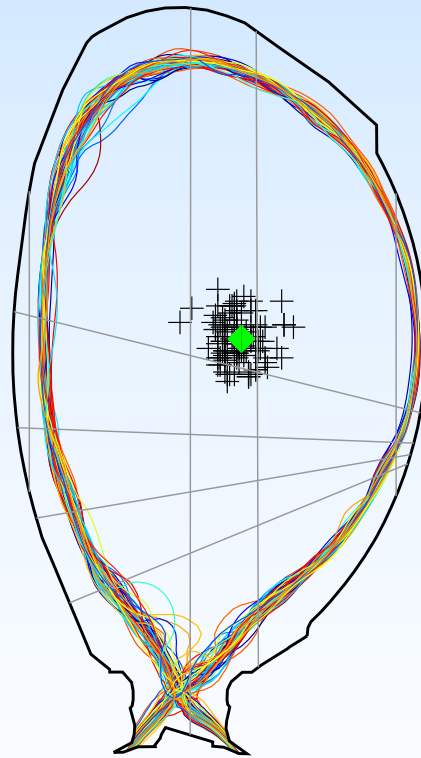
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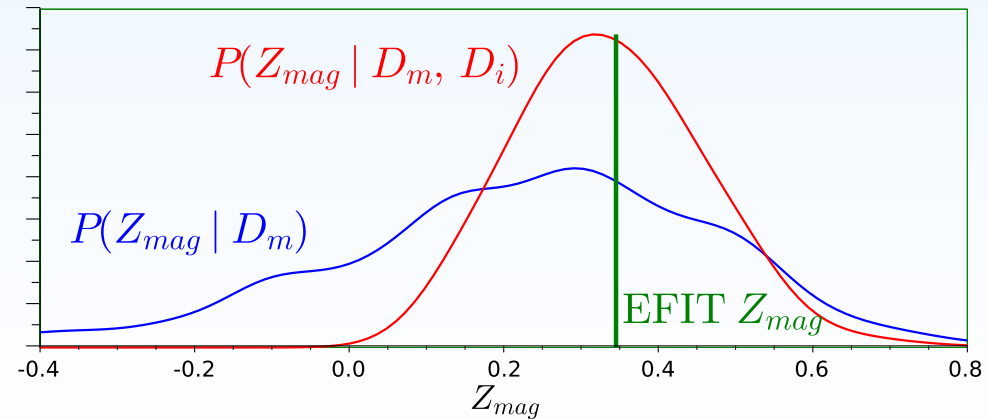
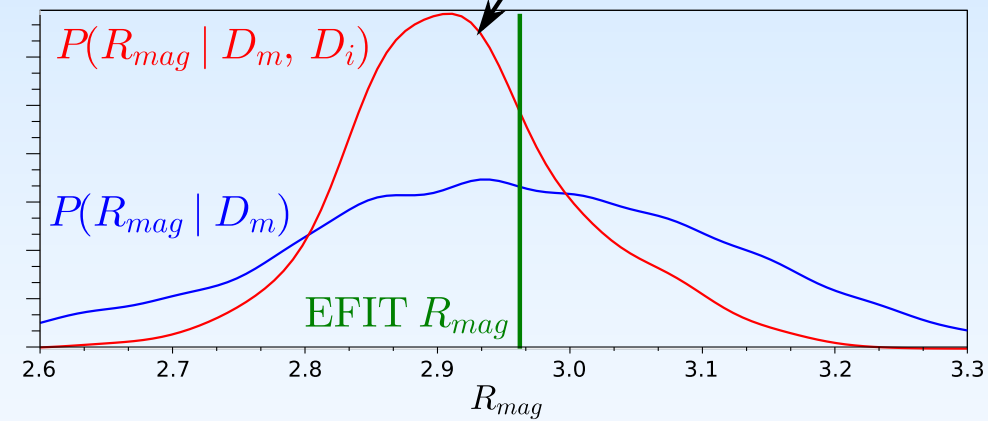
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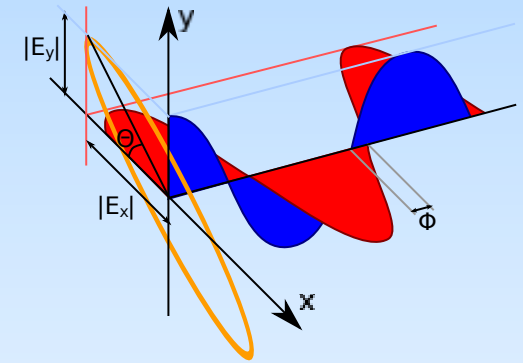
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Less obviously, gives higher certainty magnetic axis



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Use well known full plasma polarisation evolution equation.  
Depends primarily on  $n_e$  and  $\mathbf{B}$ .

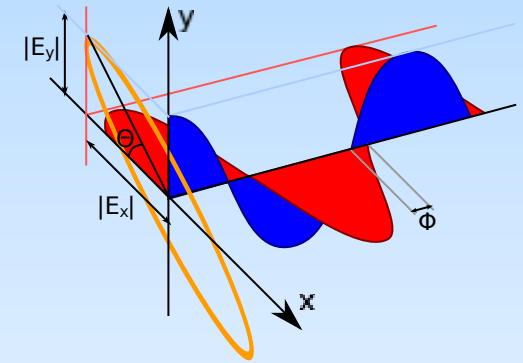


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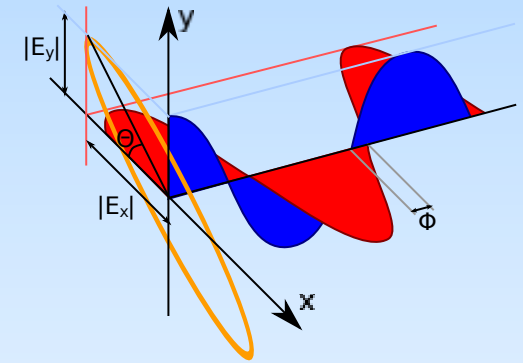


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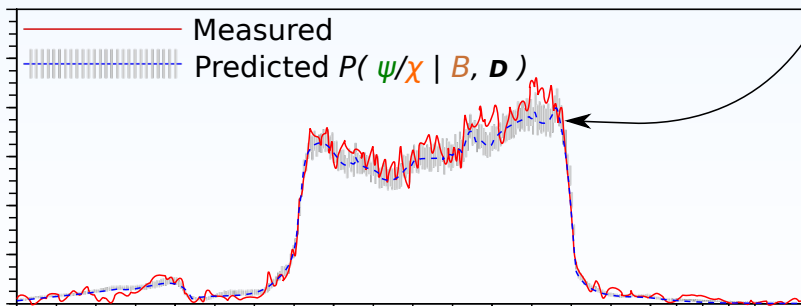
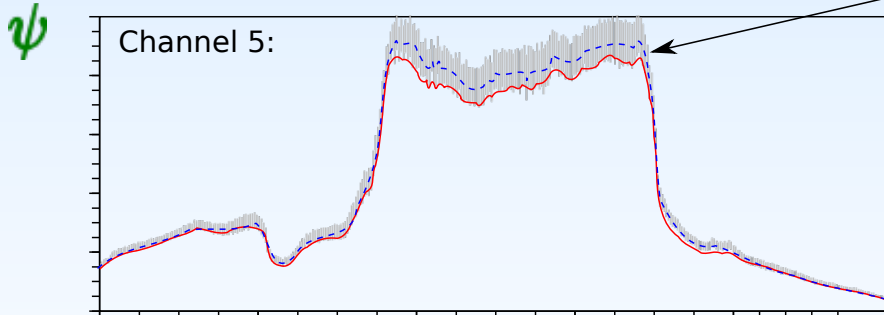
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Grey bands represent  $2\sigma$  of  $P(\psi/\chi | \mathbf{B}, \mathbf{D})$ . Despite large variation in  $n_e$  profiles used, predictions are well determined.



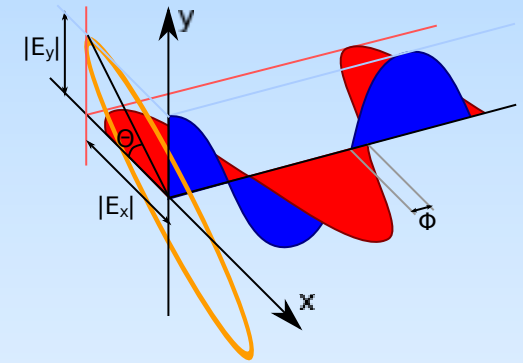


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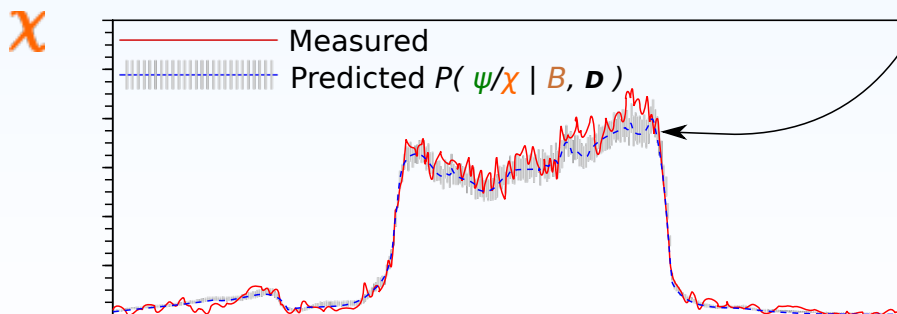
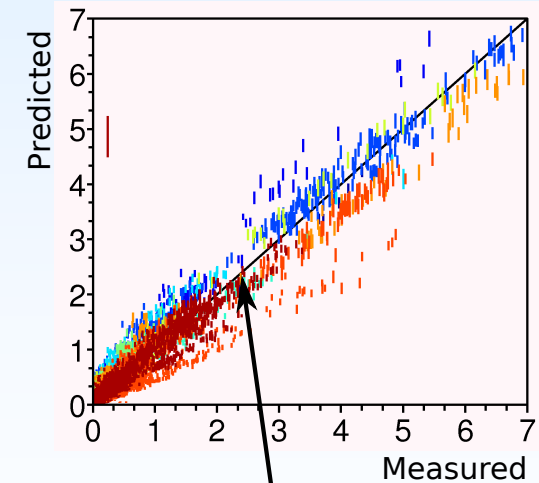
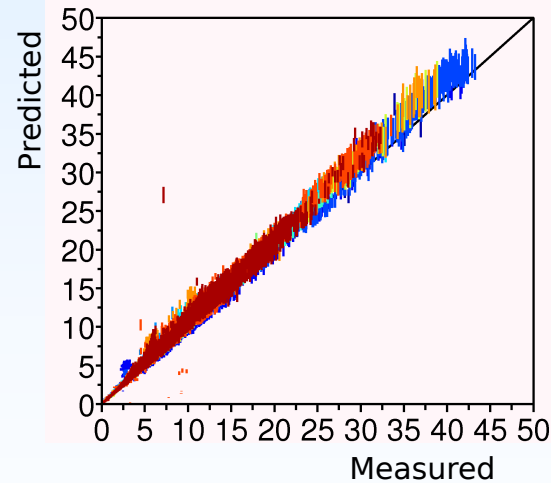
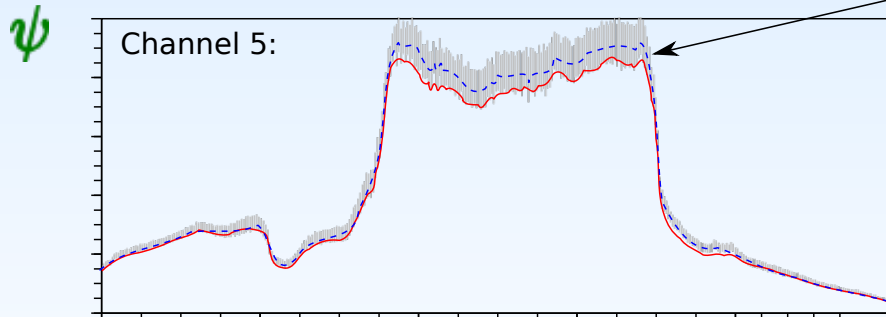
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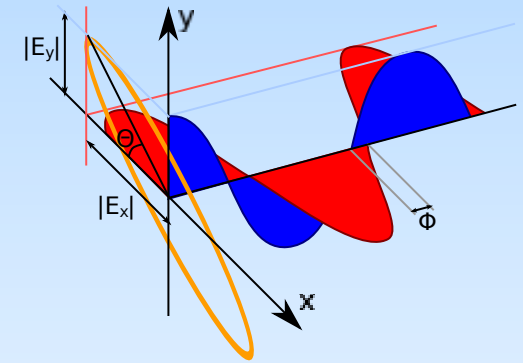
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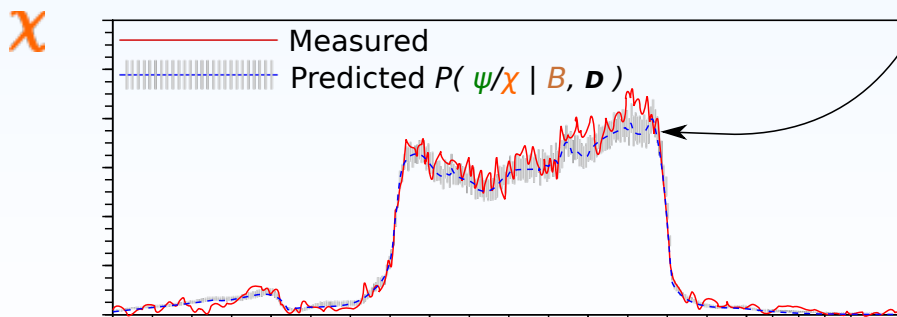
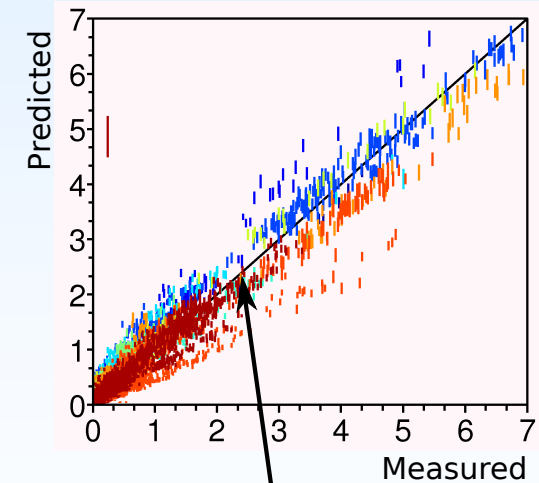
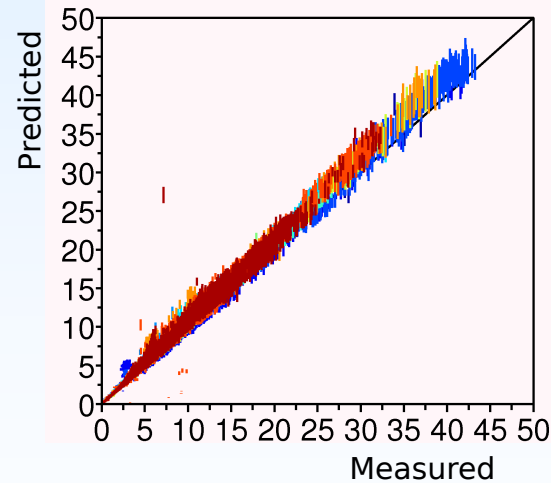
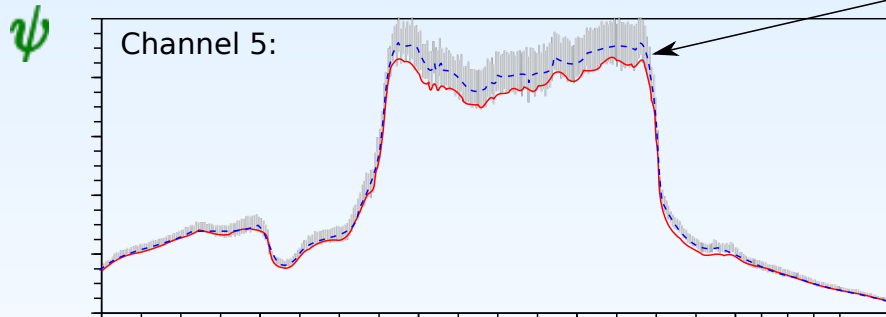
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Often,  $\psi$  and  $\chi$  approximated by 'Faraday' and 'Cotton-Mouton' effects, each valid in specific cases not generally true on JET. **Lots** of effort spent trying to 'correct' the calculations back to the full model. Leads to confusing mix of terminology and unnecessary inaccuracy that gets confused with real diagnostic uncertainty.

## Polarimetry II - High Temperature Models A

As well as 'cold plasma' model (fluid approx), two papers gave 'corrections' for high- $T_e$  effects (quoted as large for  $T_e > \sim 5\text{keV}$ ) derived from kinetic theory.

- a) S.E. Segre (2002): Argues **non-relativistic** kinetic approximation is sufficient.
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- We should be able to test, but...

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For core (high- $T_e$ ) channels, measurement and prediction for cold plasmas differ systematically over entire pulses and campaigns. Partly due to inaccurate knowledge of  $\mathbf{B}$  (from magnetics EFIT here), but diagnostic behaviour is not fully understood (optics etc) and the calibration varies significantly.

**Uncertainty due to calibration is much larger than model differences and is systematic for entire pulses:**

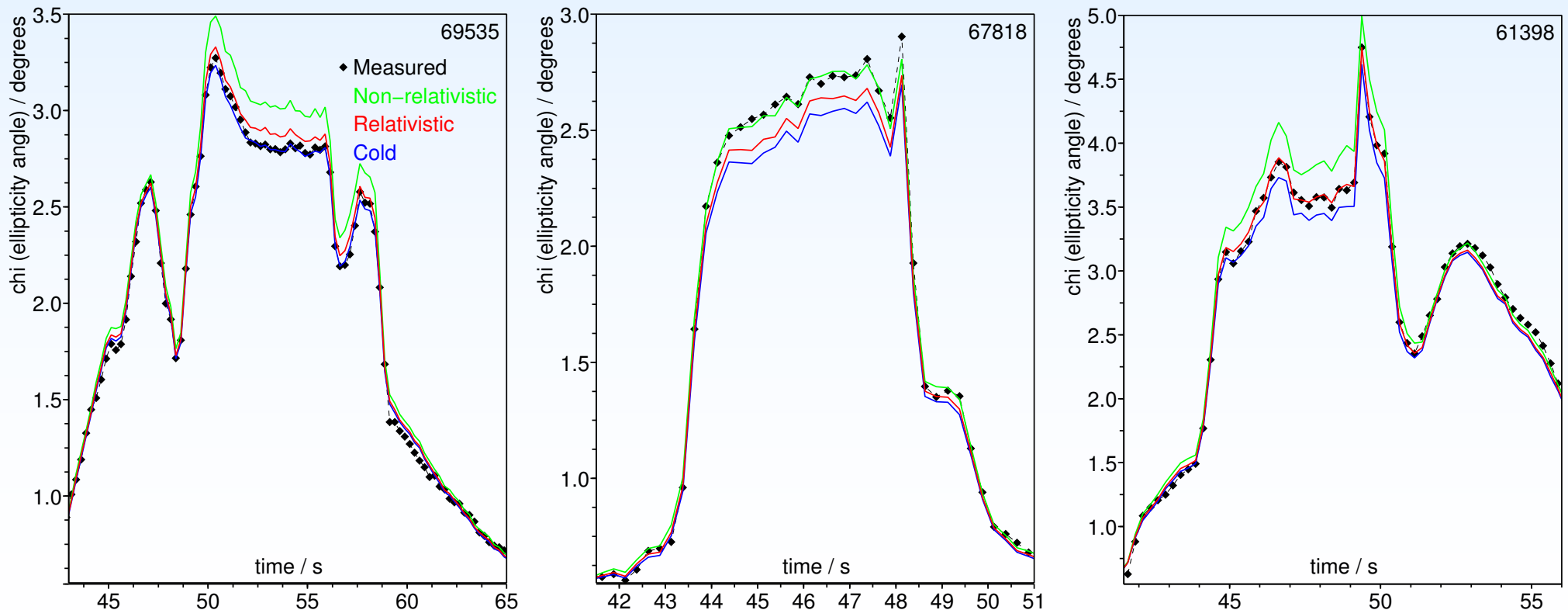
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Can easily find pulses that agree with any model.

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Solutions: Run session of pulses at very high  $T_e$  to get  $\sim 10$  pulses with effect bigger than uncertainty?



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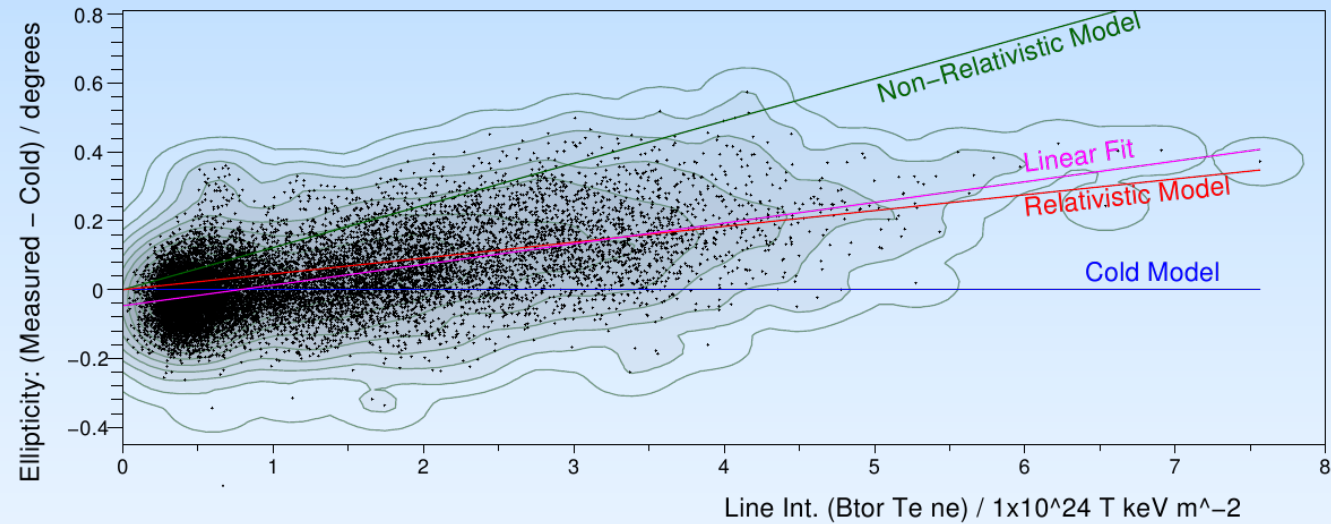
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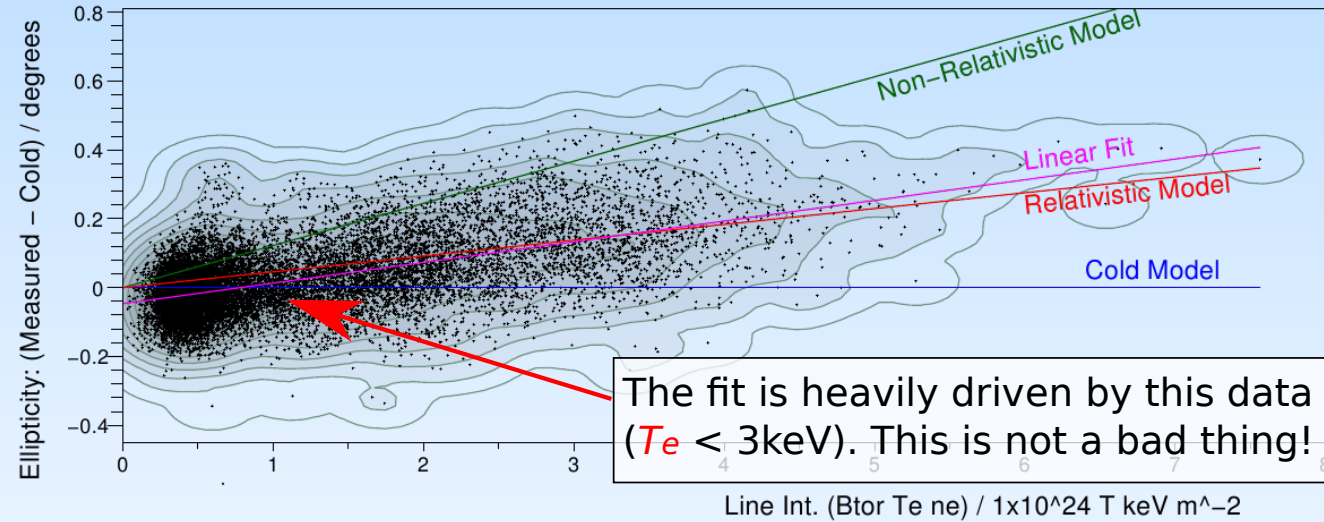
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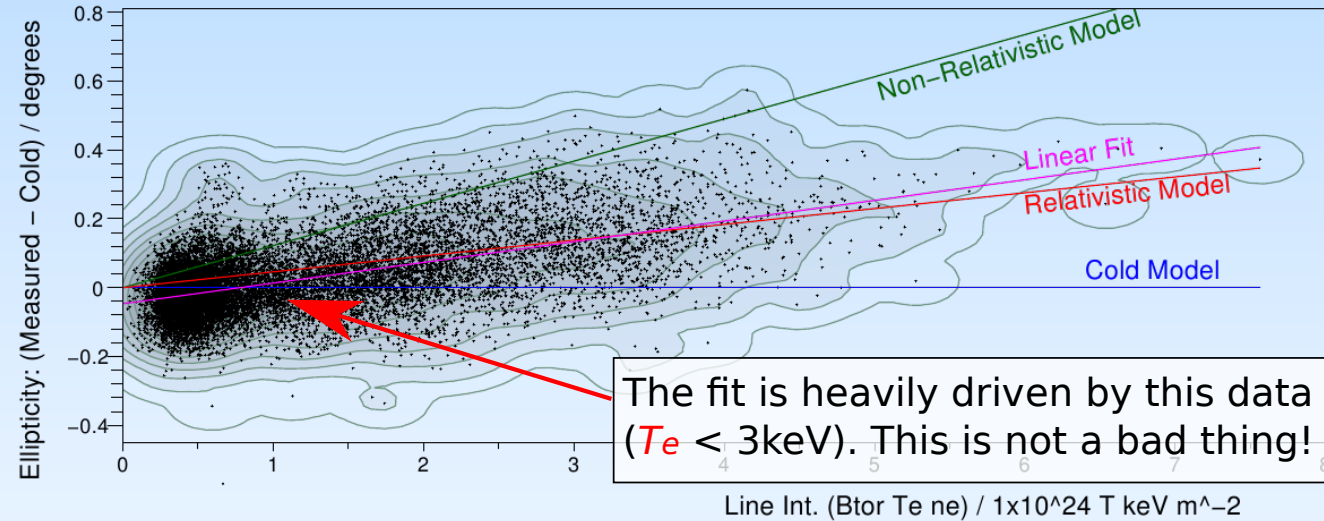
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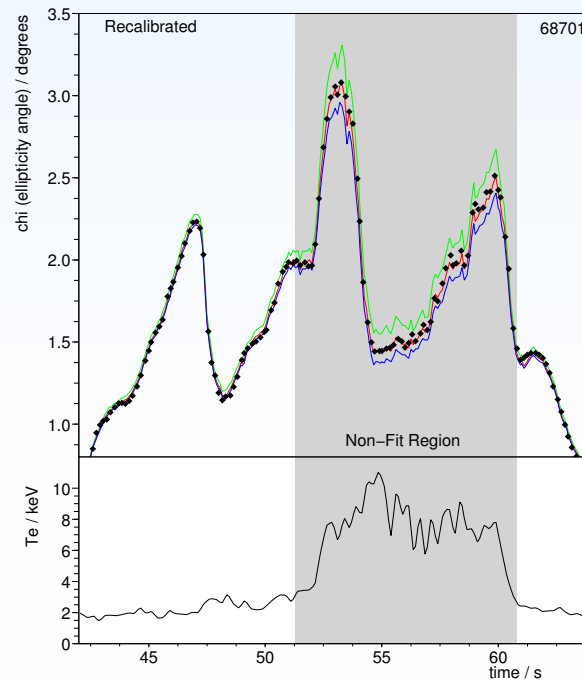
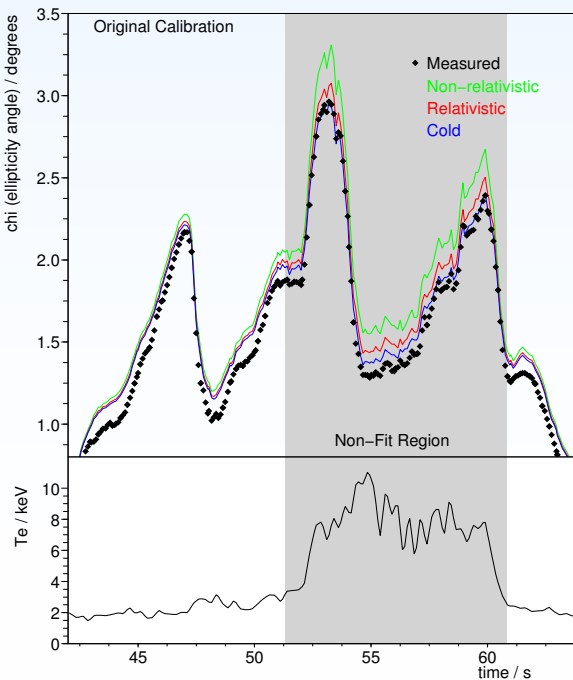
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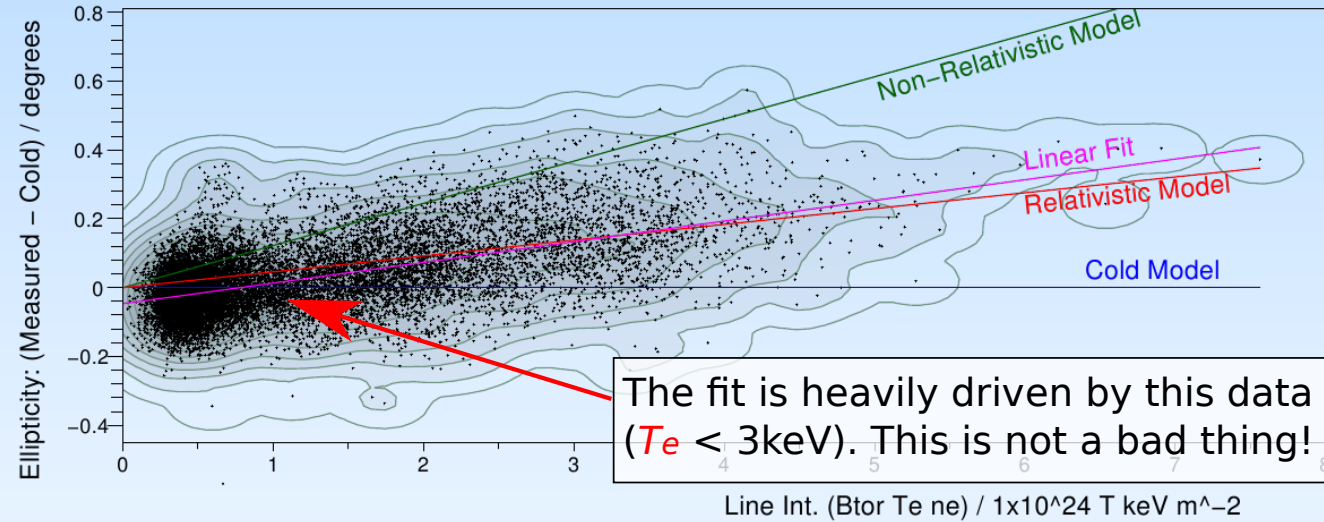


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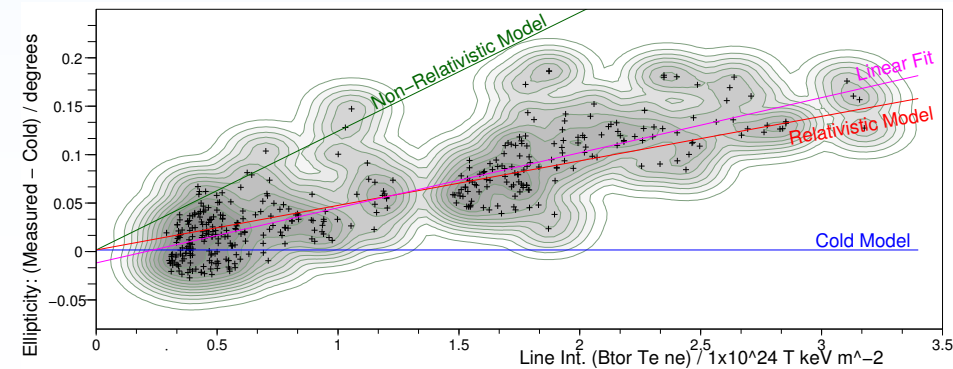
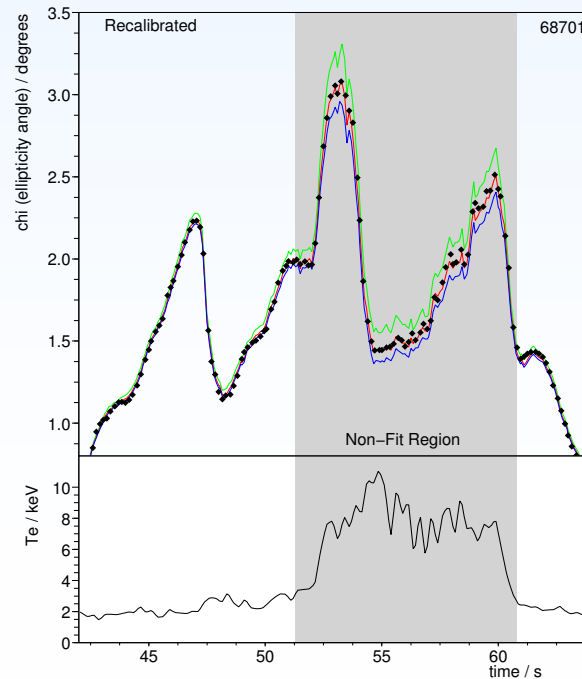
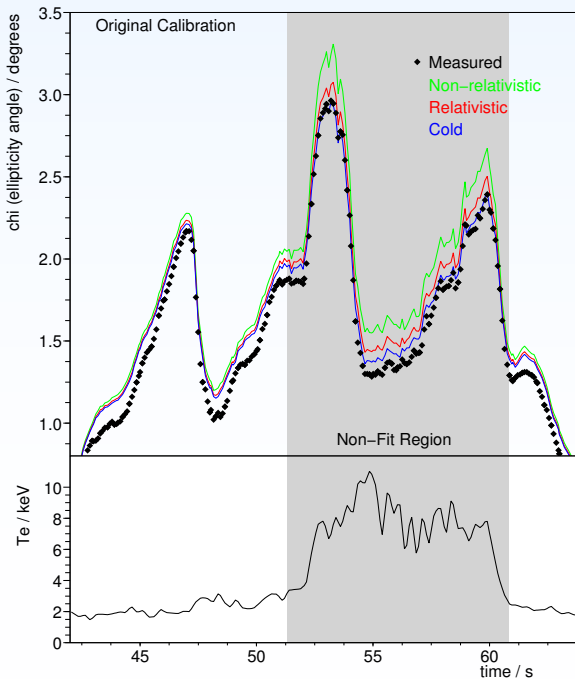
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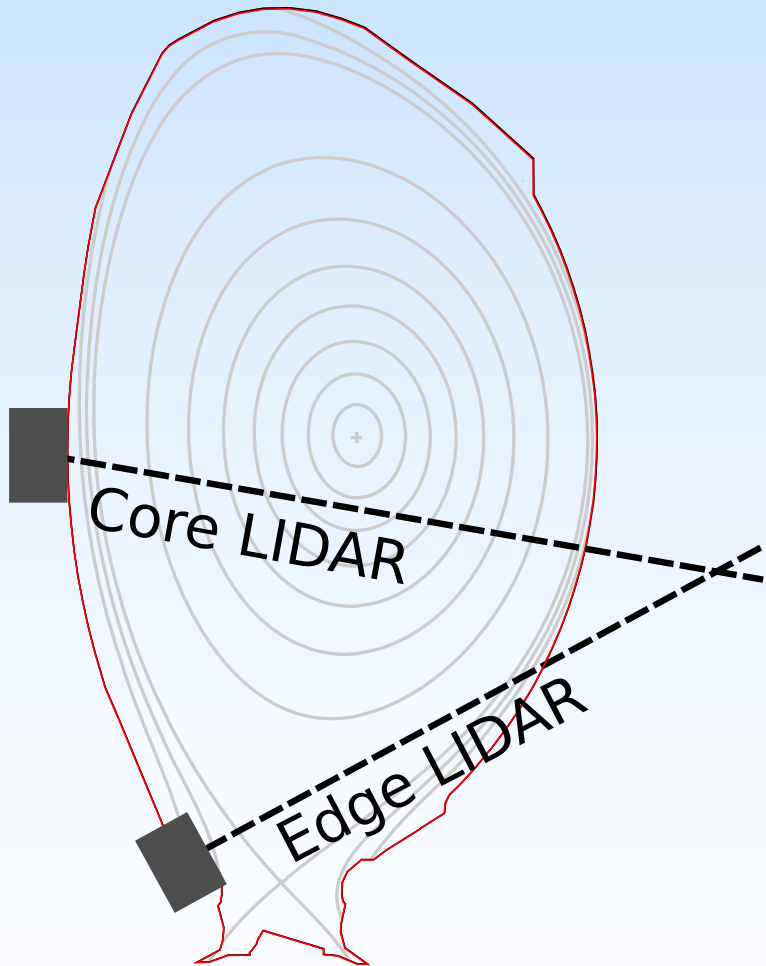
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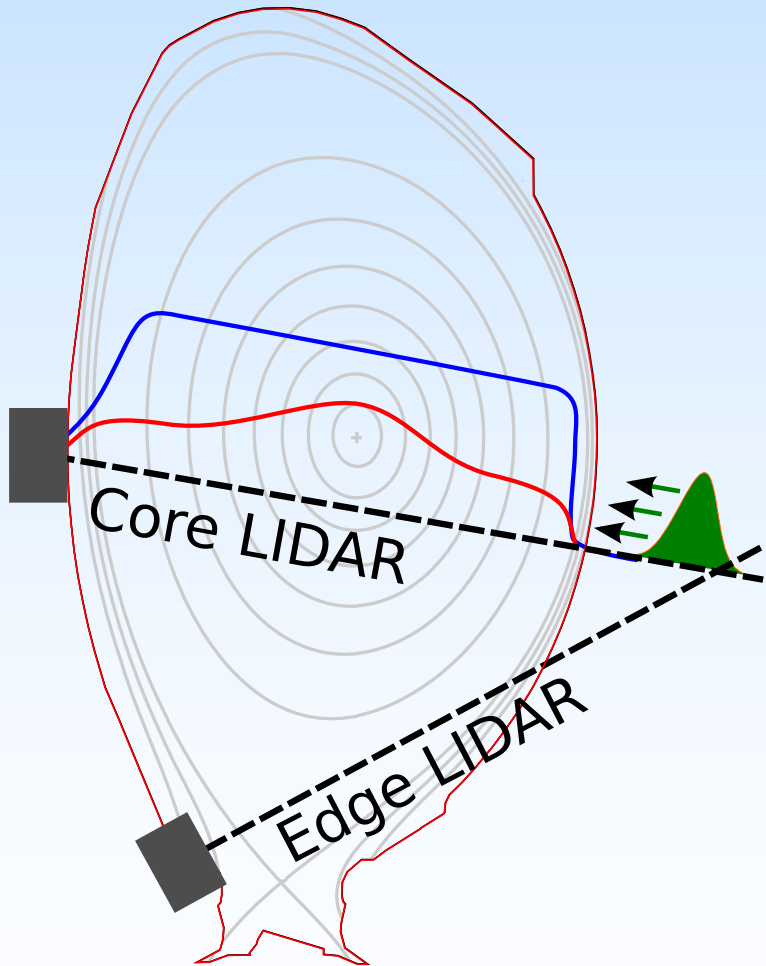
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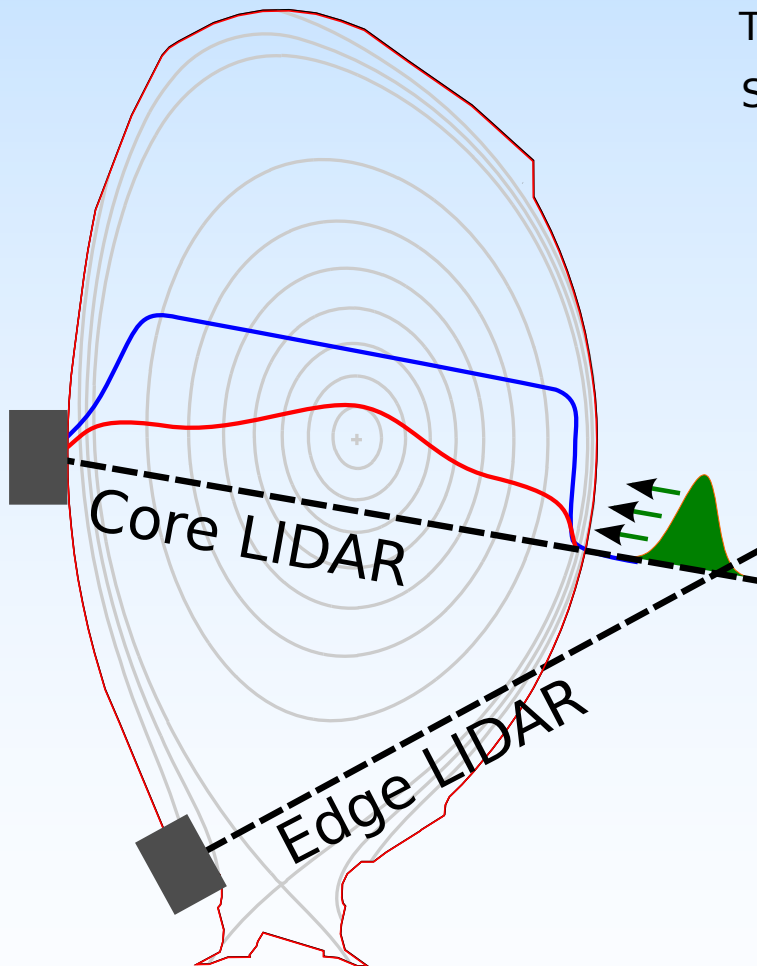
TS physics well understood but hardware system very complex.

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Effective convolution of light signal.

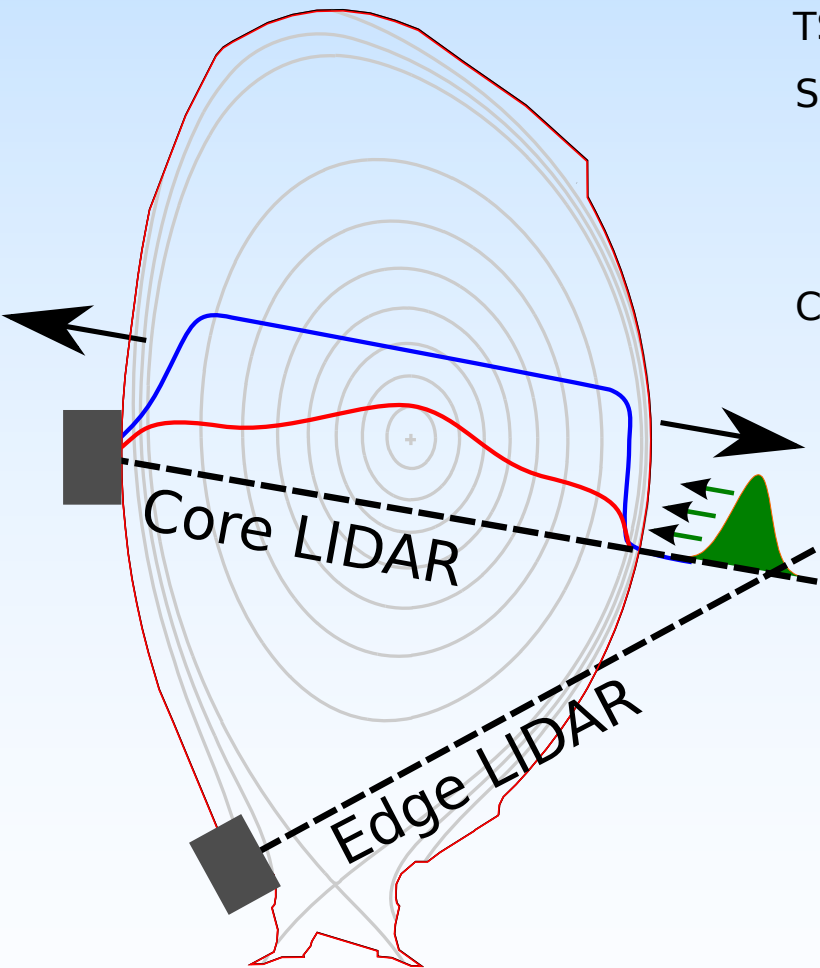
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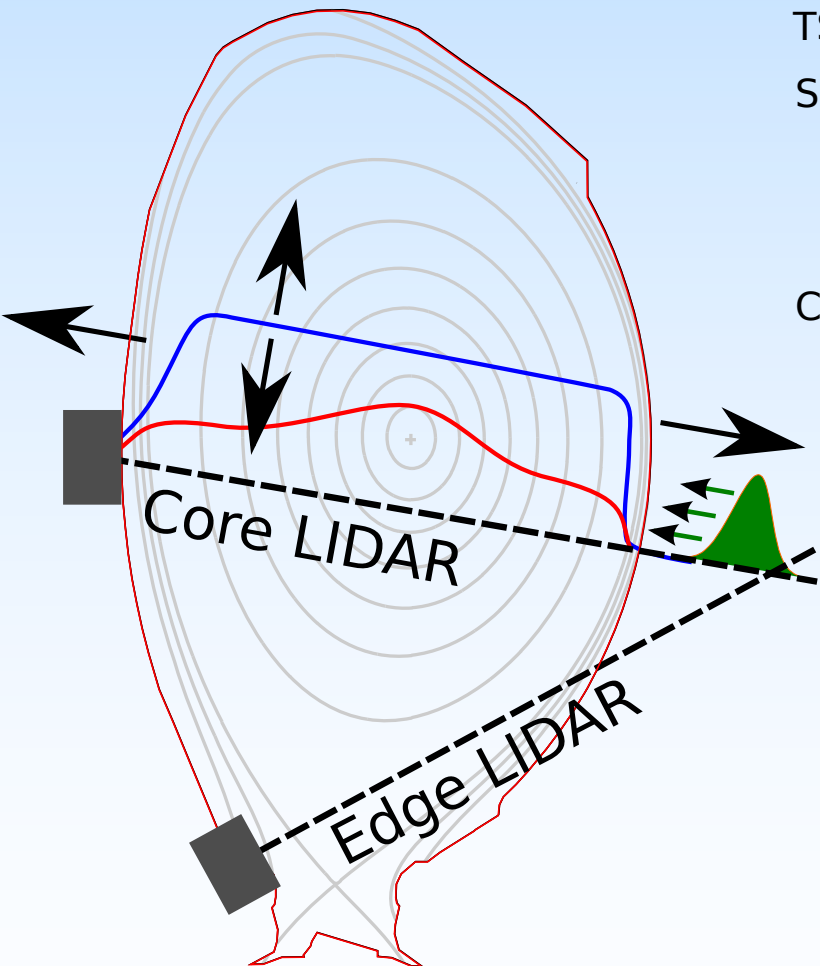
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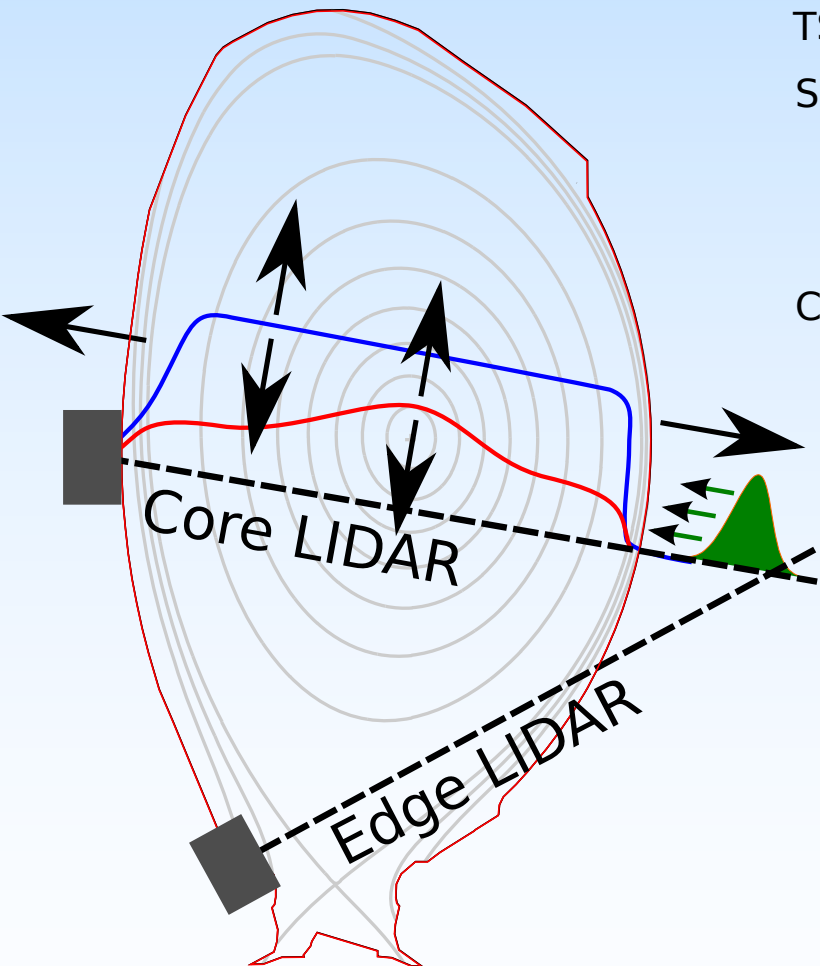
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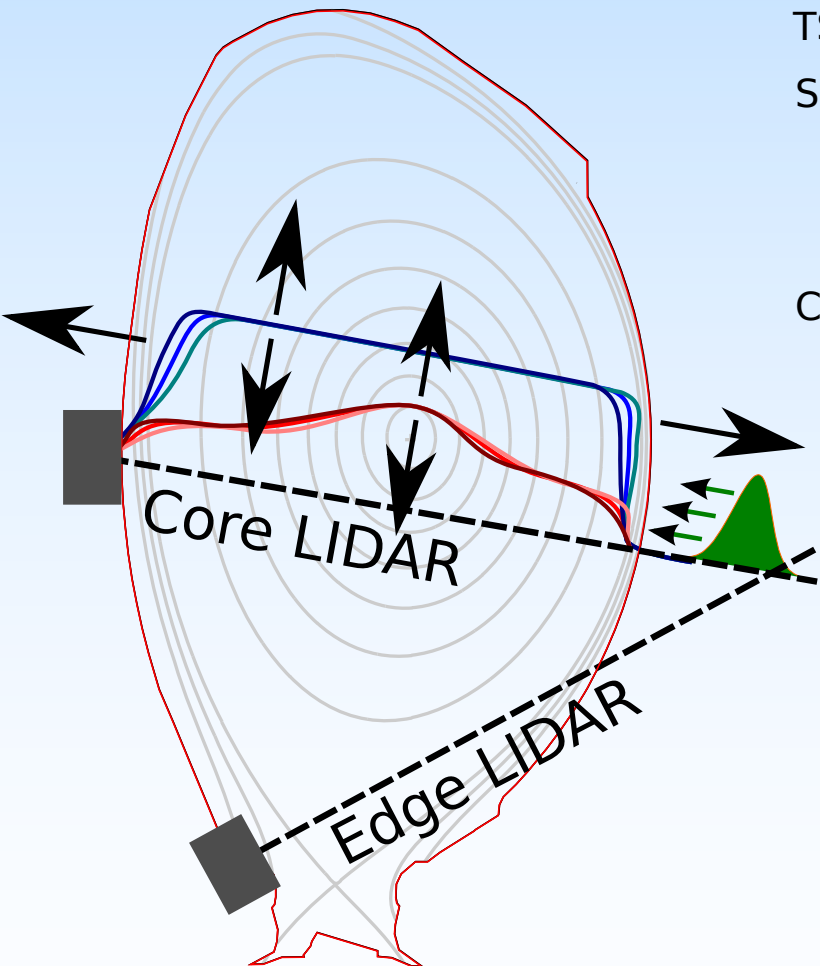
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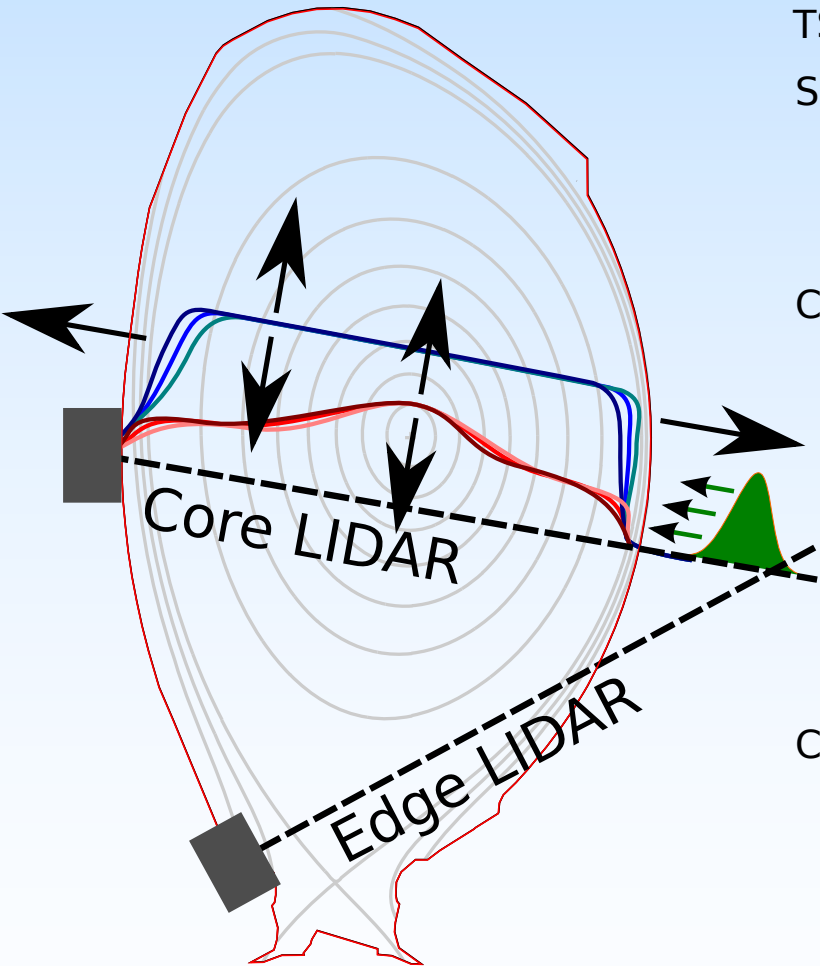
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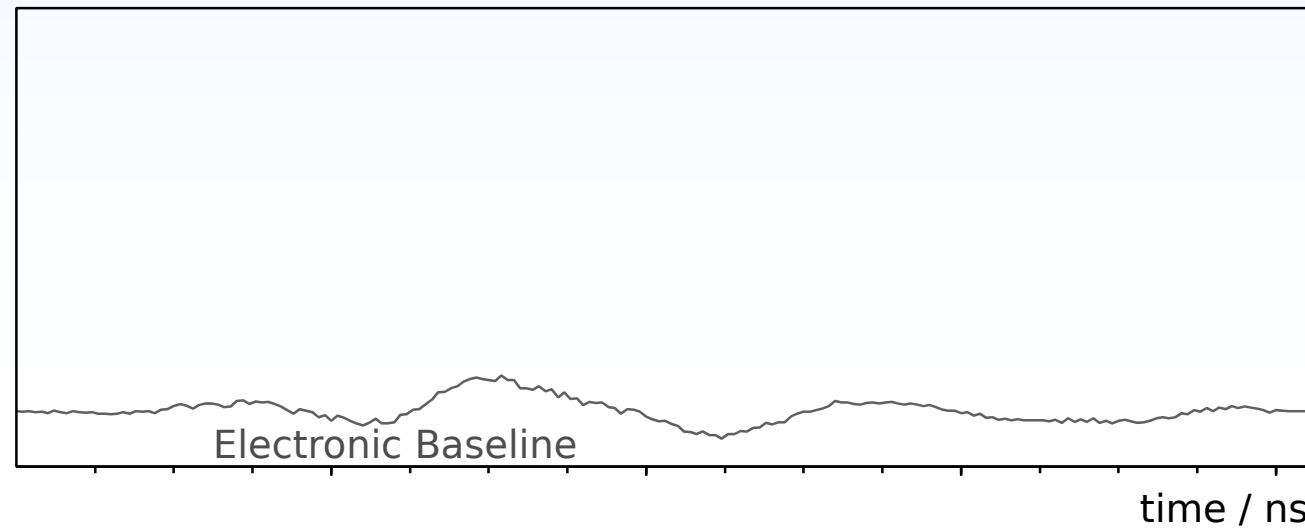
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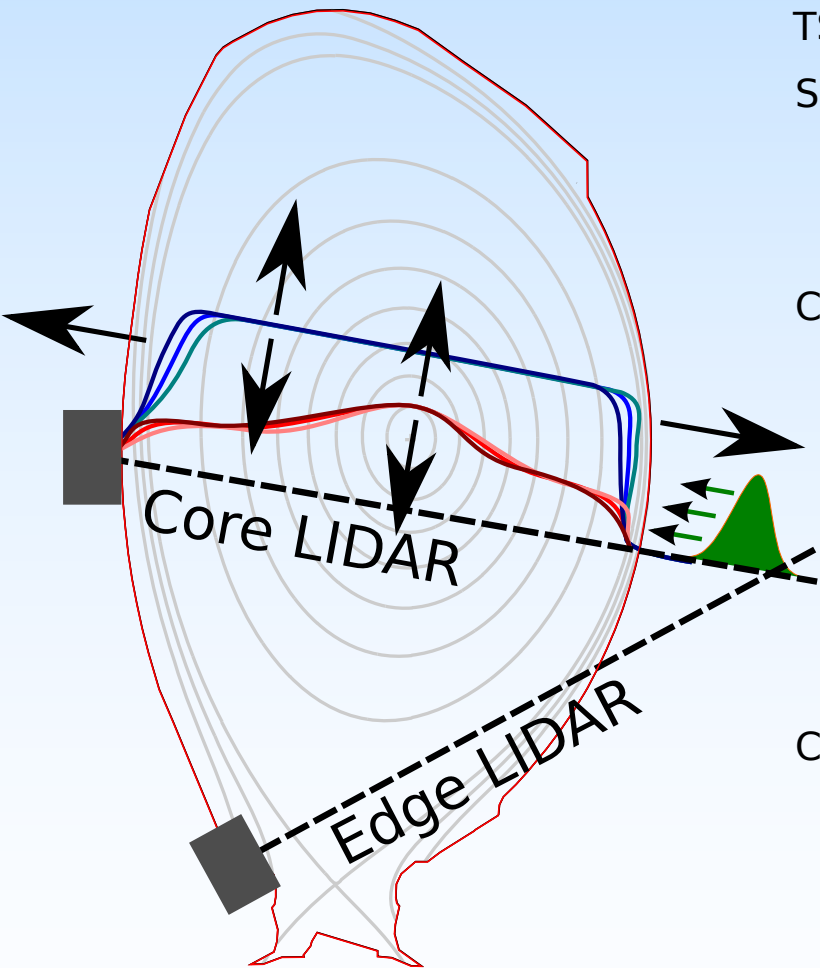
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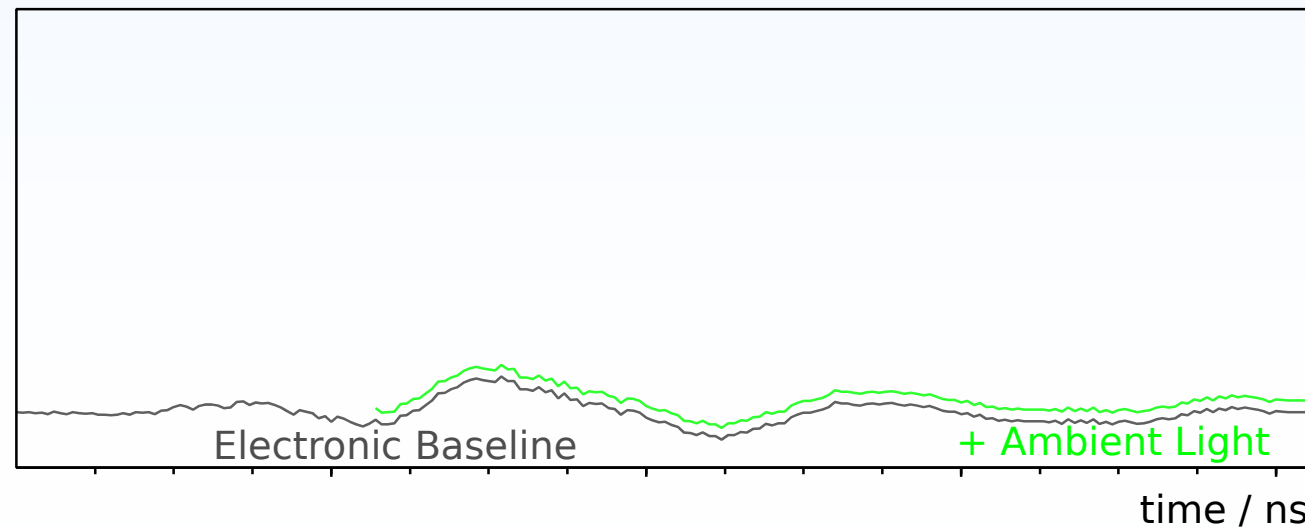
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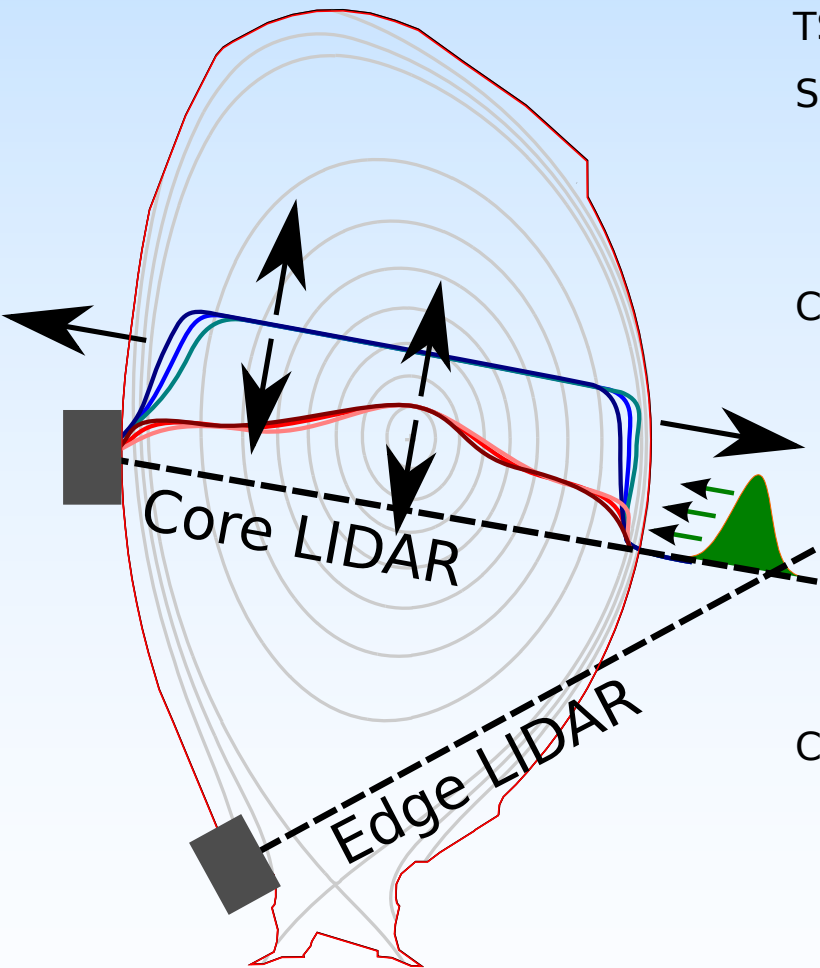
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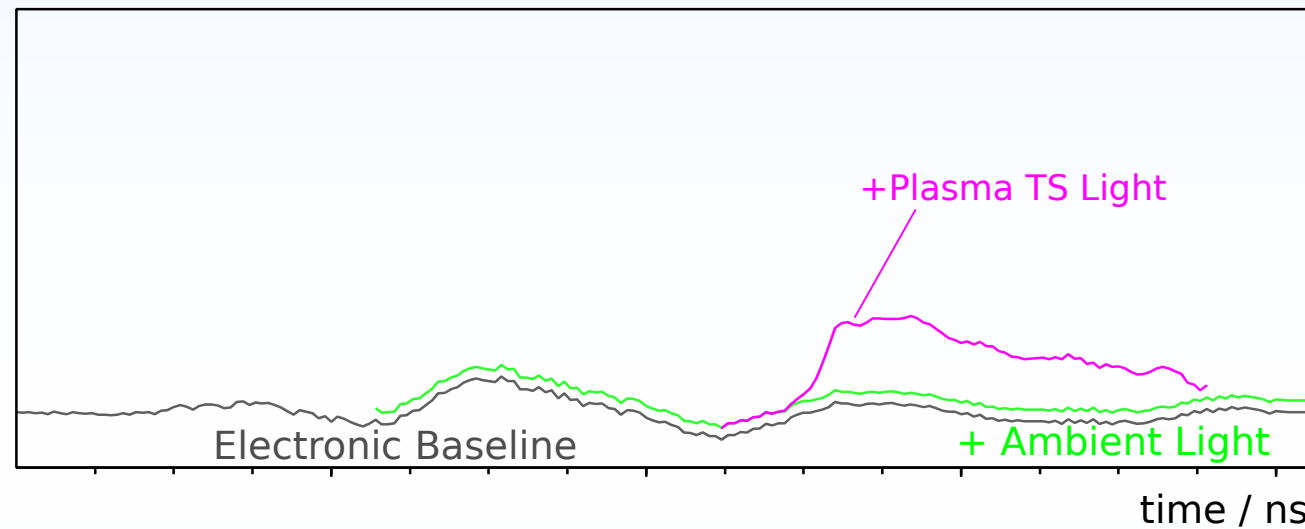
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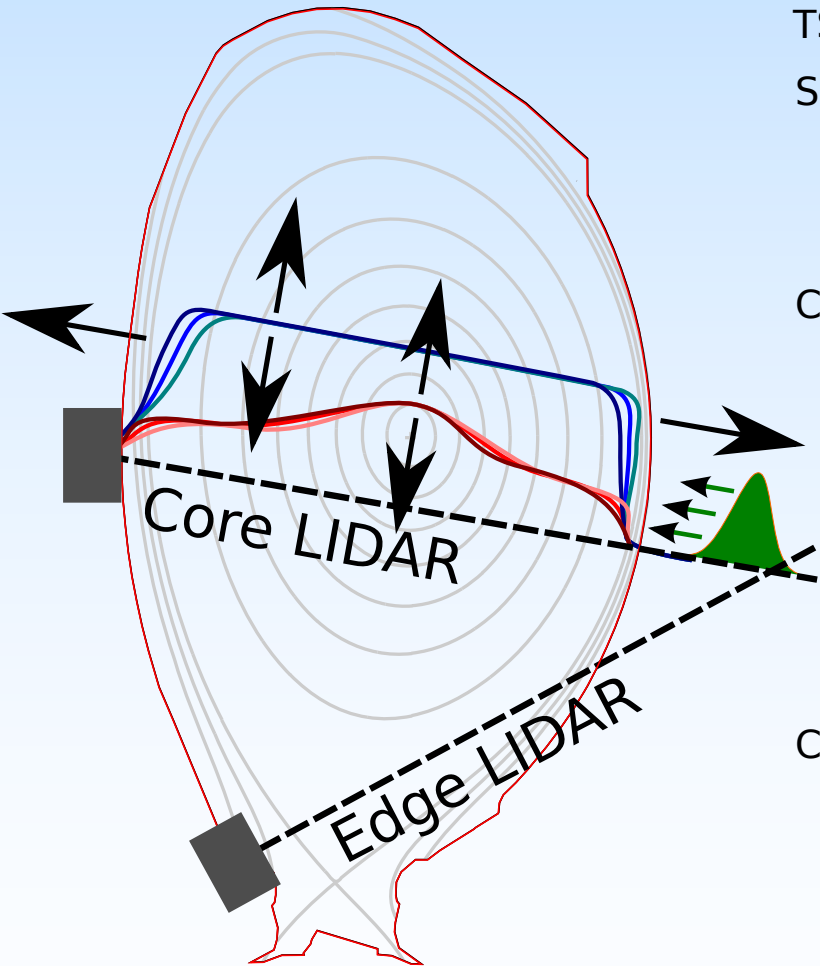
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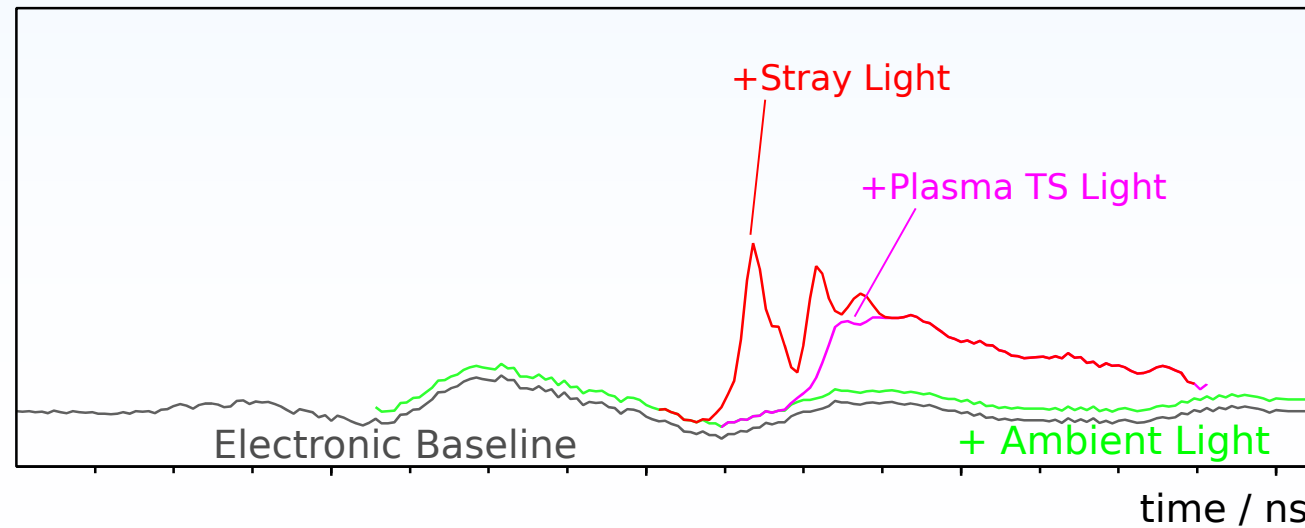
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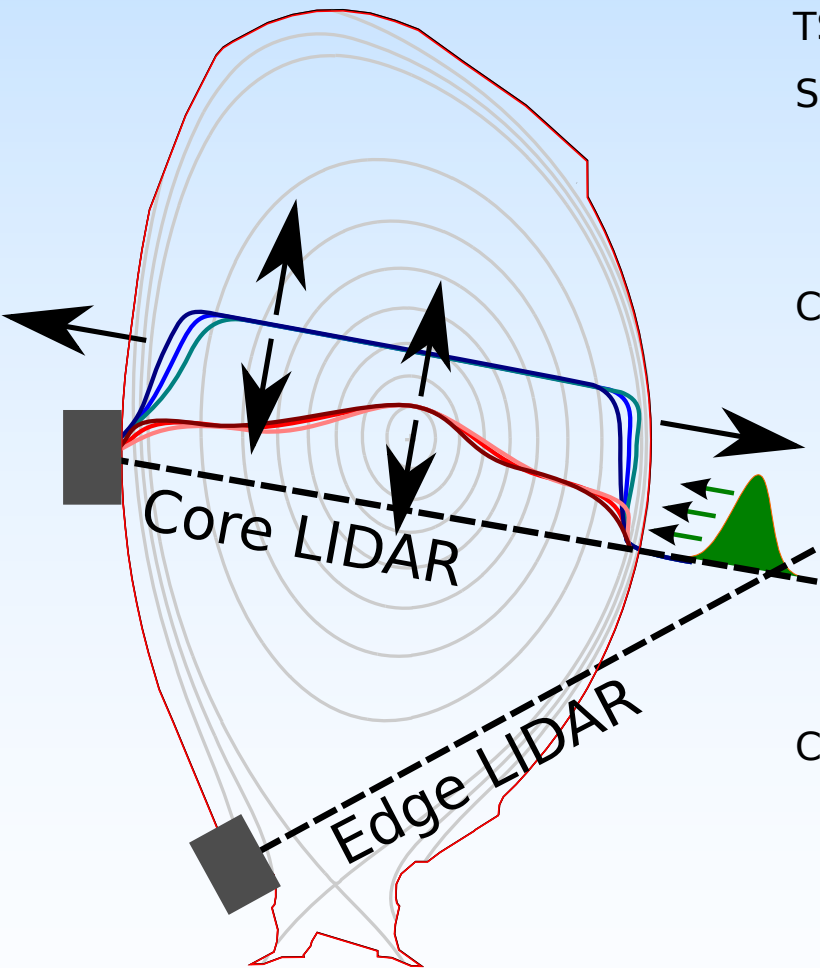
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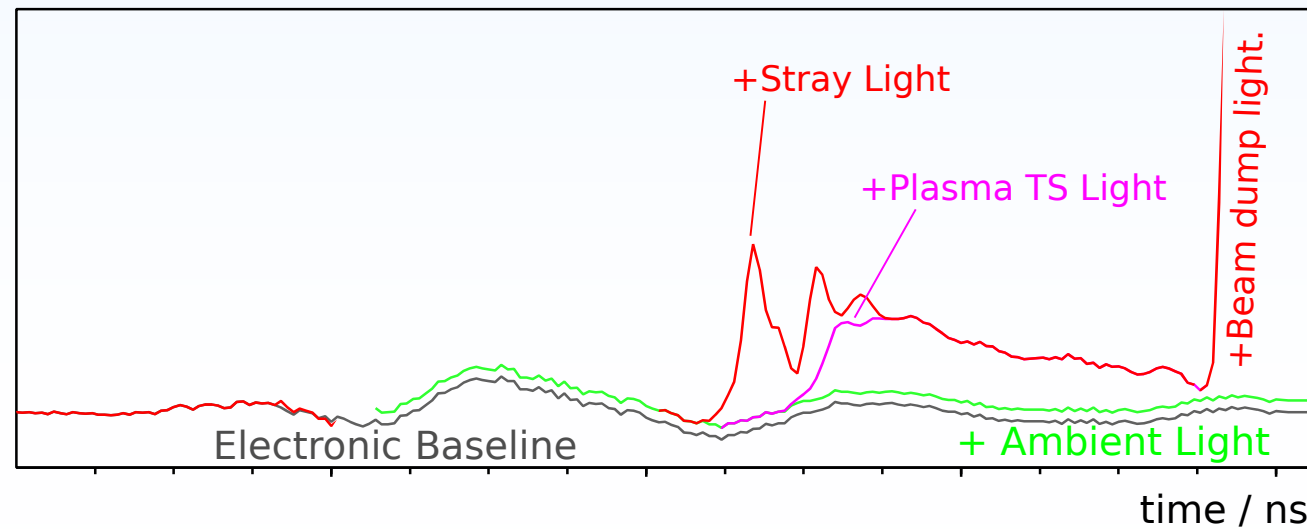
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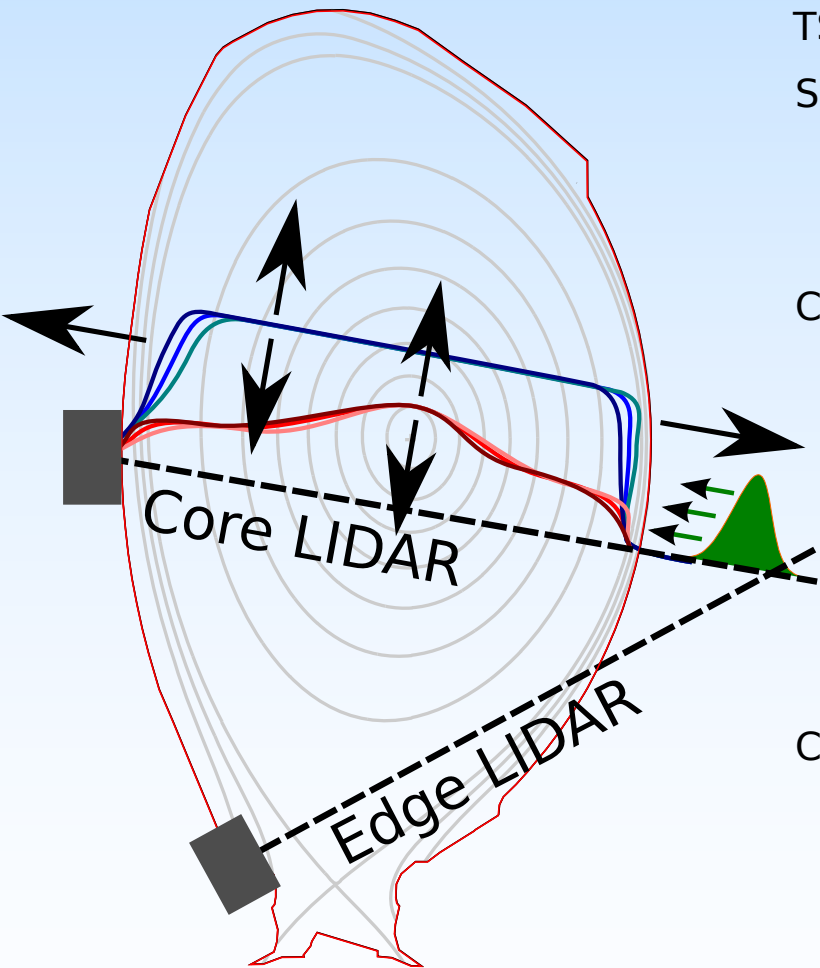
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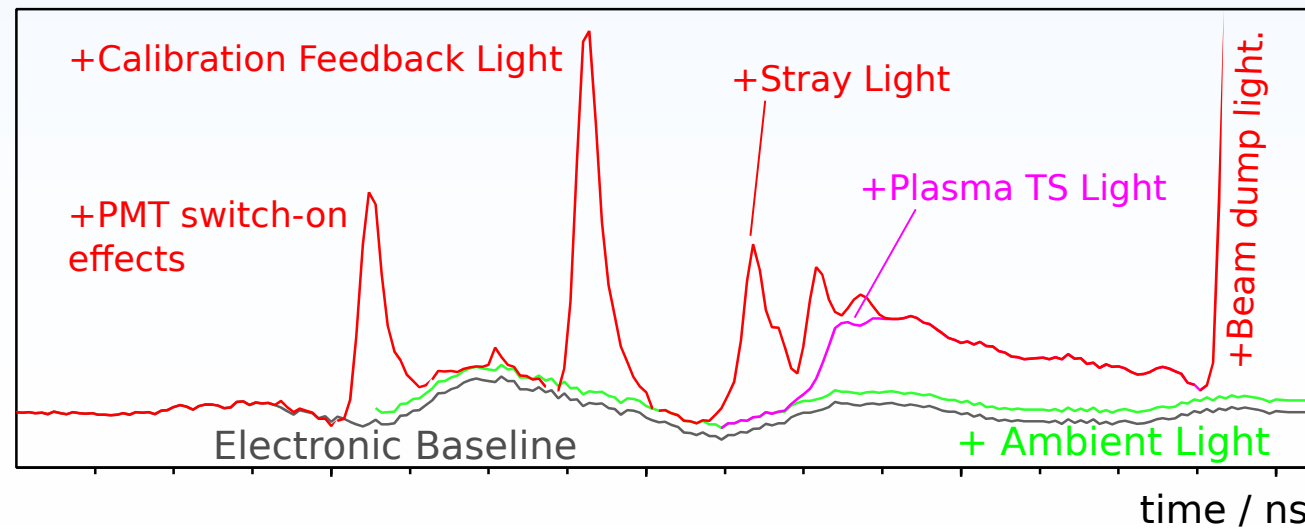
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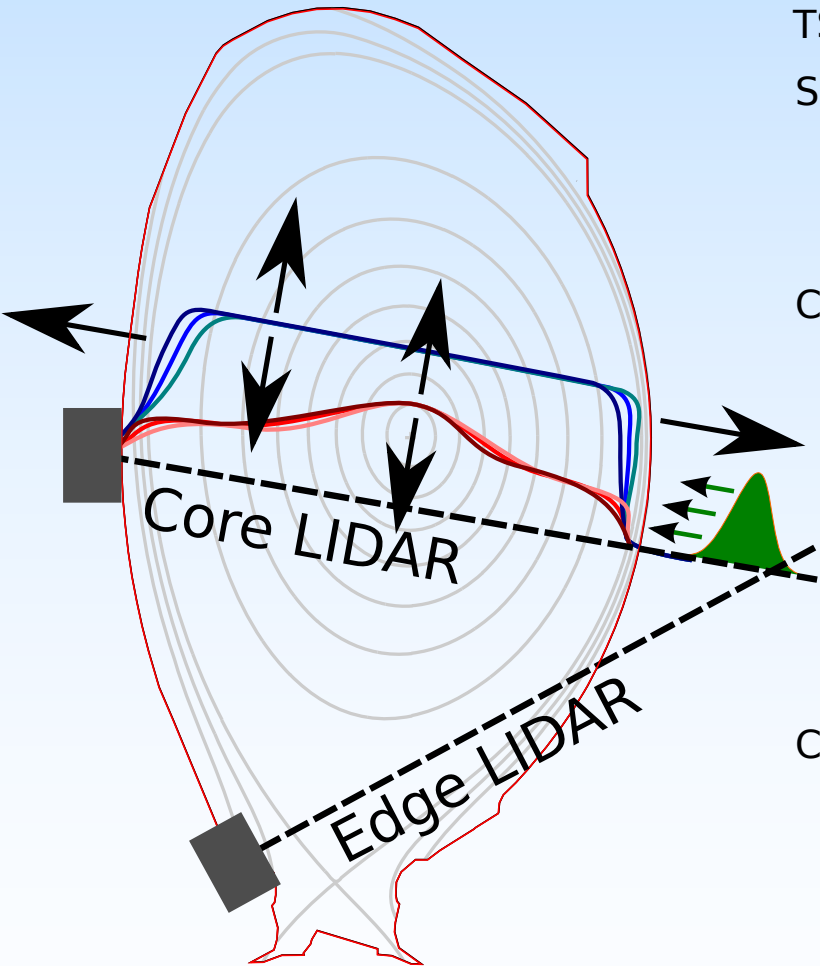
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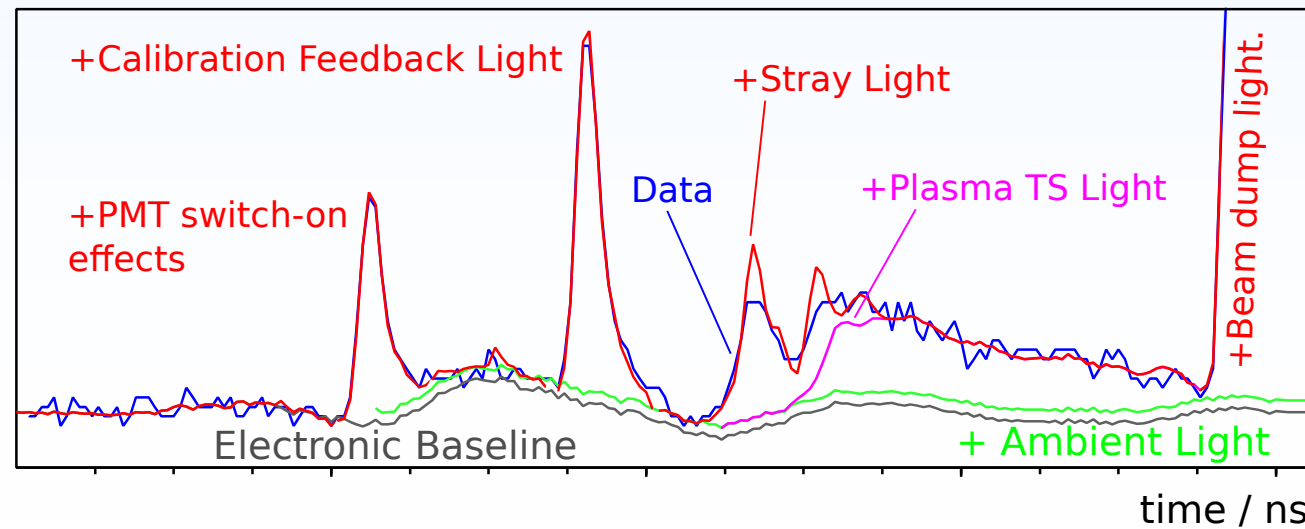
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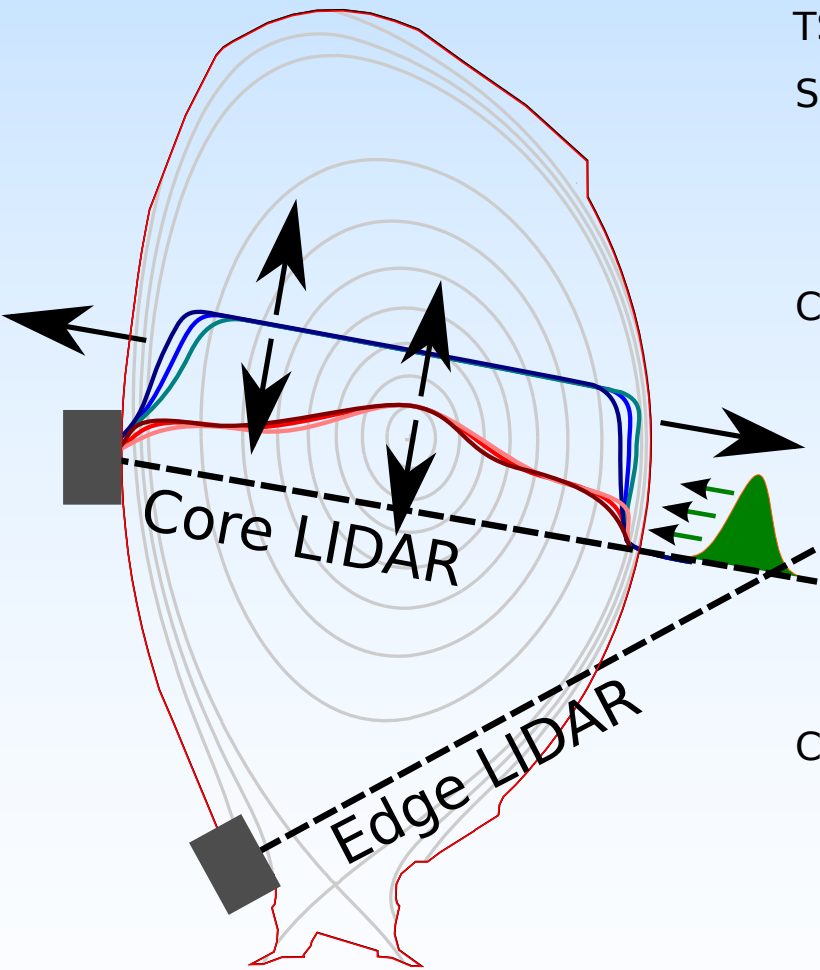
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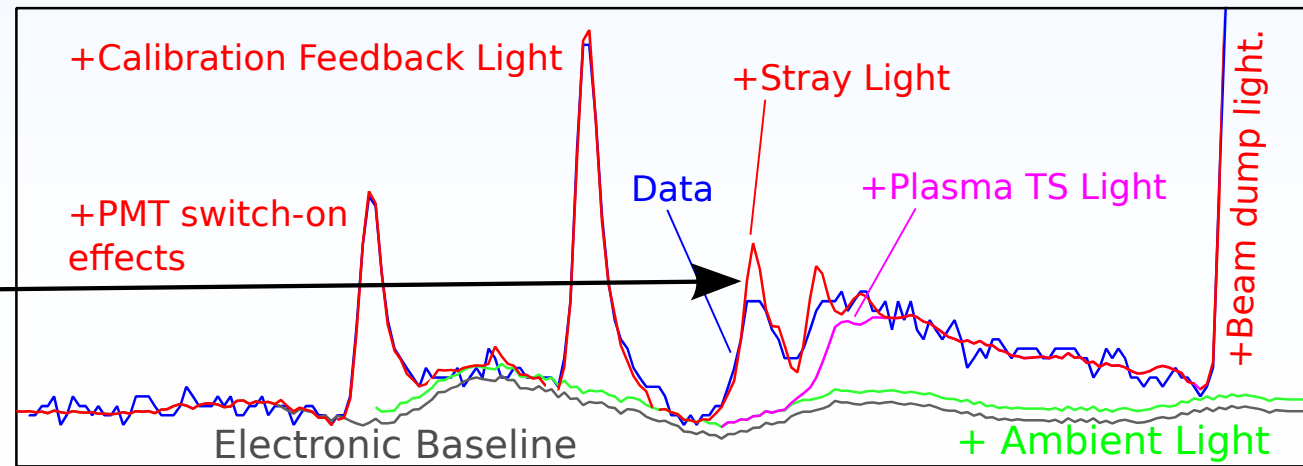
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Stray light effects low signal (low  $n_e$ ) data on both systems but is **vital** for proper edge LIDAR analysis.



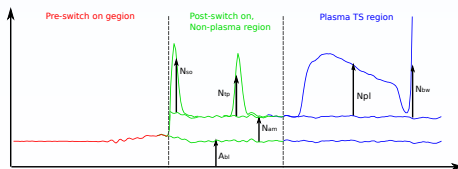
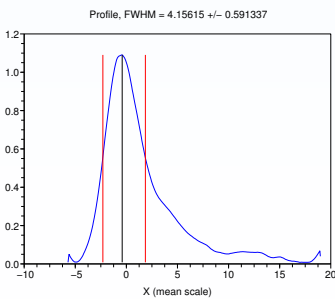
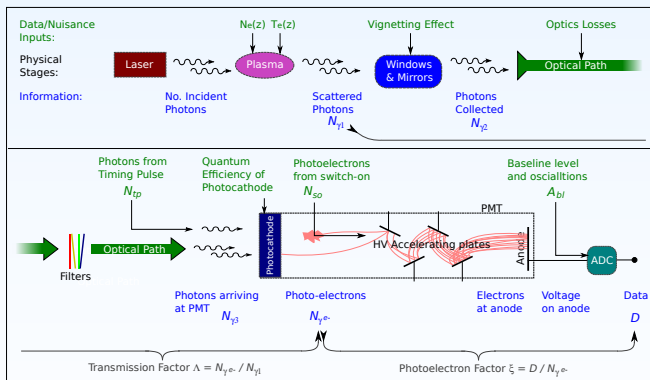
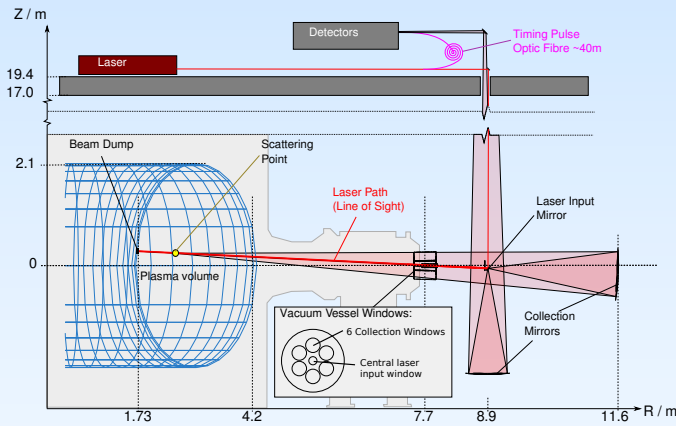
time / ns

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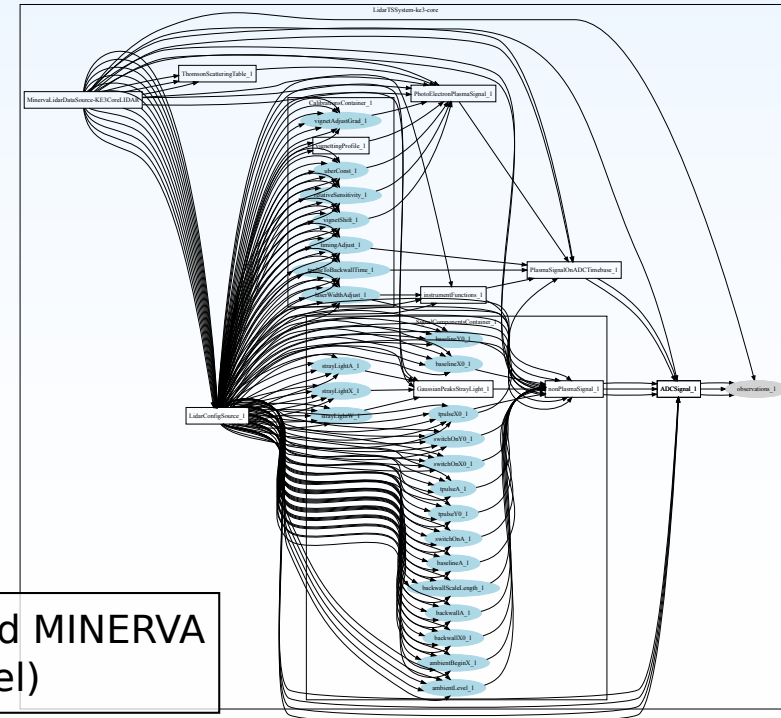
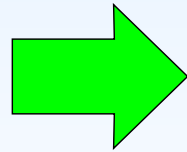
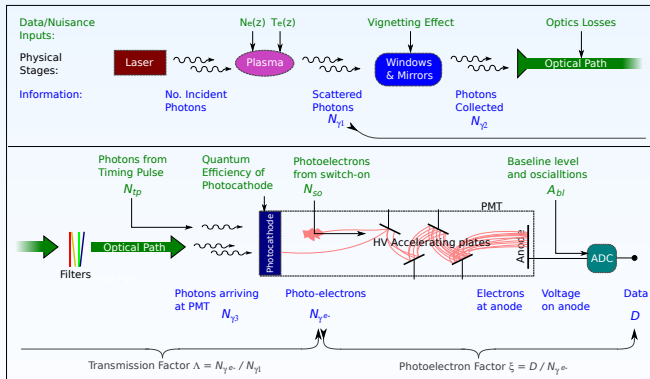
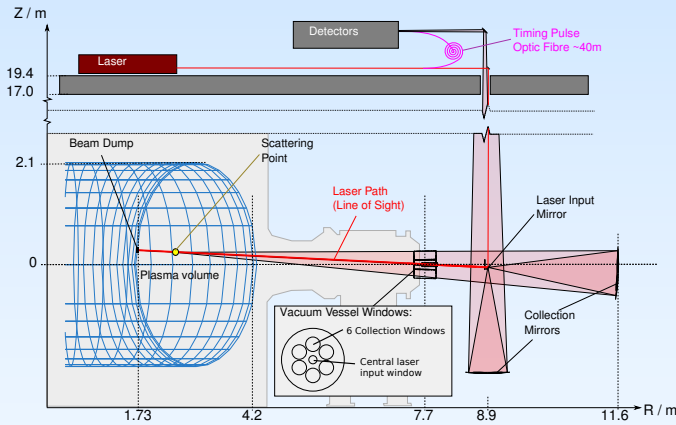


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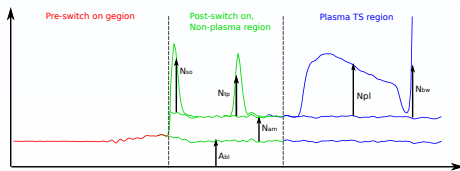
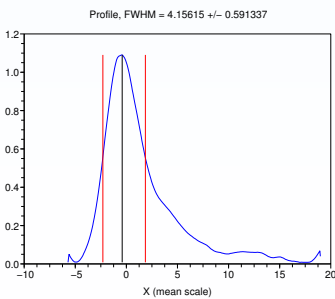
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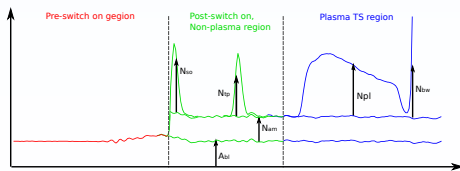
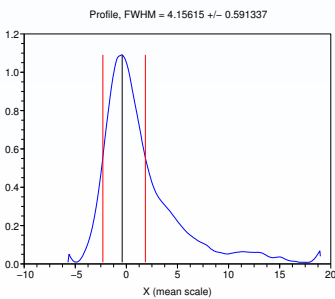
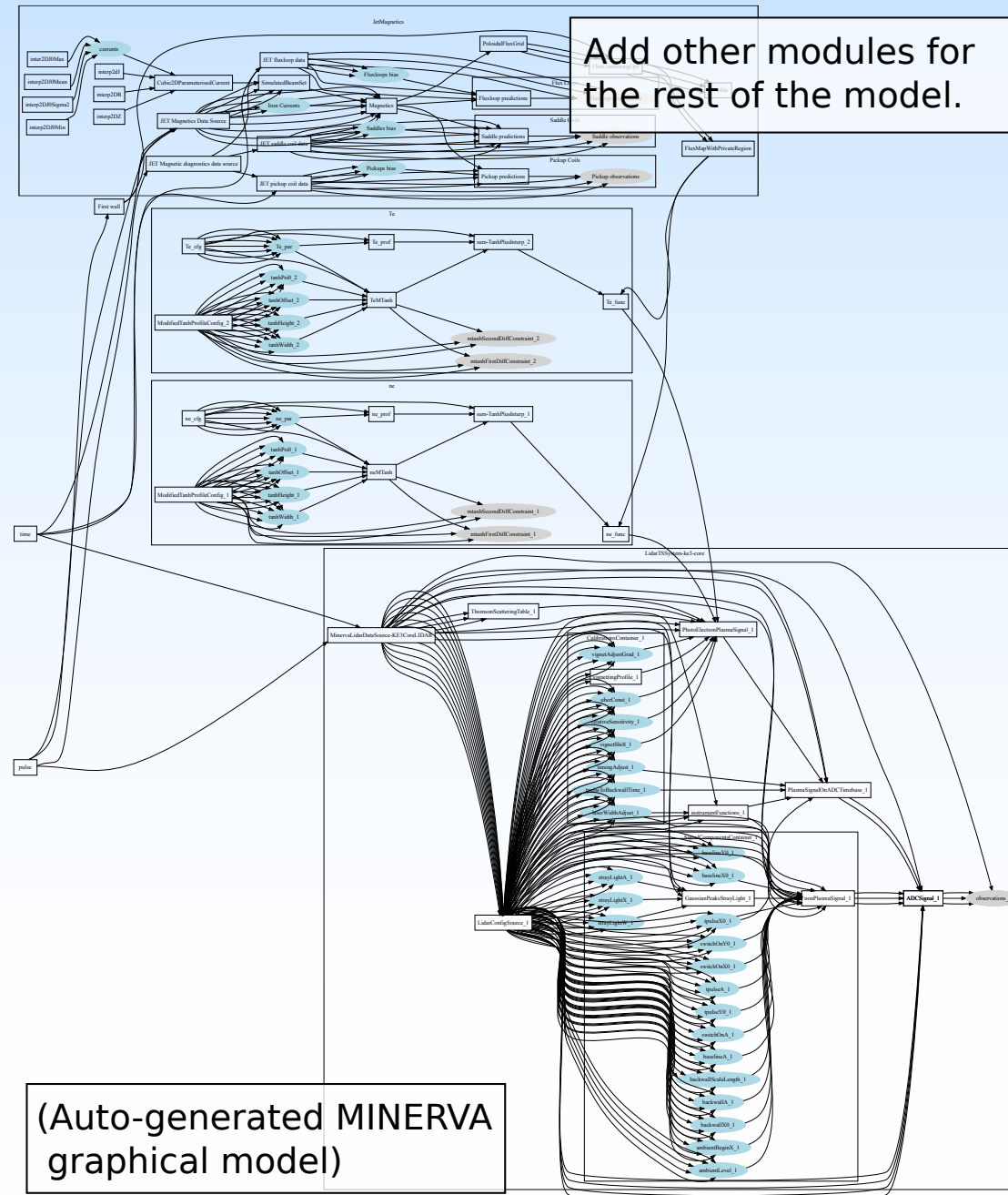
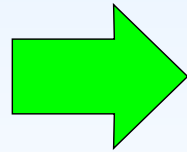
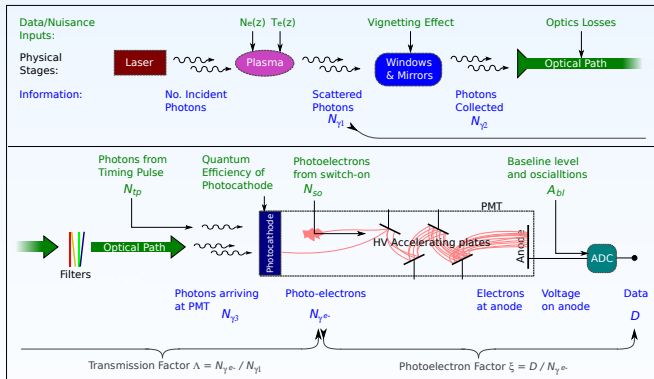
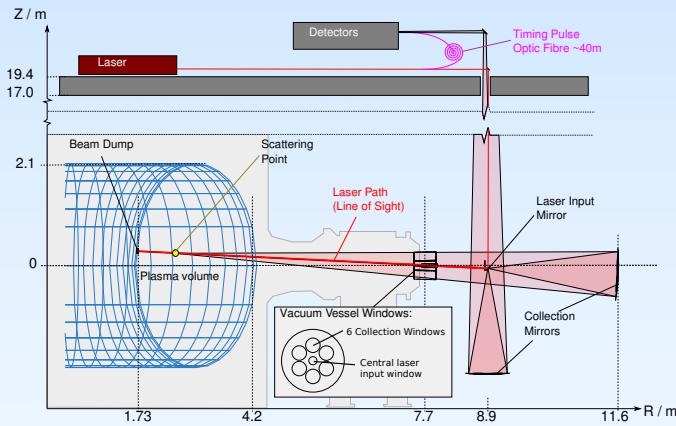




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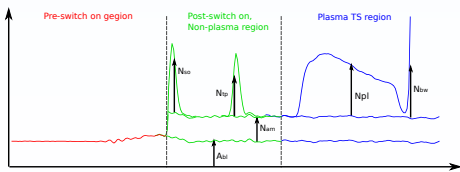
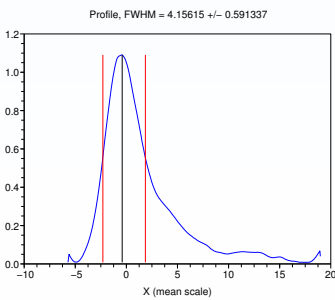
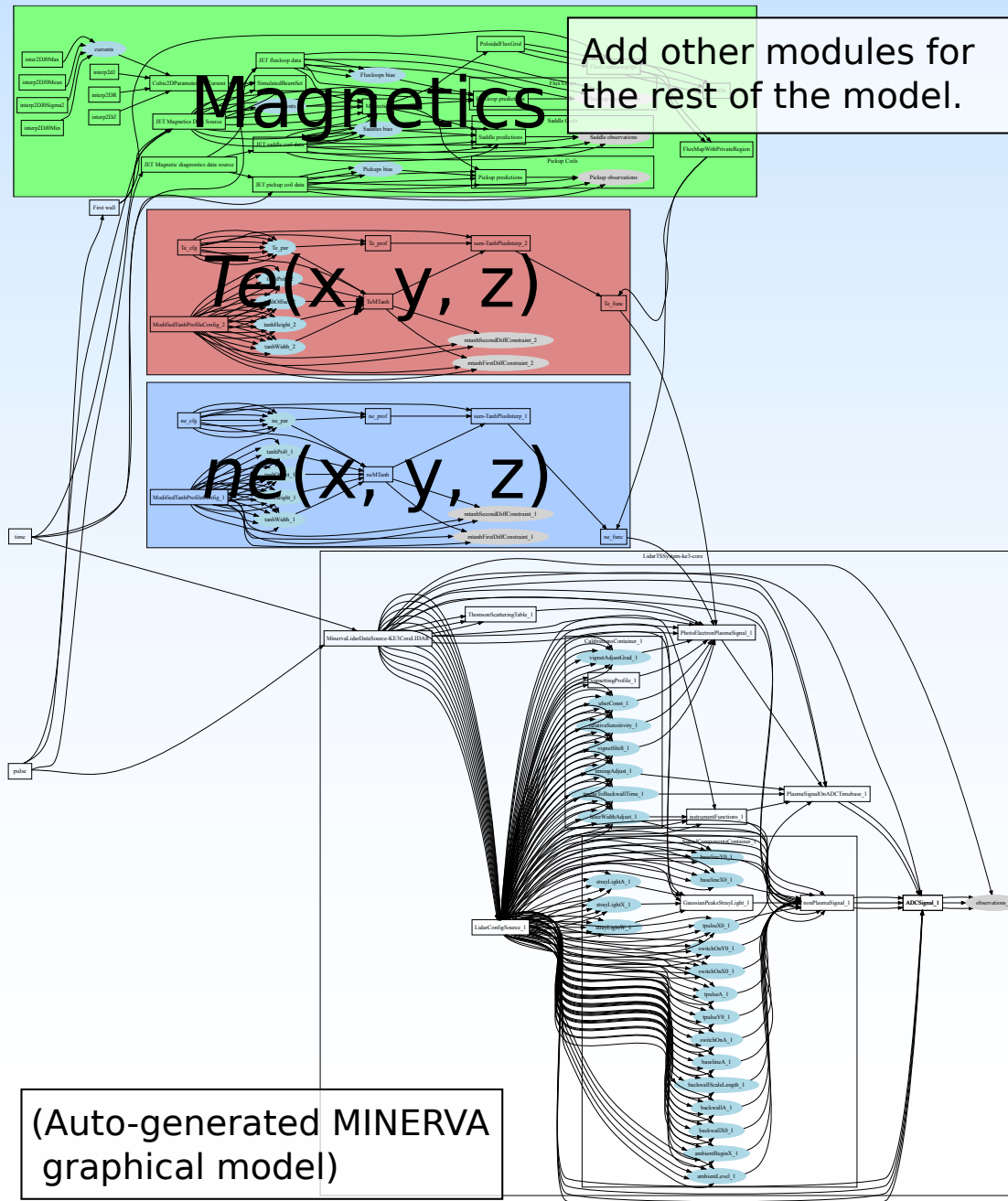
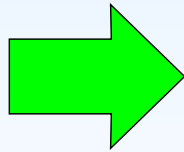
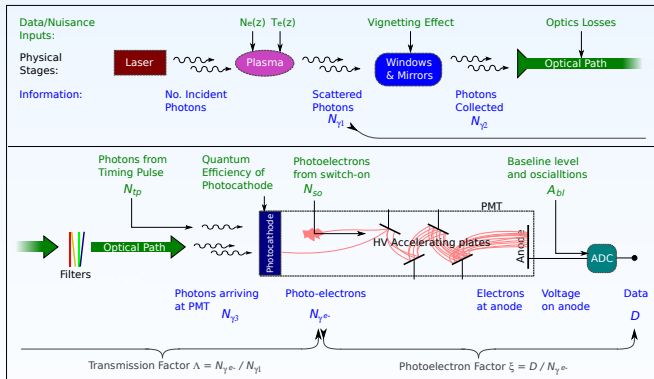
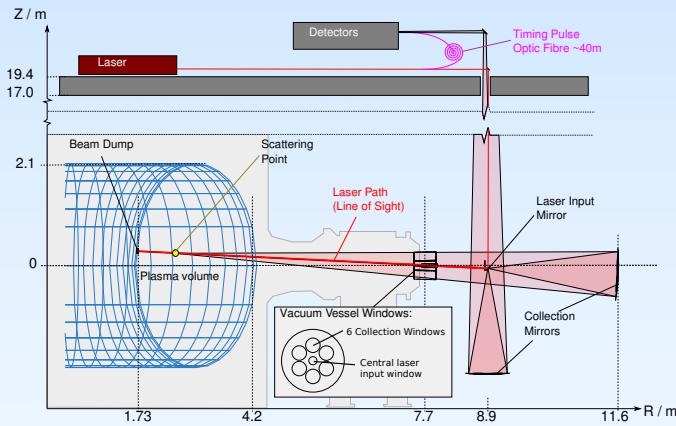
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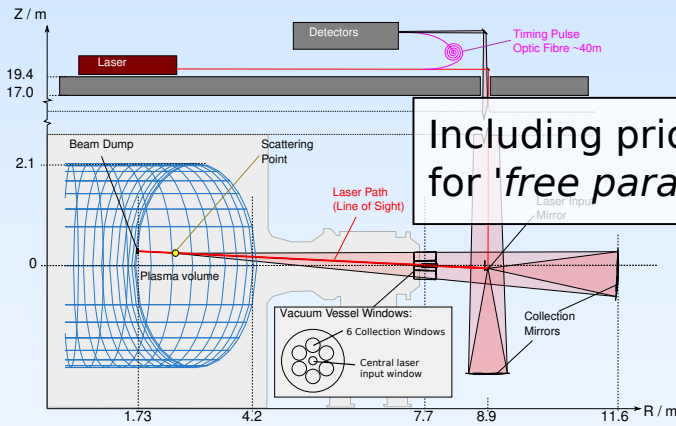
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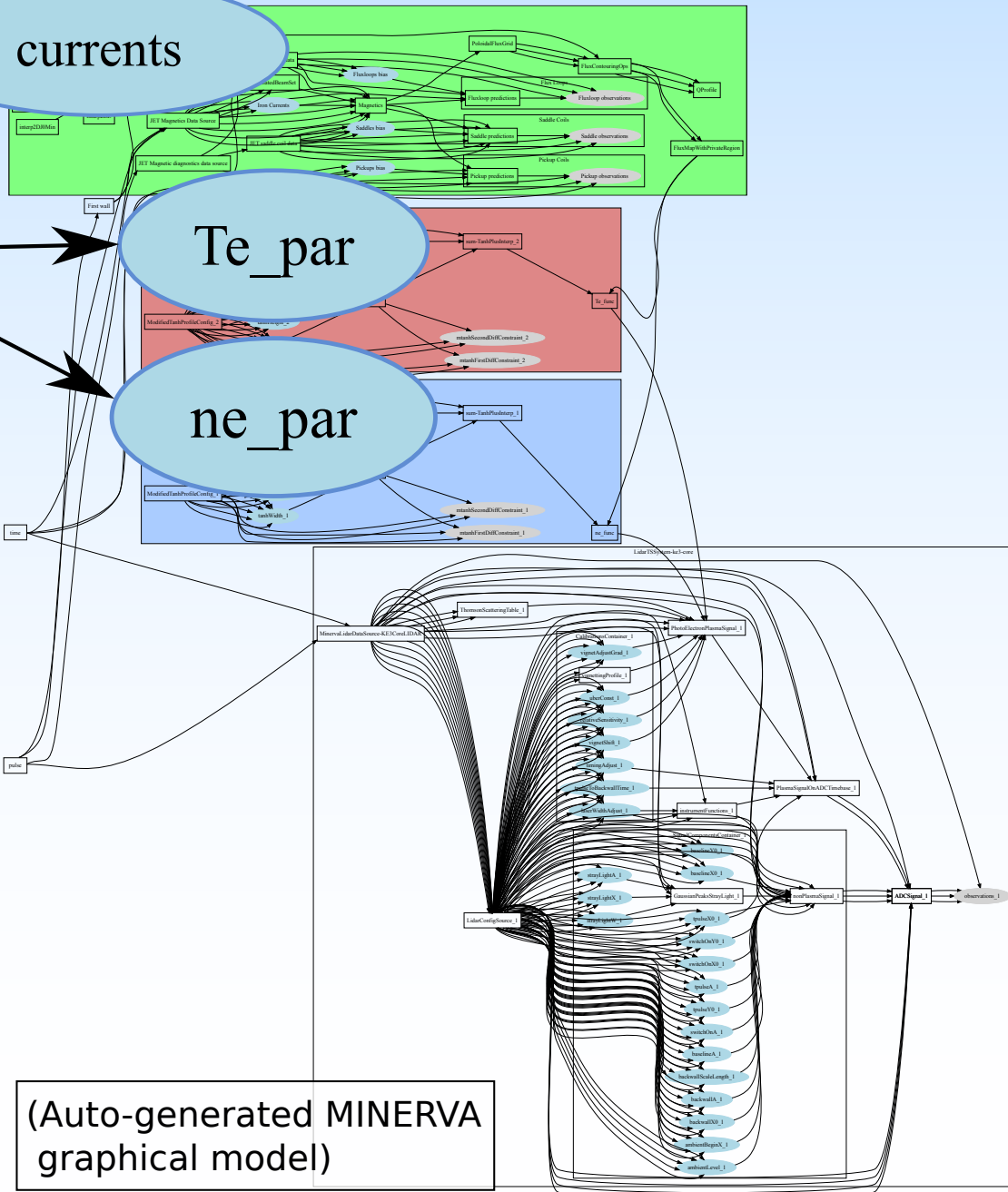
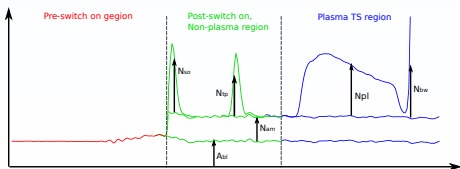
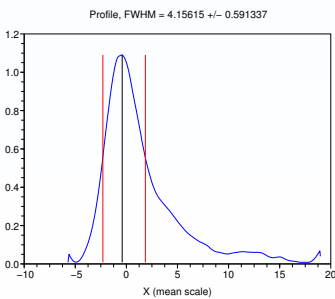
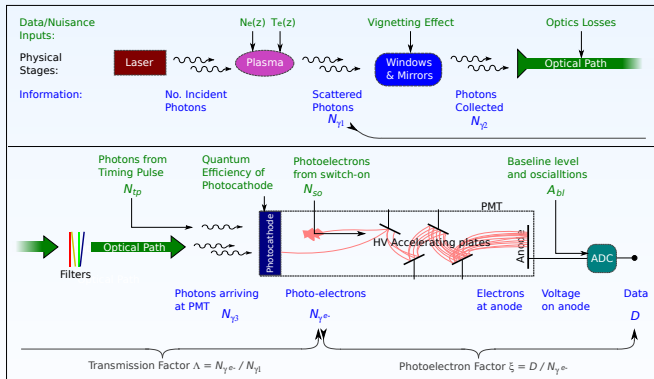
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Including prior PDFs for 'free parameters'



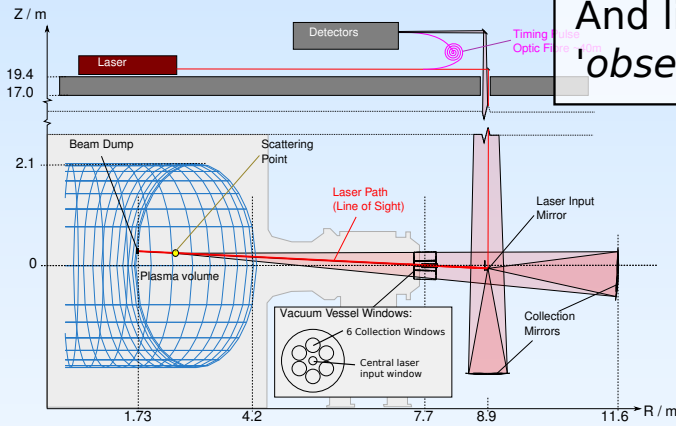
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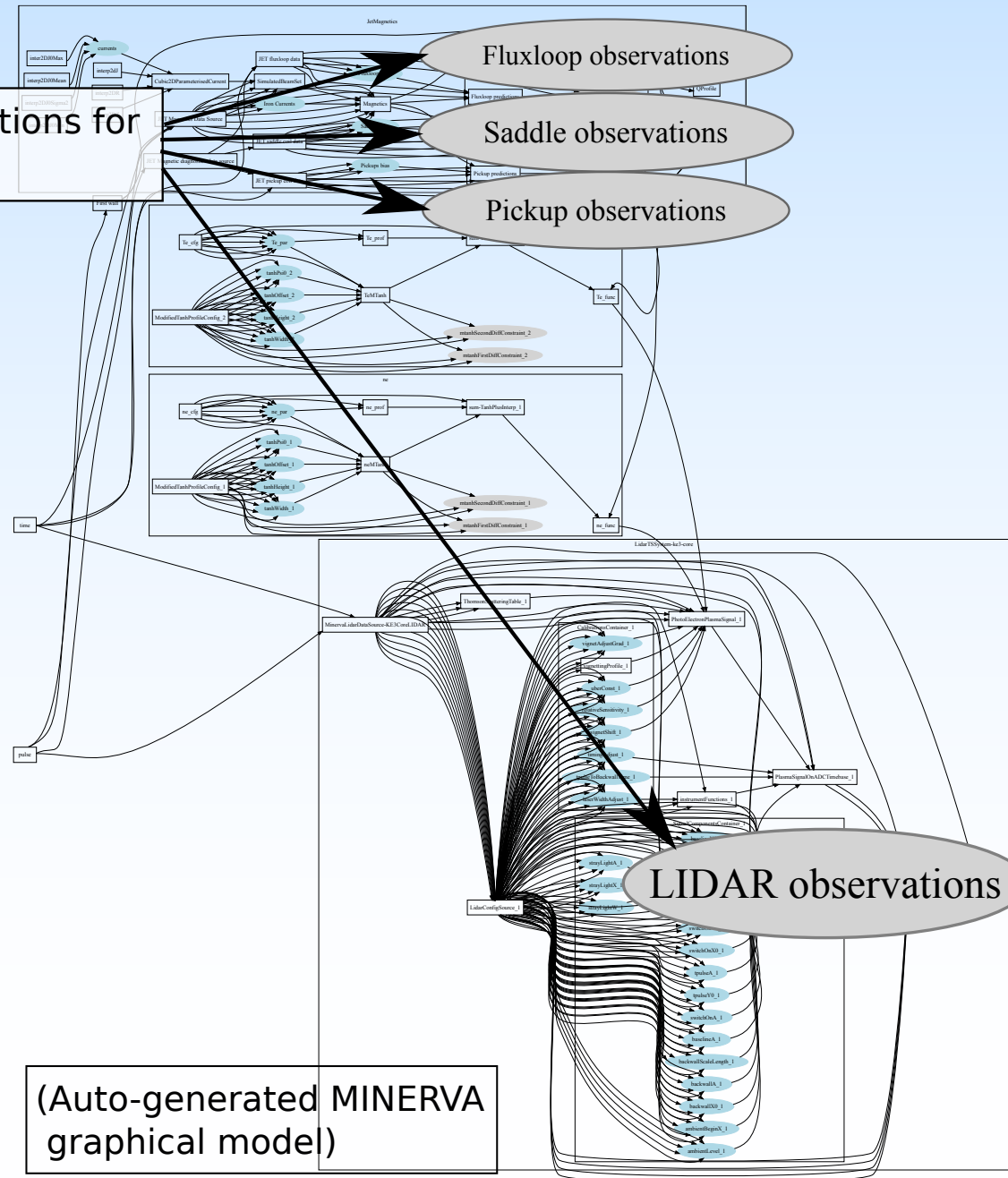
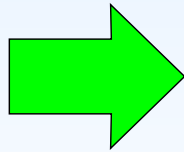
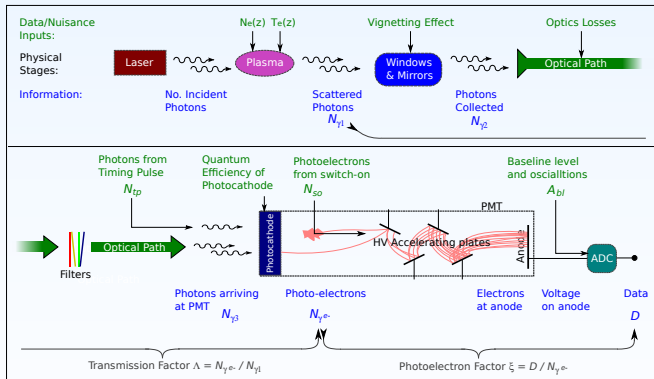
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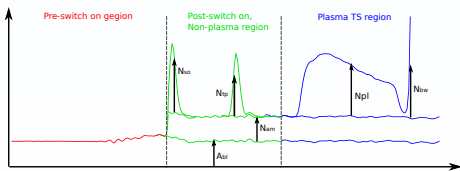
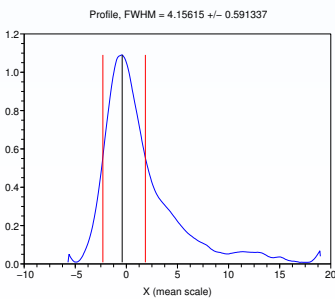
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And likelihood distributions for 'observations'.



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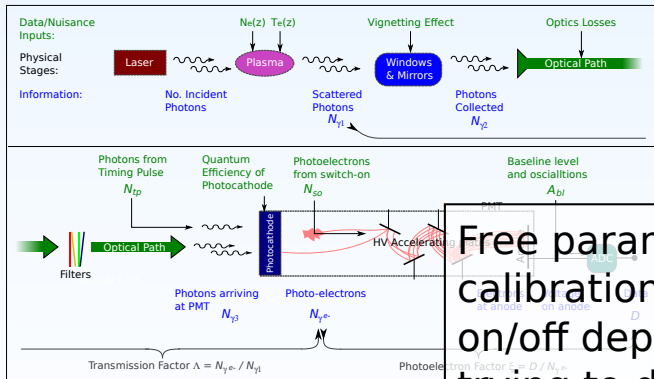
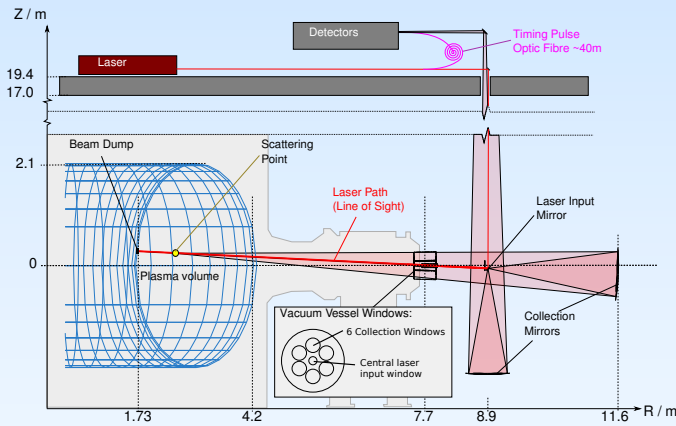


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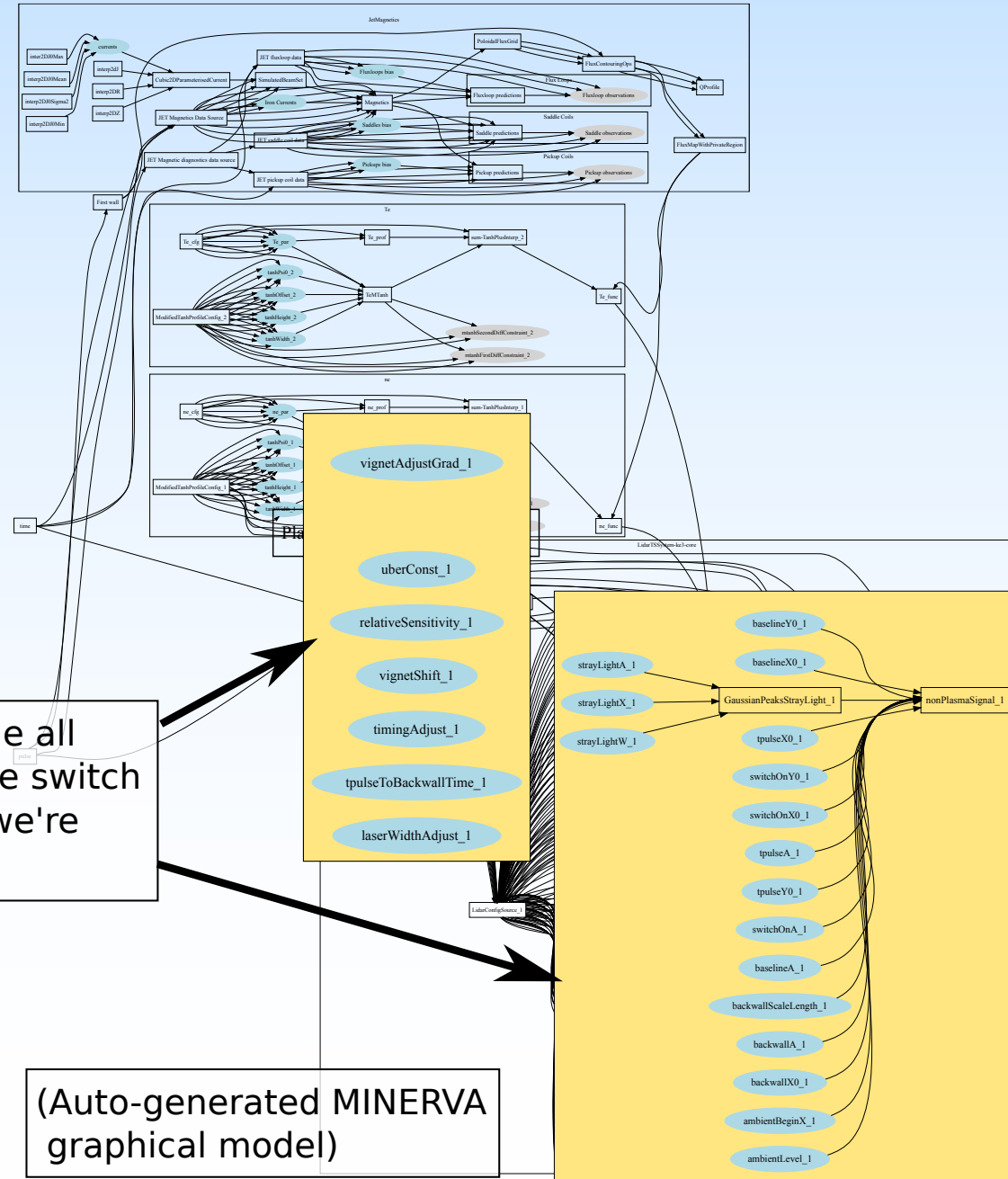
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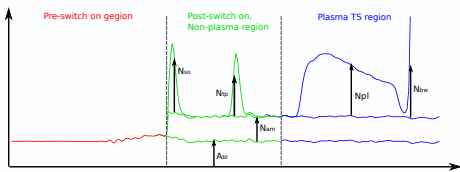
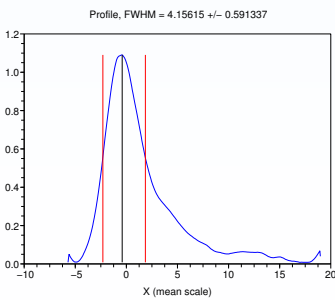
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Free parameters can include all calibration values, which we switch on/off depending on what we're trying to do.



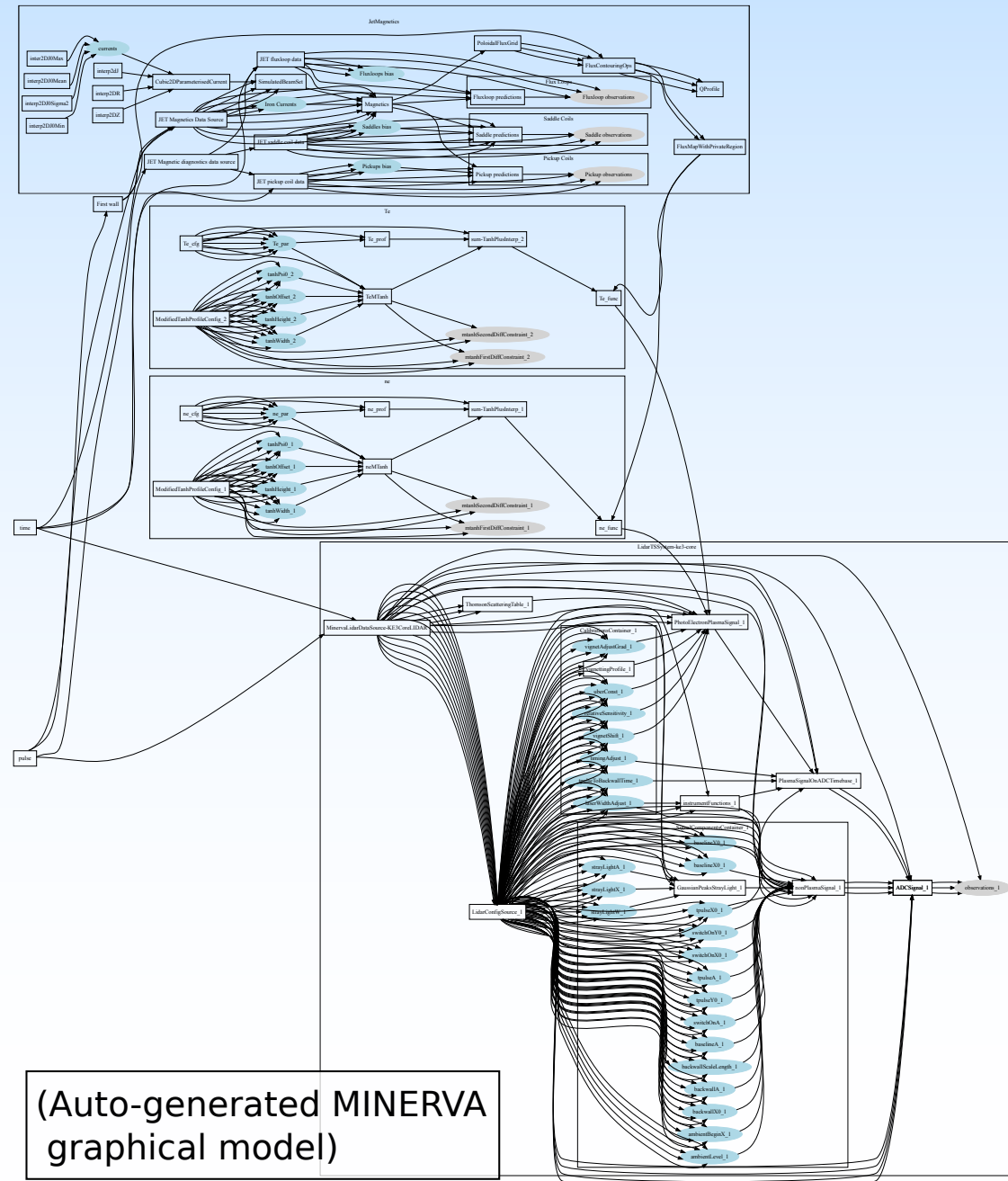
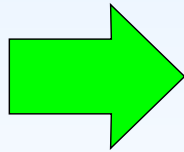
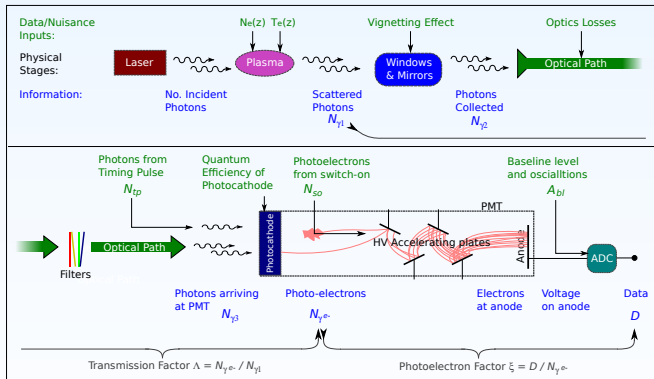
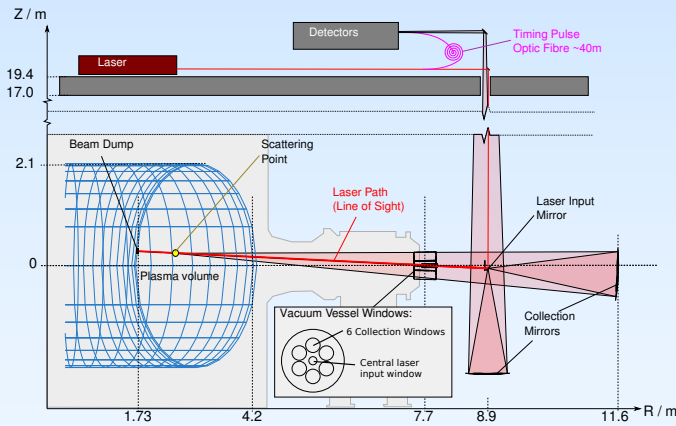
(Auto-generated MINERVA graphical model)



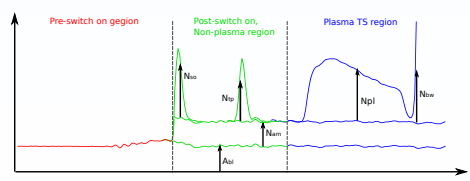
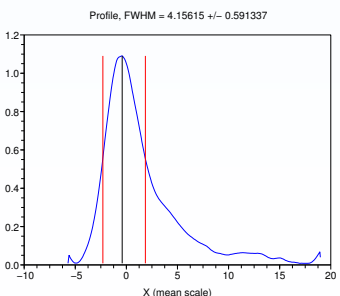
# Core + Edge LIDAR I: The model

- 1) Really understand how each part of the system works:  
Laser Pulse, TS physics, Optics, Filters, Photomultipliers, Counting Noise (PDFs), ADCs.

- 2) Develop MINERVA node for each part of the system.
- 3) Connect it all together and a plasma model.



(Auto-generated MINERVA graphical model)



## Core + Edge LIDAR III: Early results (2008)

Early results:

Core LIDAR + Interferometry on EFIT  $\psi_N$ .

Weak priors on all calibration parameters except relative sensitivities ( $T_e$  magnitude calibration).

Most calibrations are determined by consistency and data (either LIDAR or Interferometry).



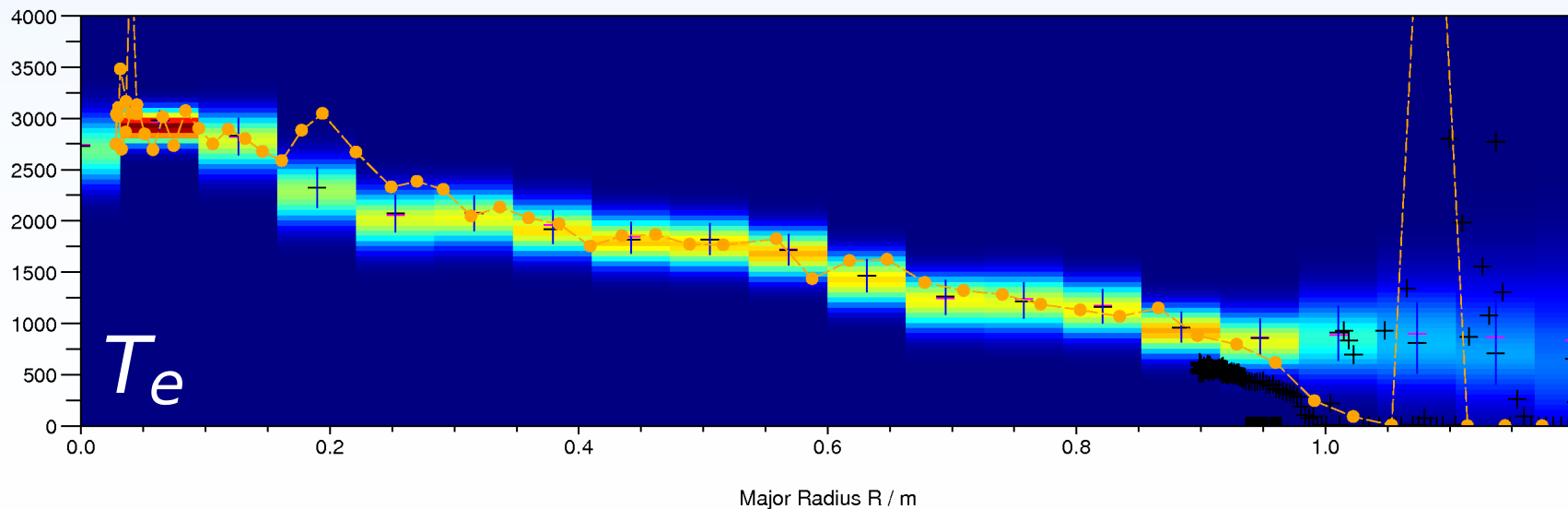
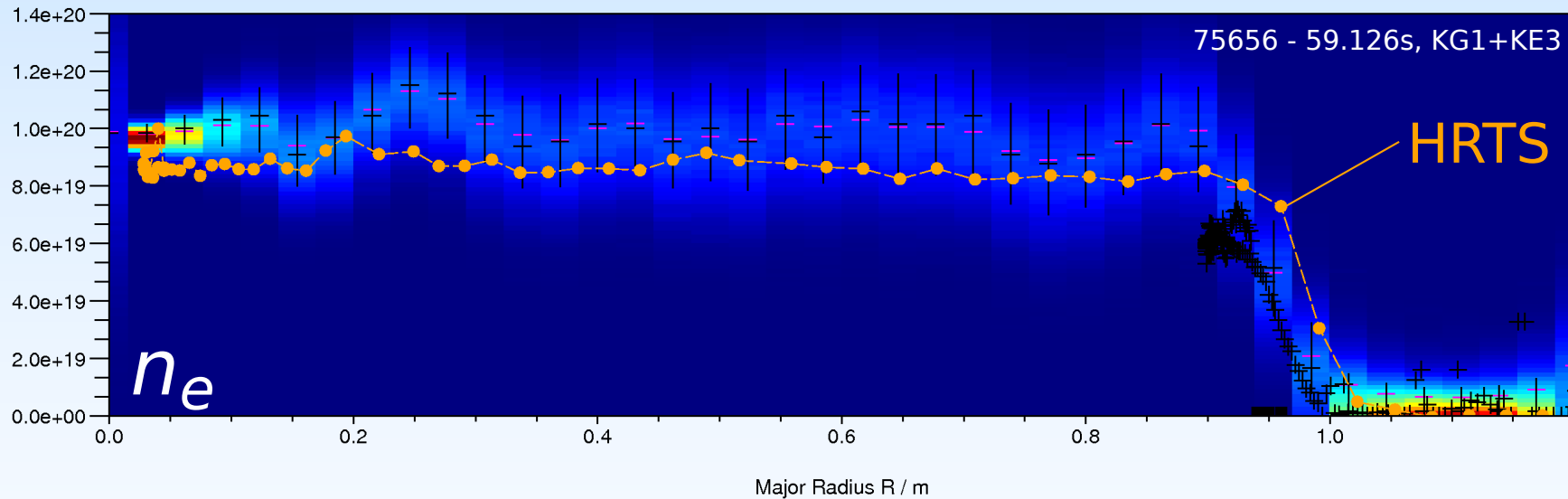
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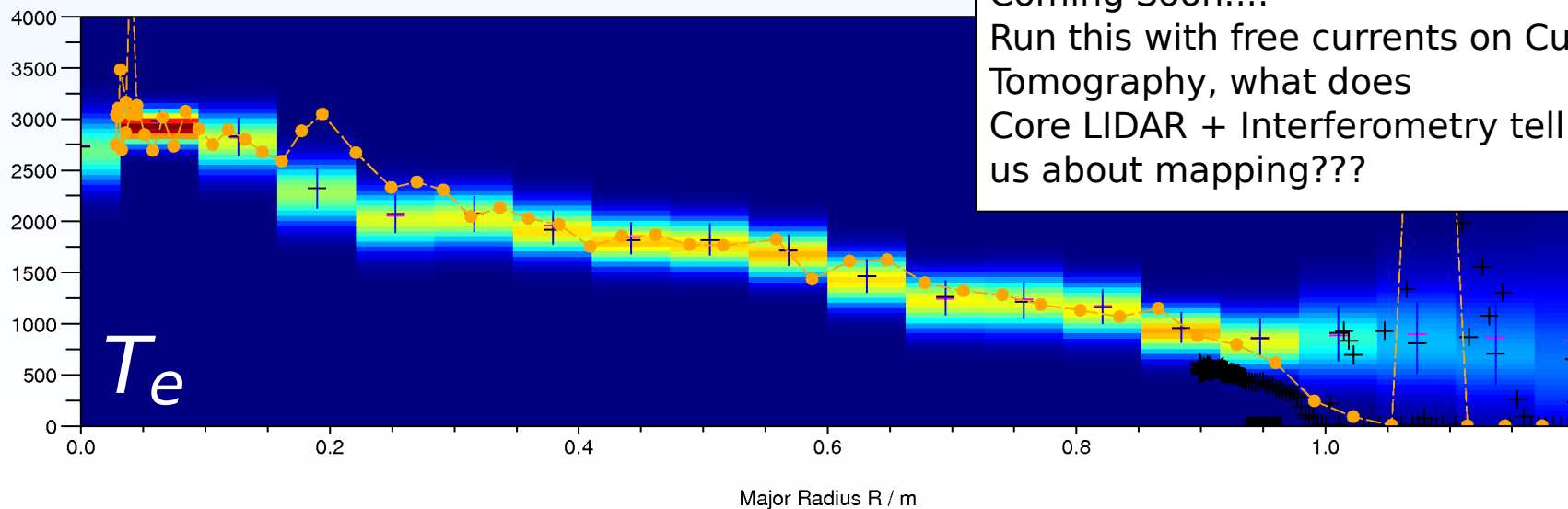
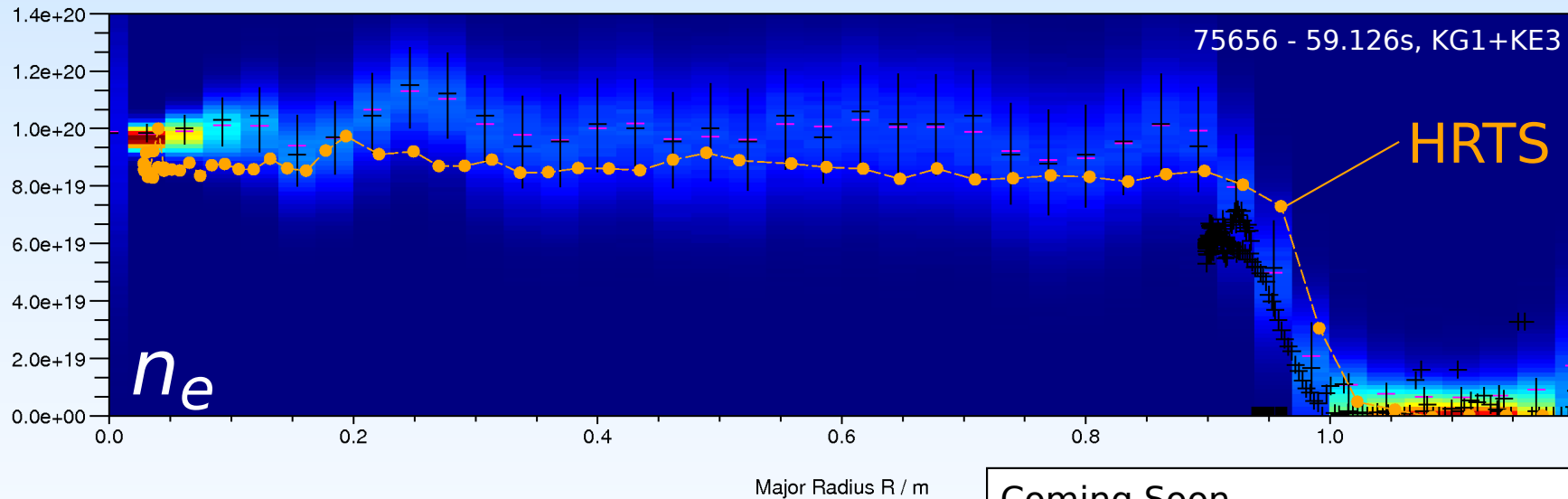
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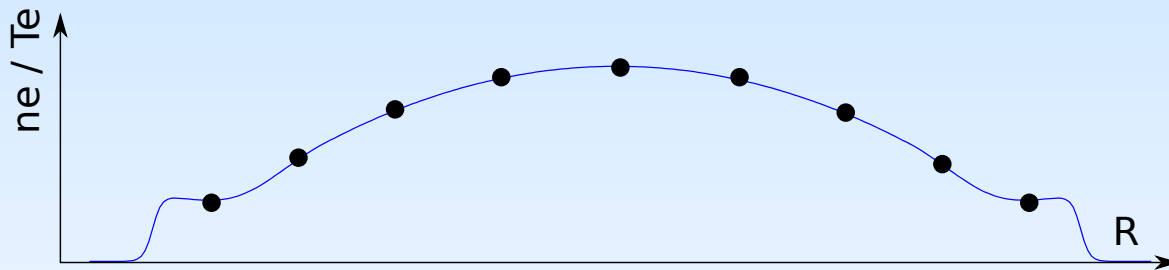
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Core LIDAR has  $\sim 12$ cm convolution and data points for every 3cm - it will never completely 'resolve' the pedestal. But, can it tell us anything, if we help it out a bit?...

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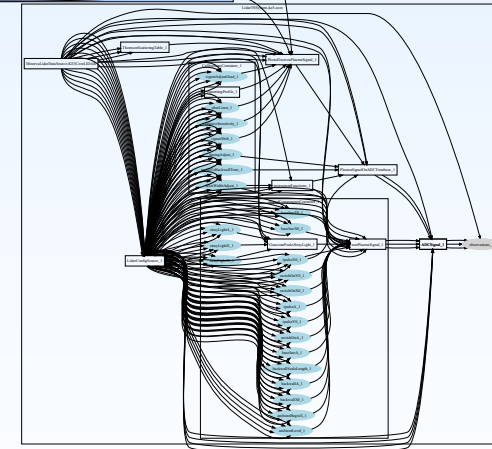
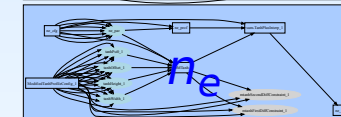
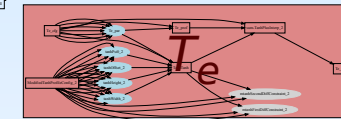
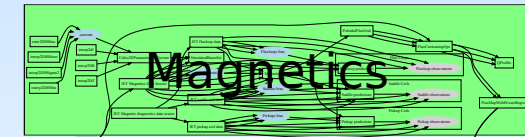
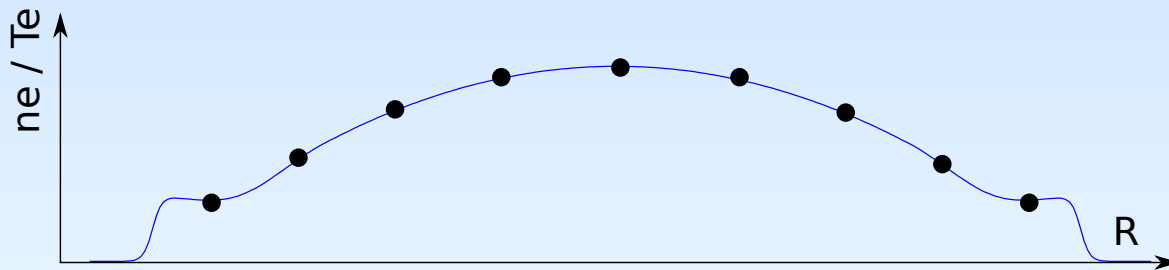
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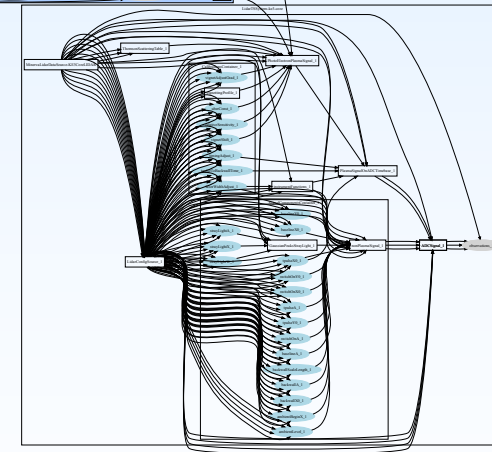
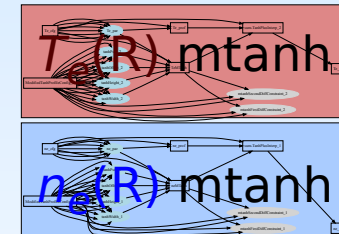
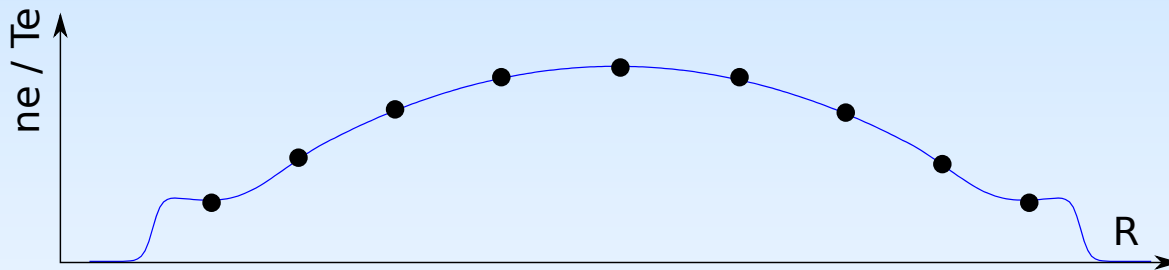
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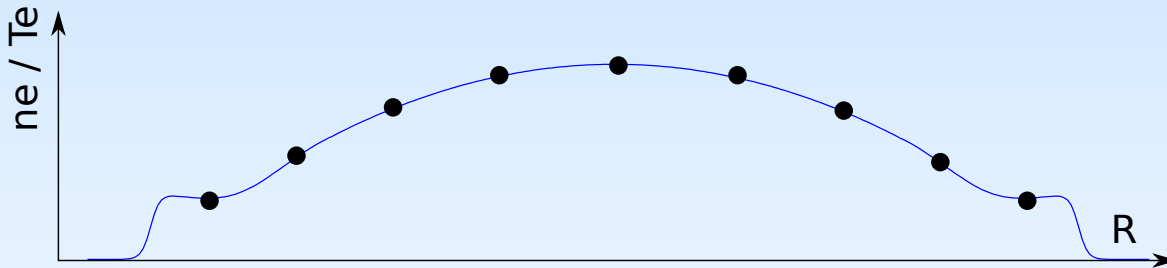




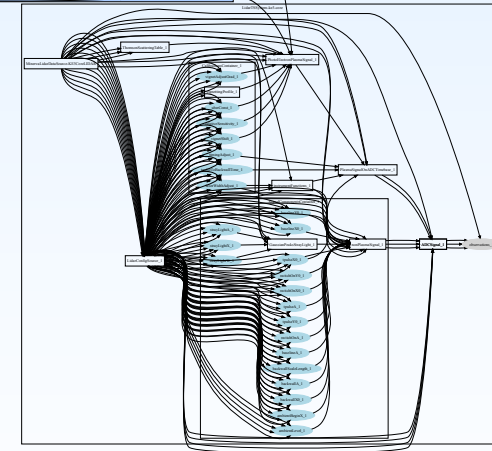
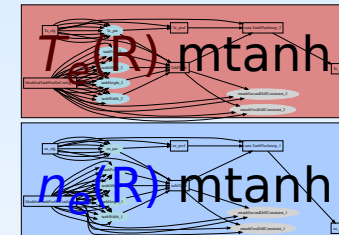
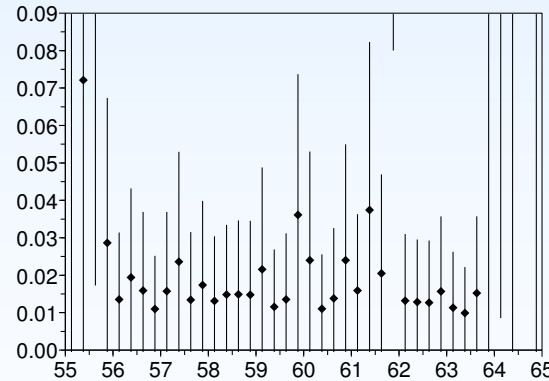
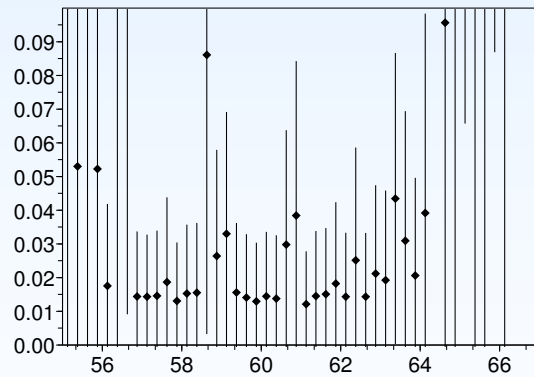
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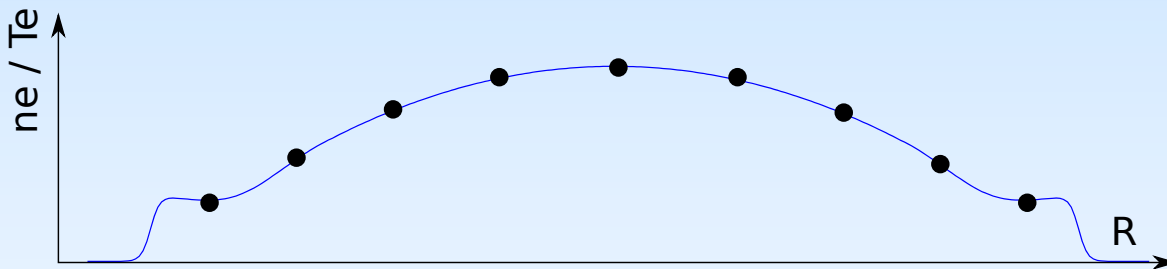
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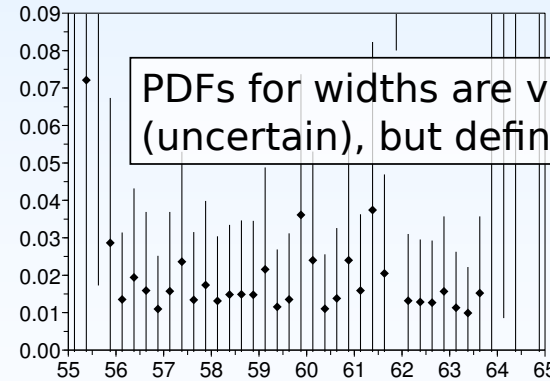
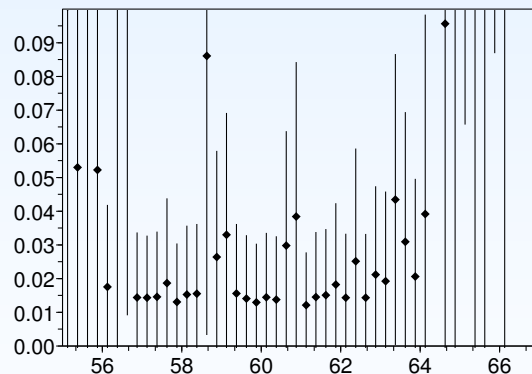
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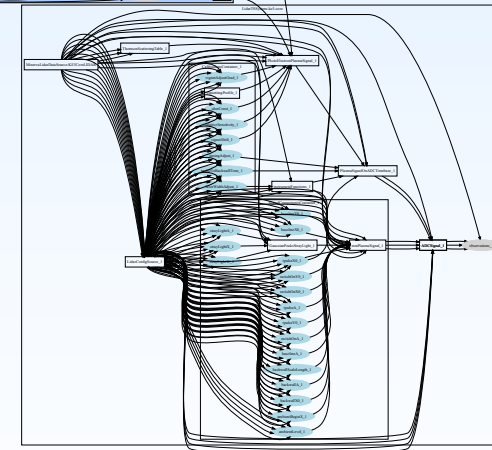
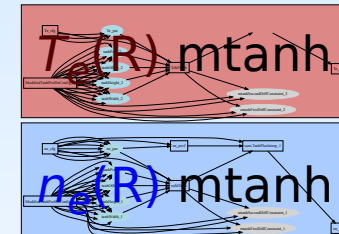
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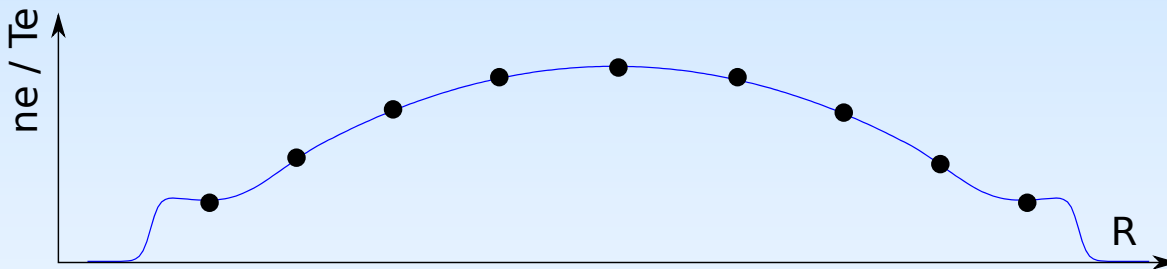
Inboard (High field side)

Outboard (Low field side)

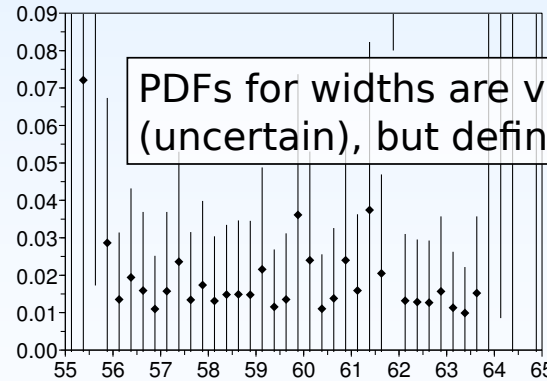
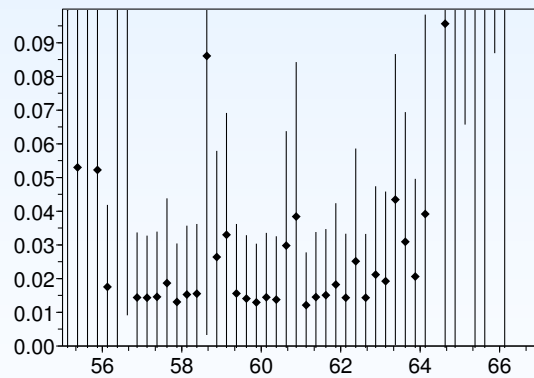
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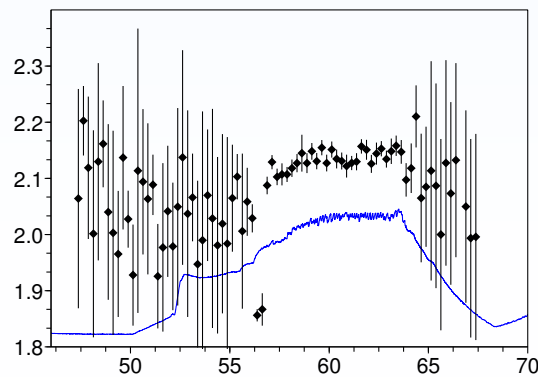


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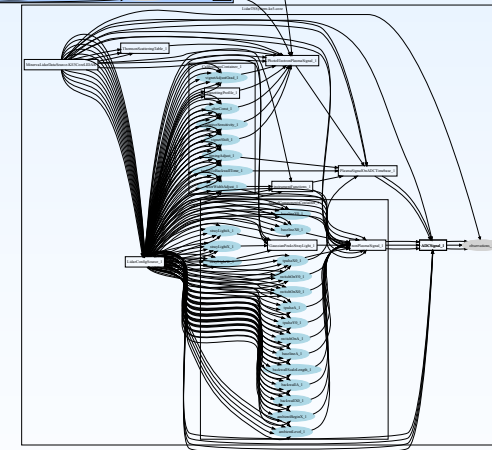
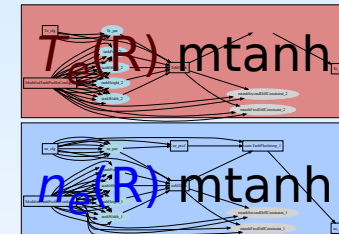
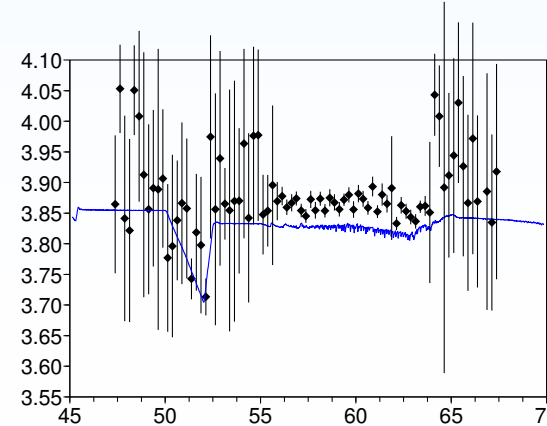


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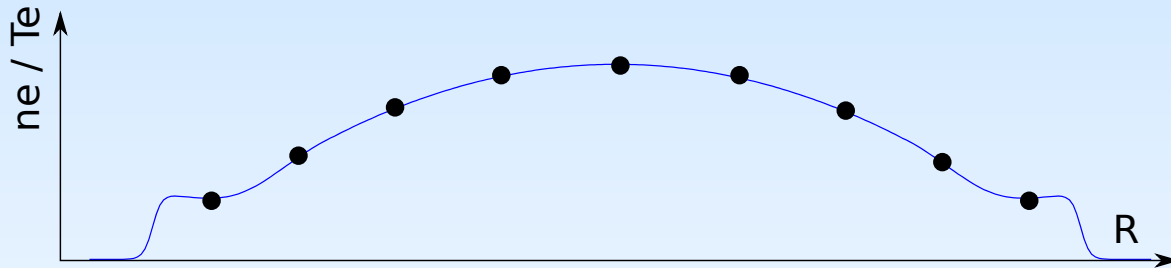
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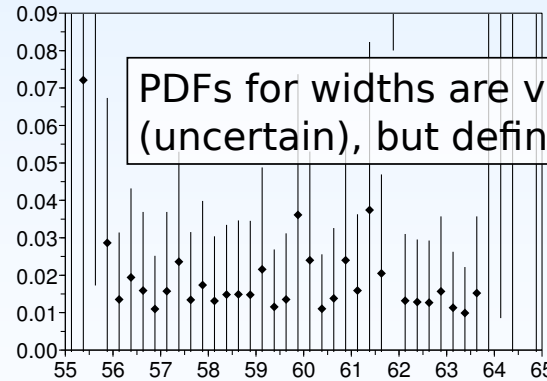
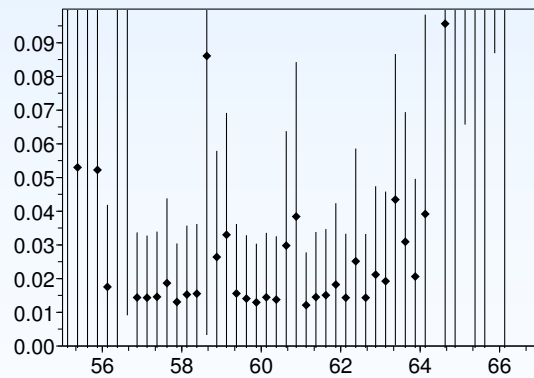
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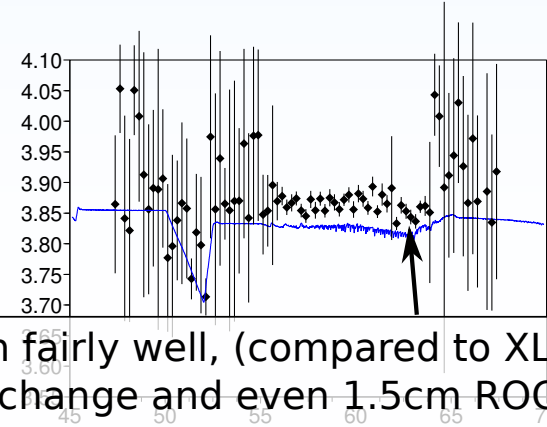
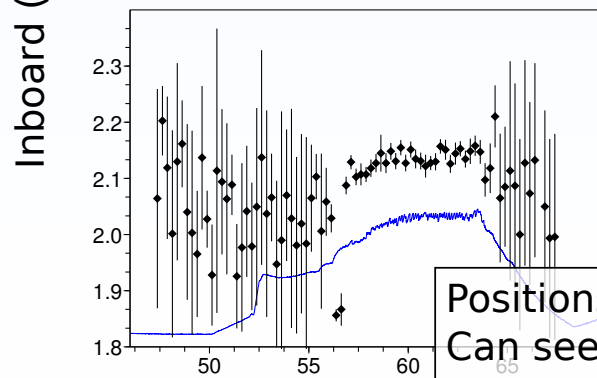
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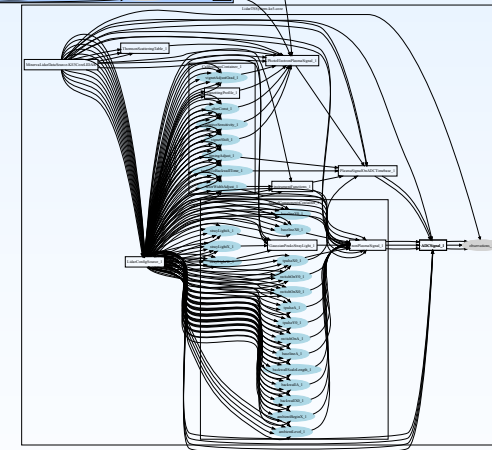
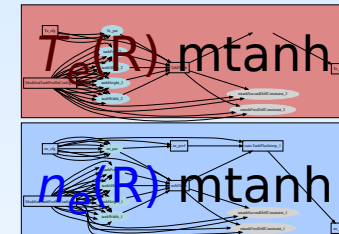
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Positions known fairly well, (compared to XLOC here)  
Can see shape change and even  $1.5\text{cm}$  ROG sweep through average.



## Core + Edge LIDAR V: Add edge LIDAR.

As with core LIDAR, calibrations (**position**,  $n_e$  **magnitude** etc) all have uncertainty (some large).

 $n_e$  $T_e$

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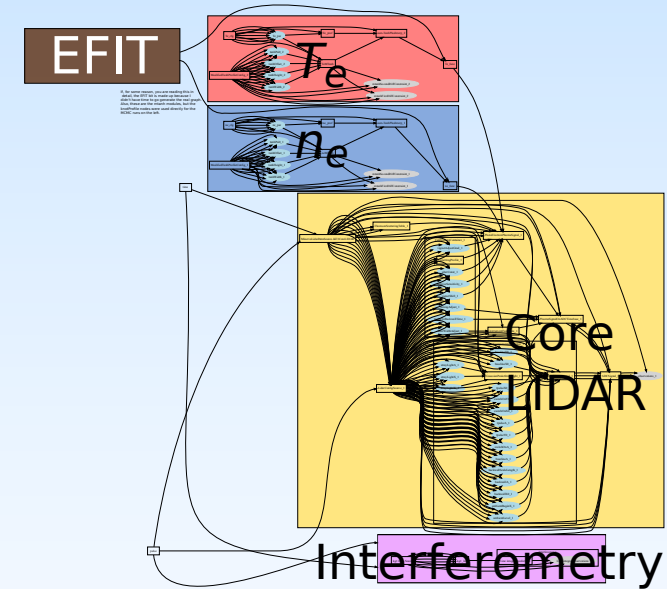
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$T_e$



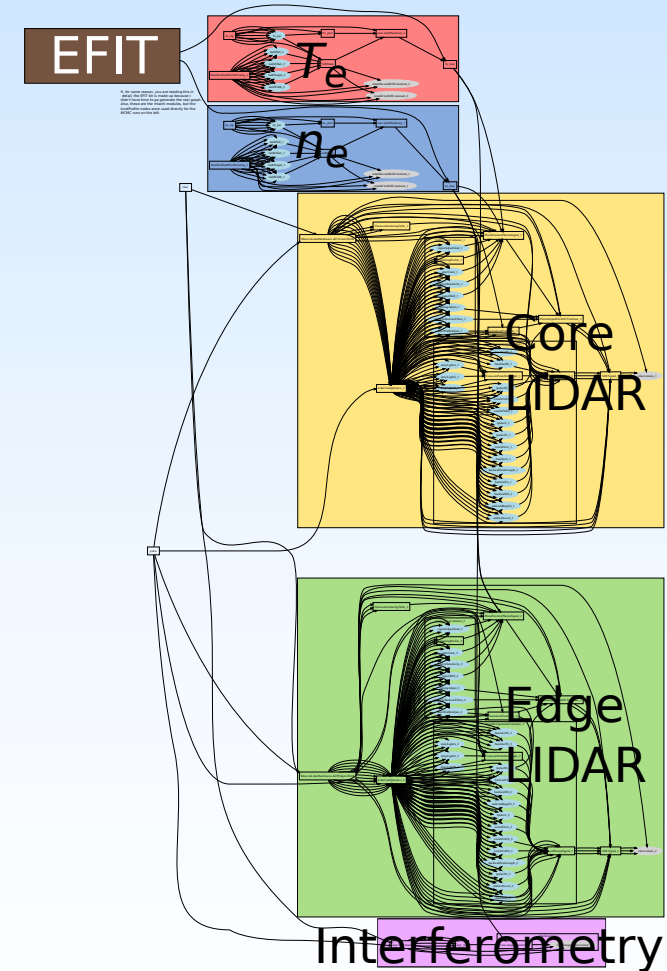
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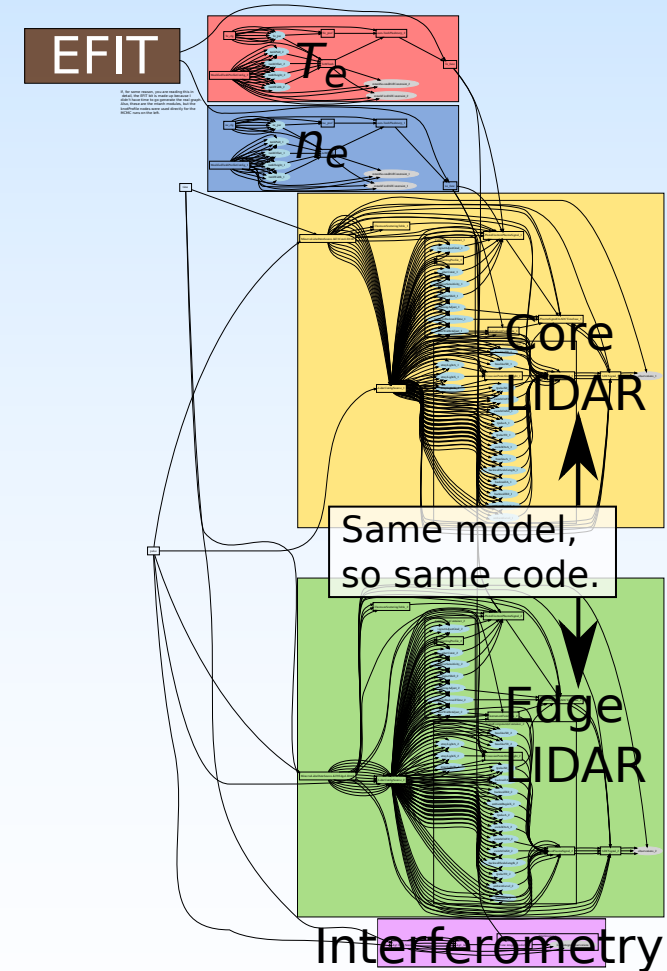
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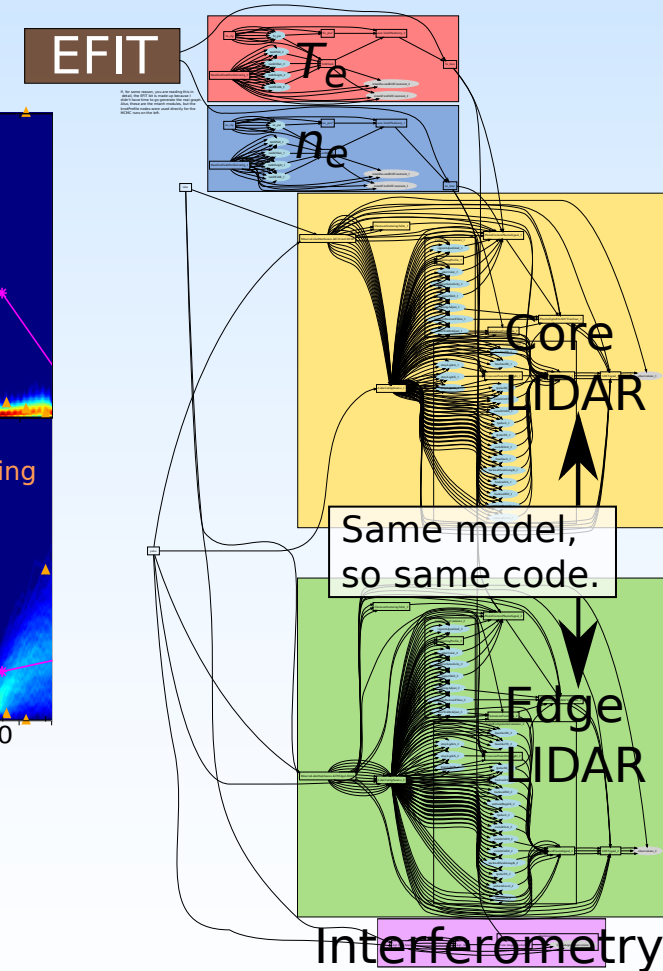
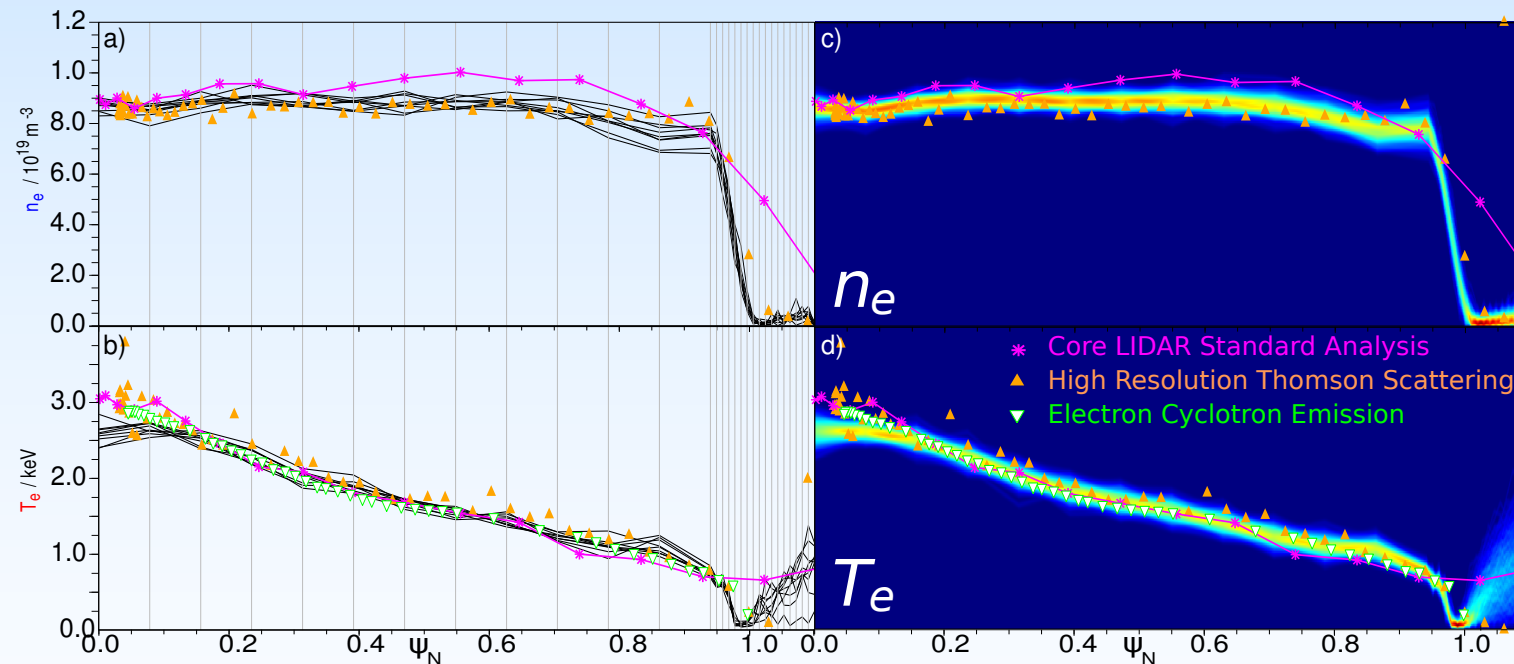


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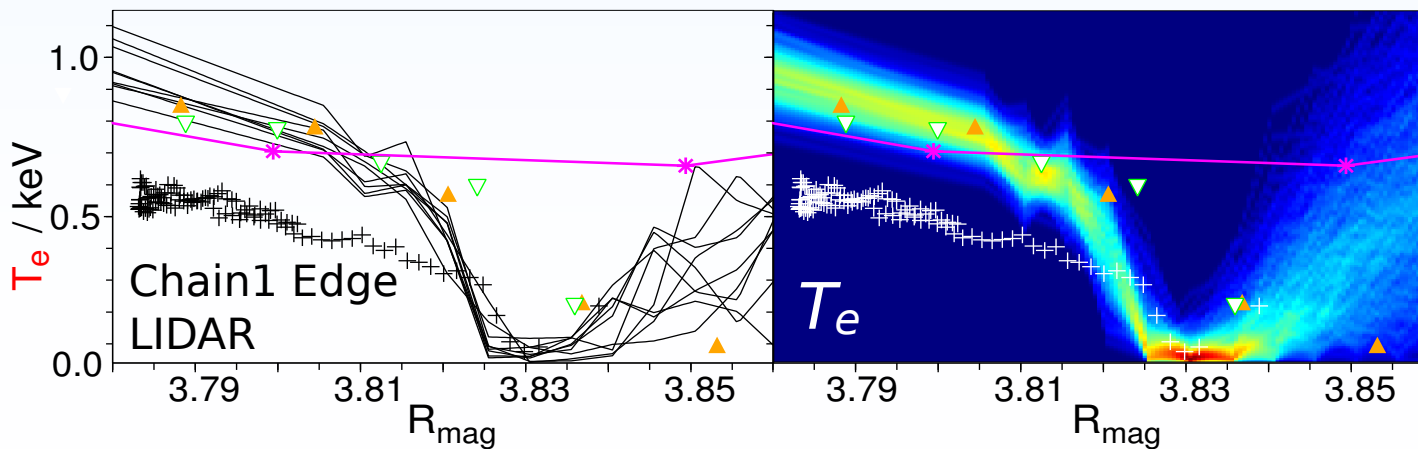
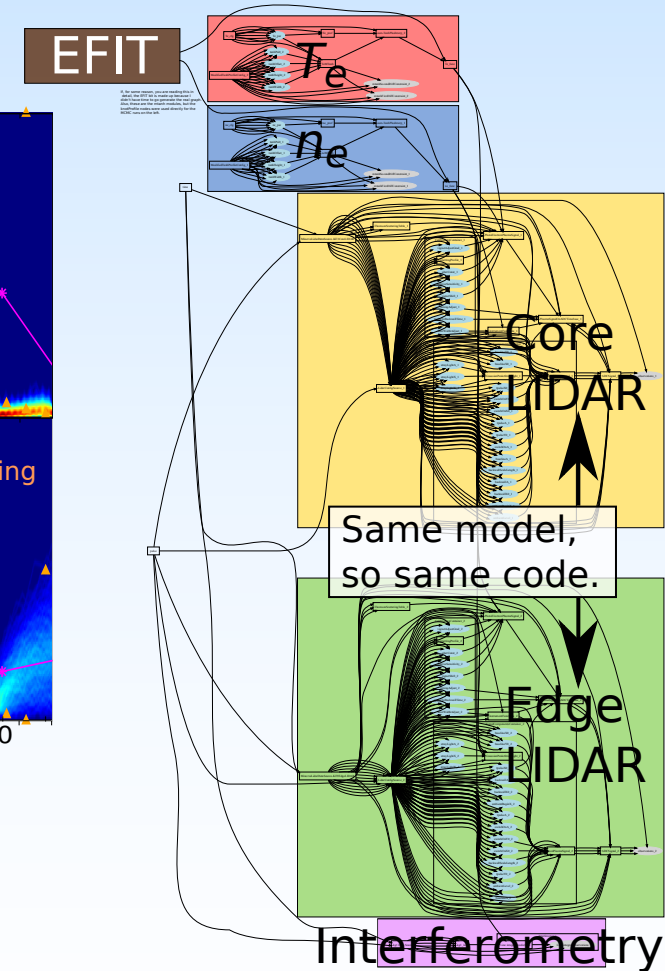
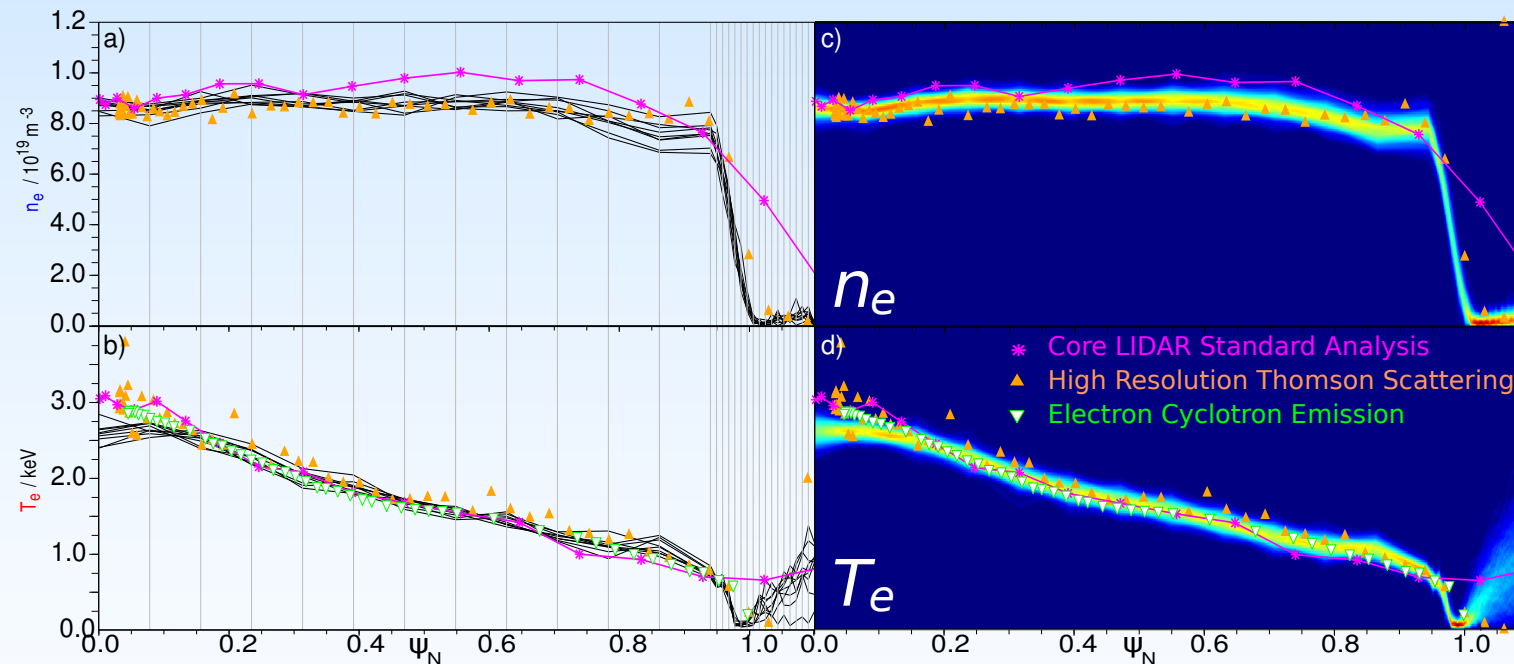


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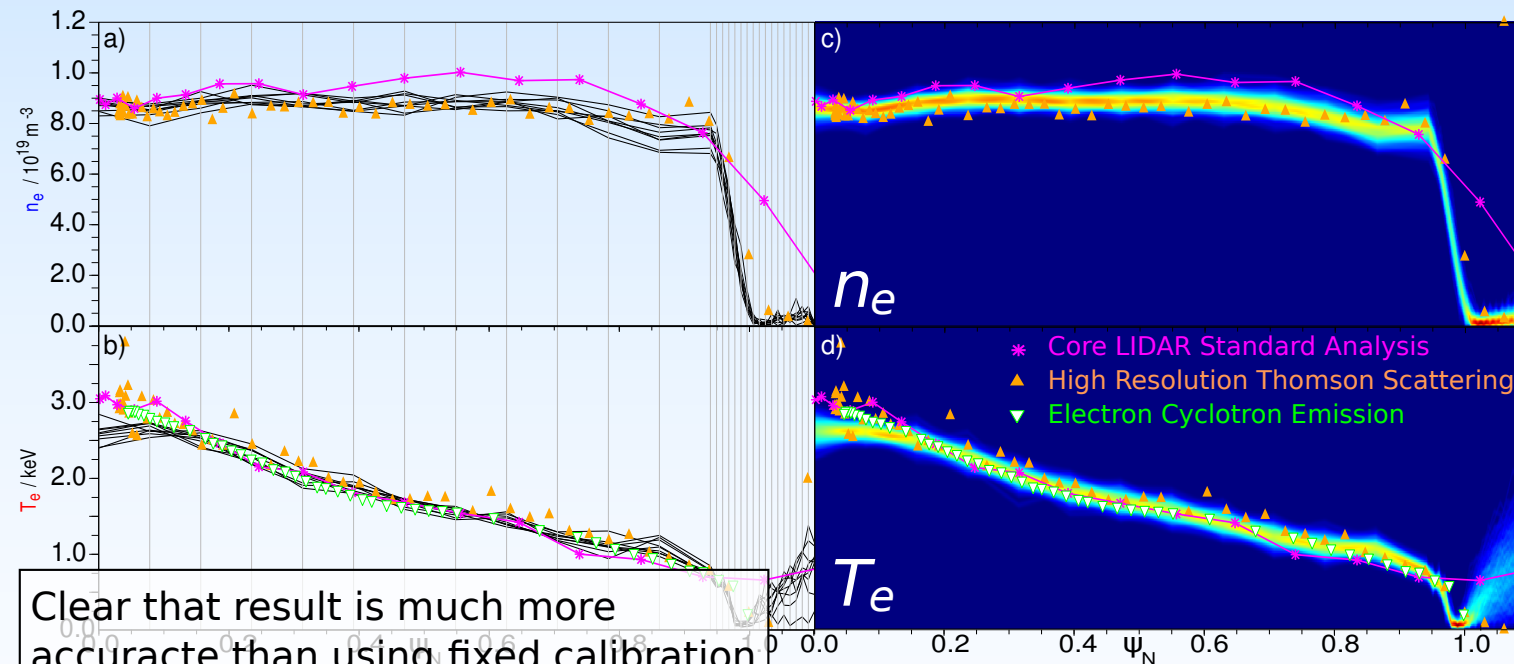


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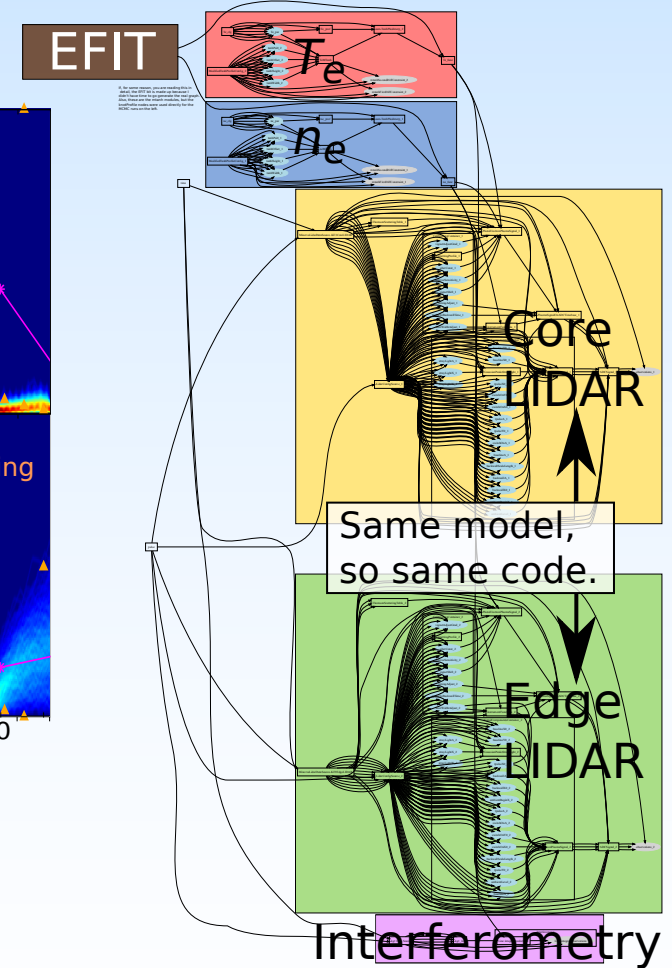
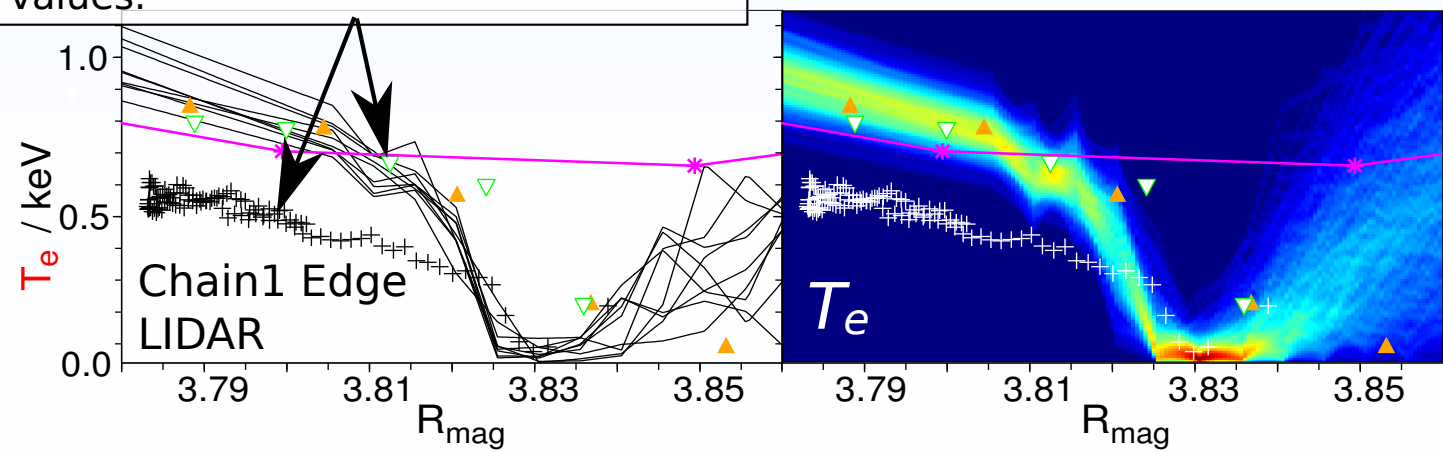
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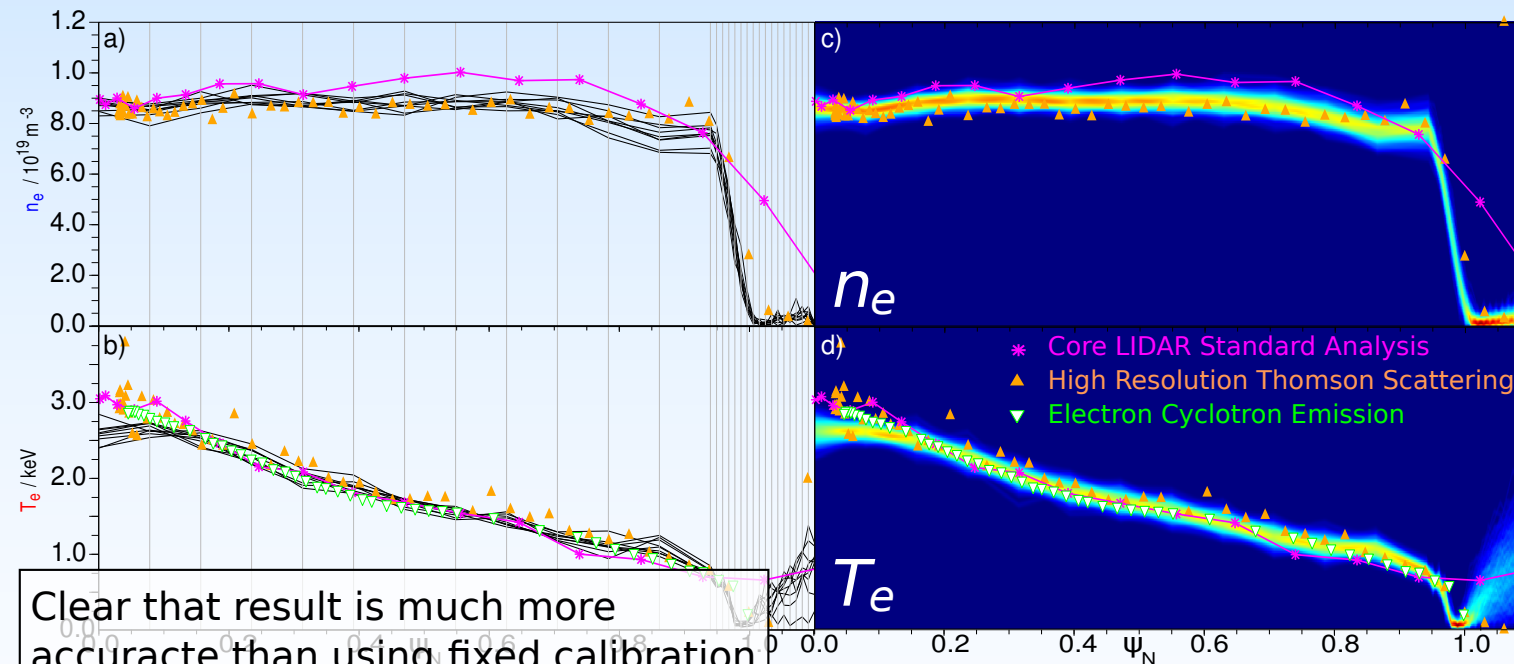


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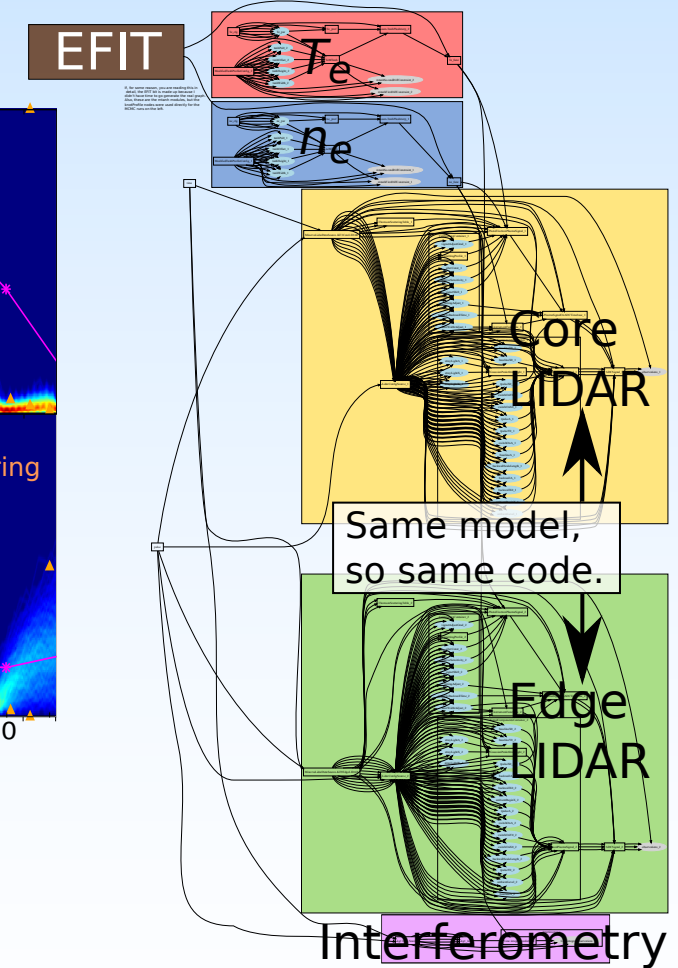
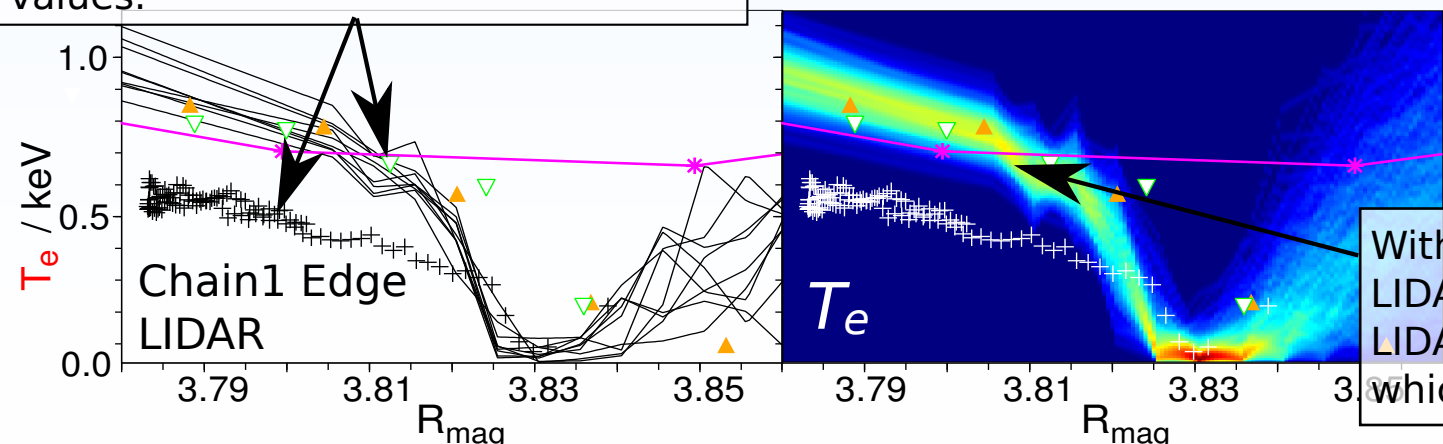
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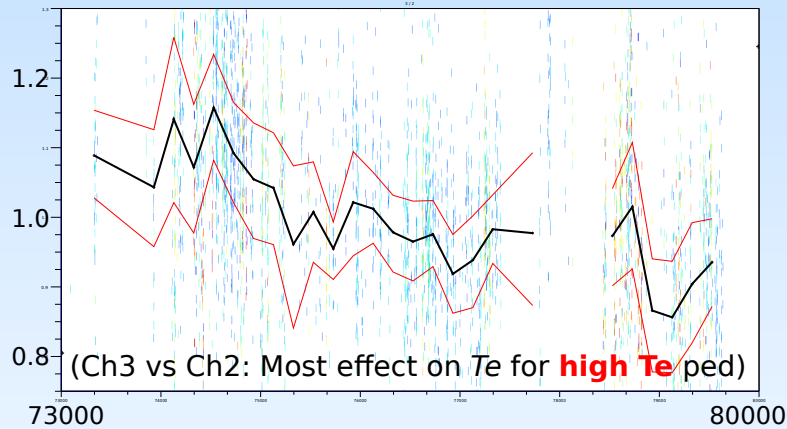
With completely free calibration, edge LIDAR provides shape with which Core LIDAR can give accurate  $T_e$  ped height which feeds back to Edge LIDAR

## Core + Edge LIDAR VI: Calibrations Inference.

Find posterior maximum (best fit) for mtanh parametrised  $n_e(\psi_N)$  and  $T_e(\psi_N)$  with Core+Edge LIDAR with completely free edge LIDAR  $T_e$  calibrations. Look at inferred calibration for C25-present:

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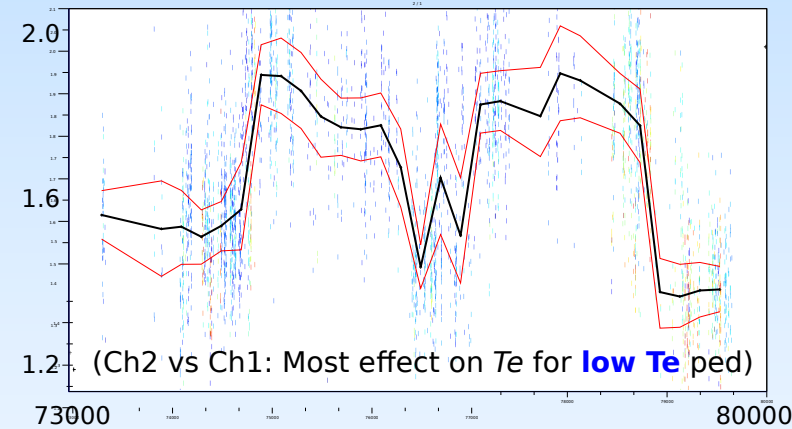
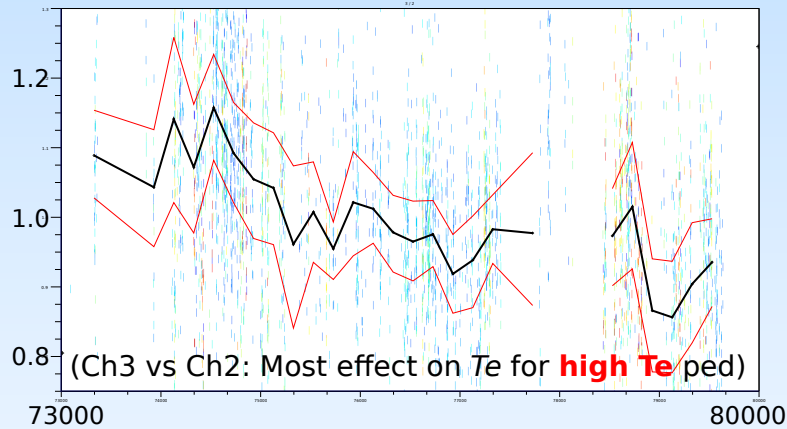
$T_e \sim$  From Core Lidar

This is effectively a cross calibration with Core LIDAR (not easy normally).

See a slow drift to edge LIDAR calibration, but overall a significant difference to calibration usually used.

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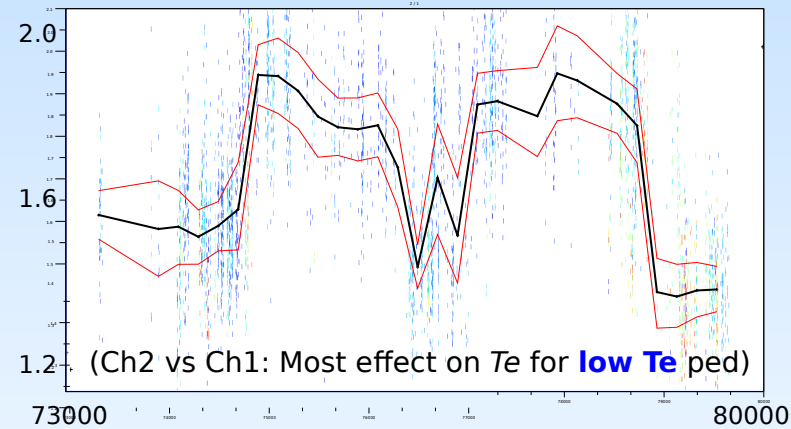
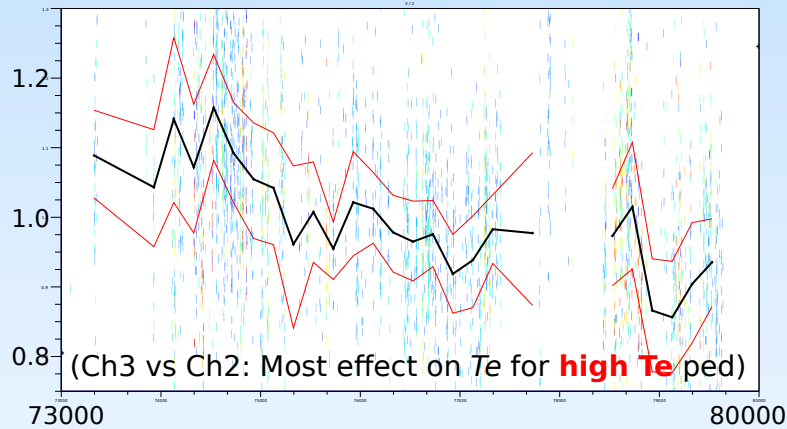
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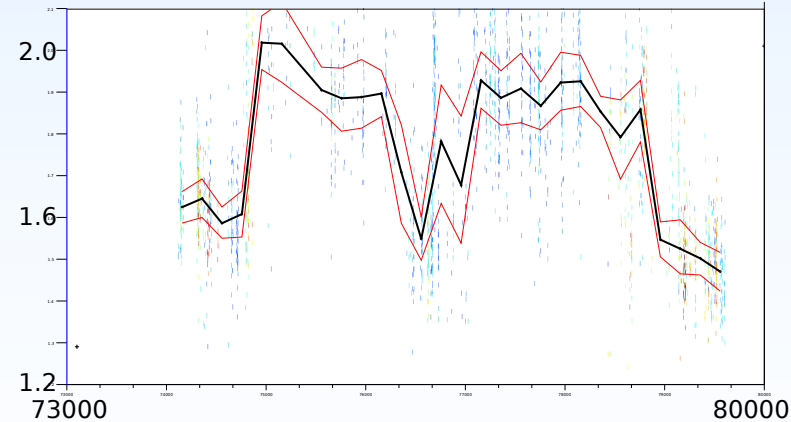
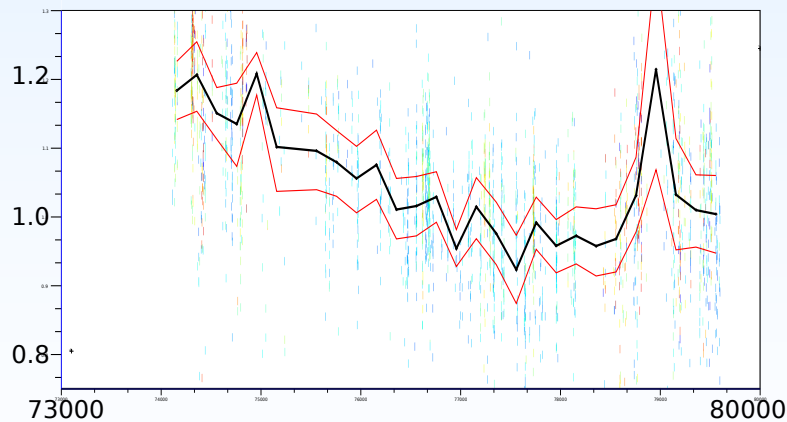
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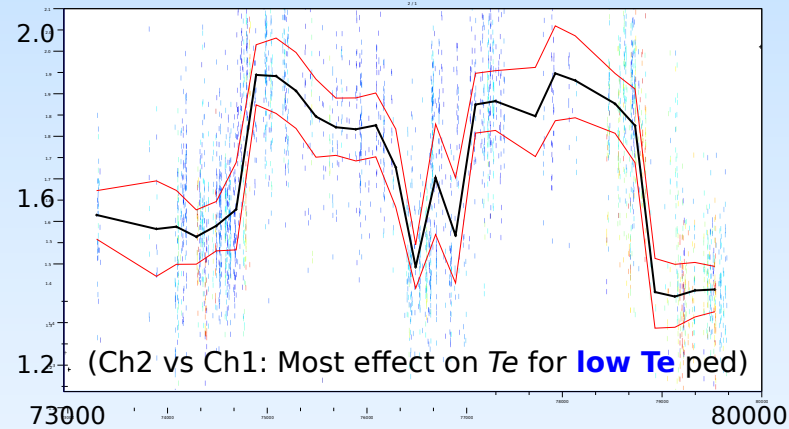
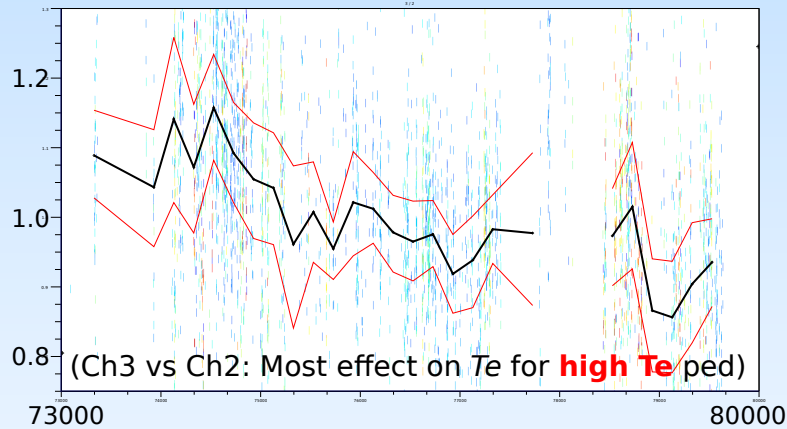


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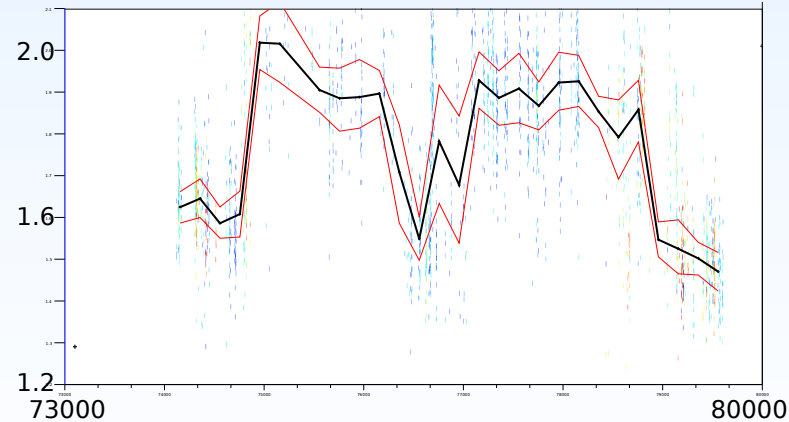
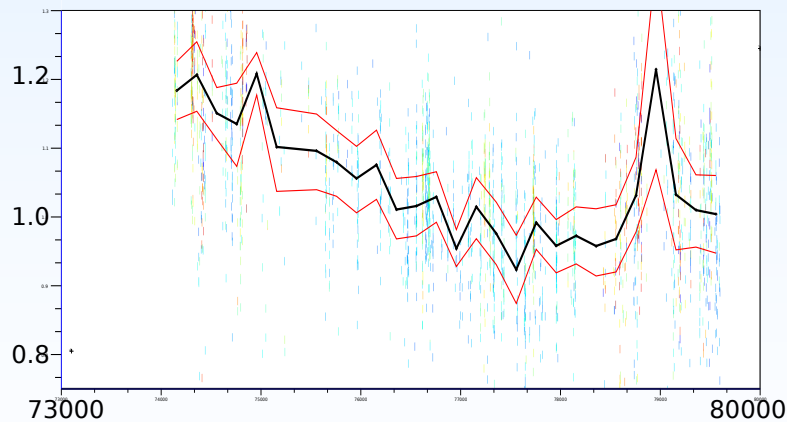
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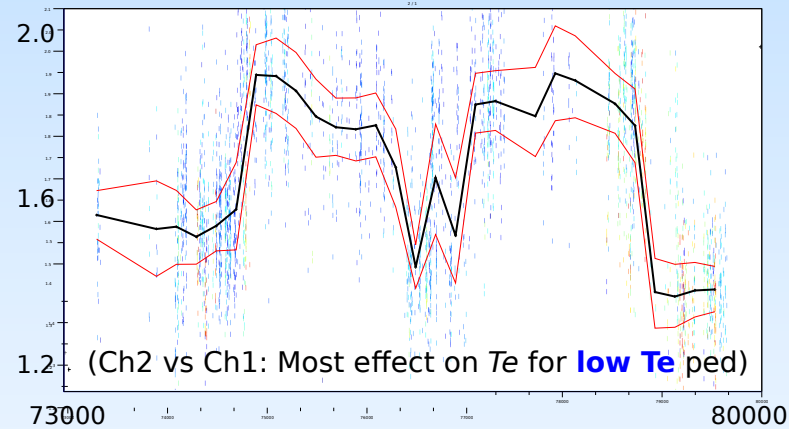
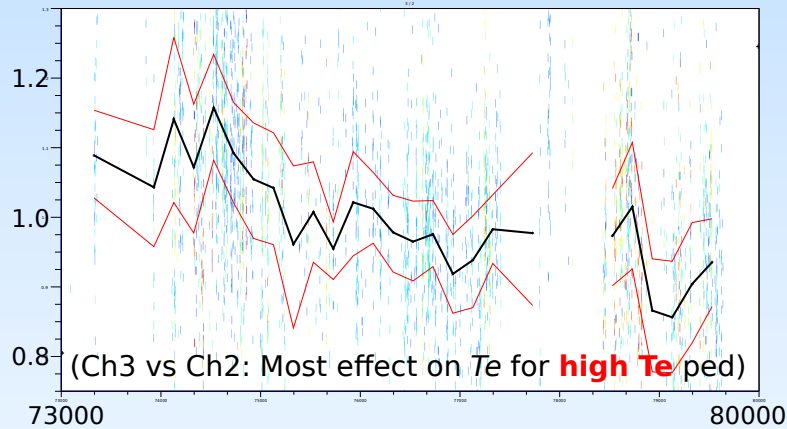
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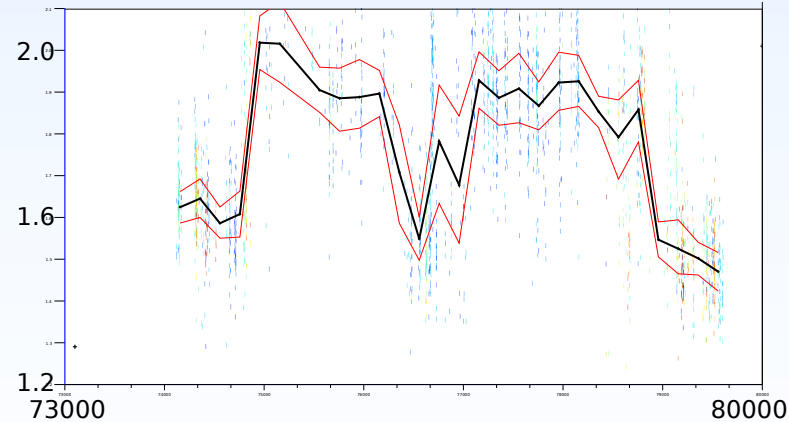
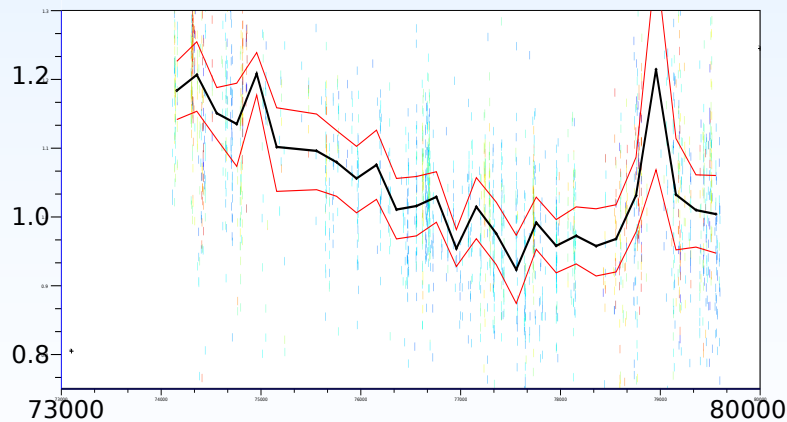
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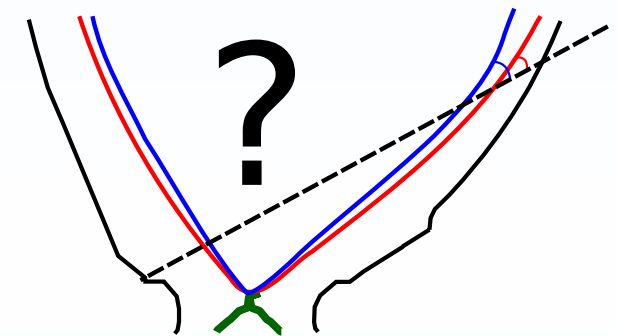
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Only remaining reason might be mapping (since we're fixed to so far).



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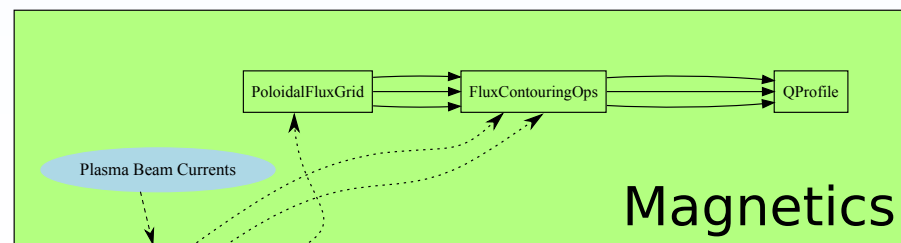
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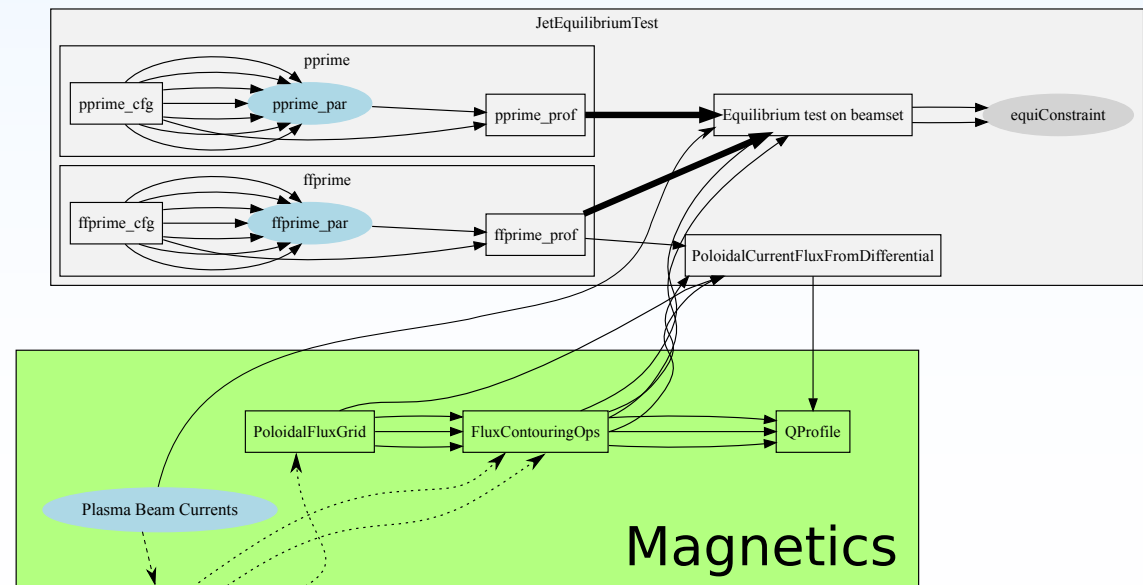
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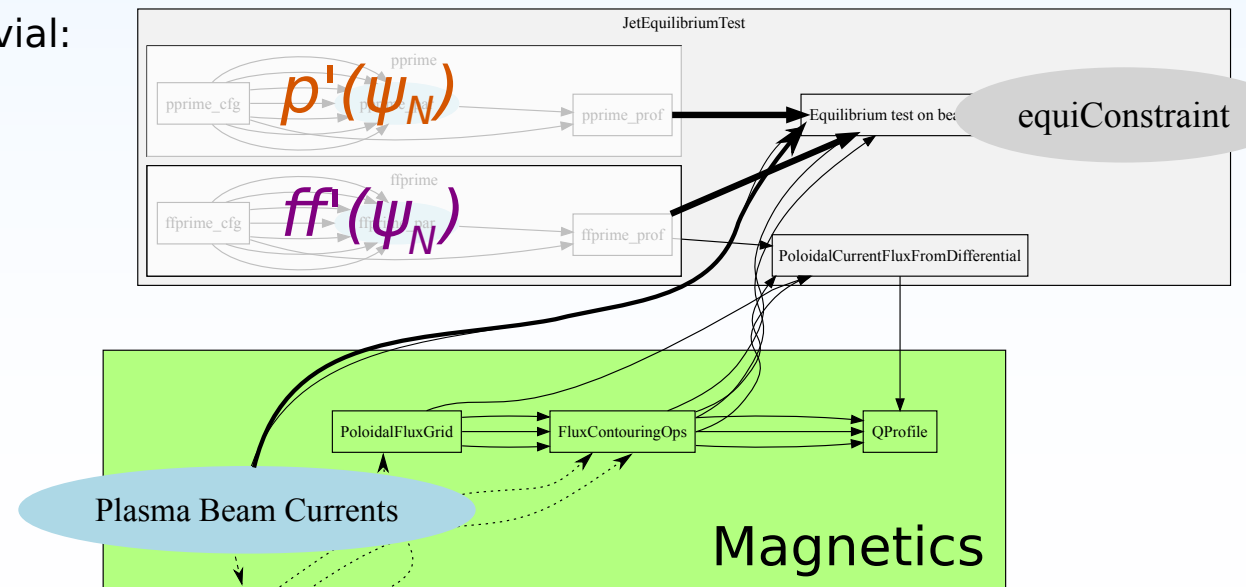
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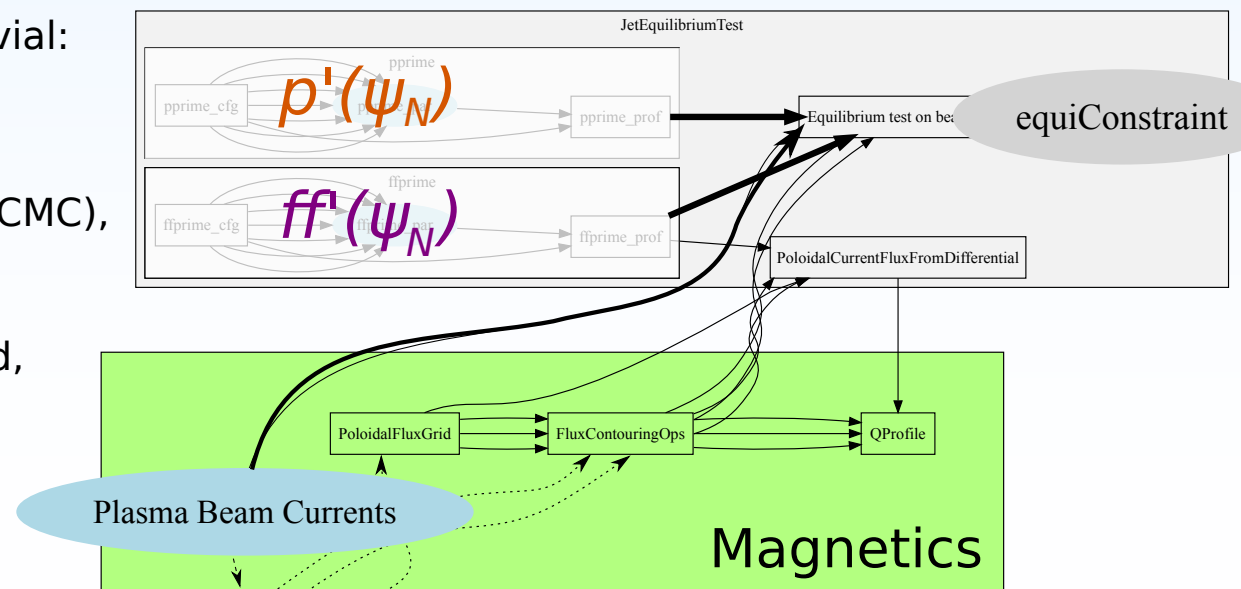
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Exploring the PDF is currently beyond the capability of our the present algorithms (MCMC), even for low resolution parametrisations.

Even finding the maximum (best fit) is hard, but can now be done...



## Equilibrium II: Maximum Posterior (Magnetics Only)

78601 High ne  
H-Mode (pellets)

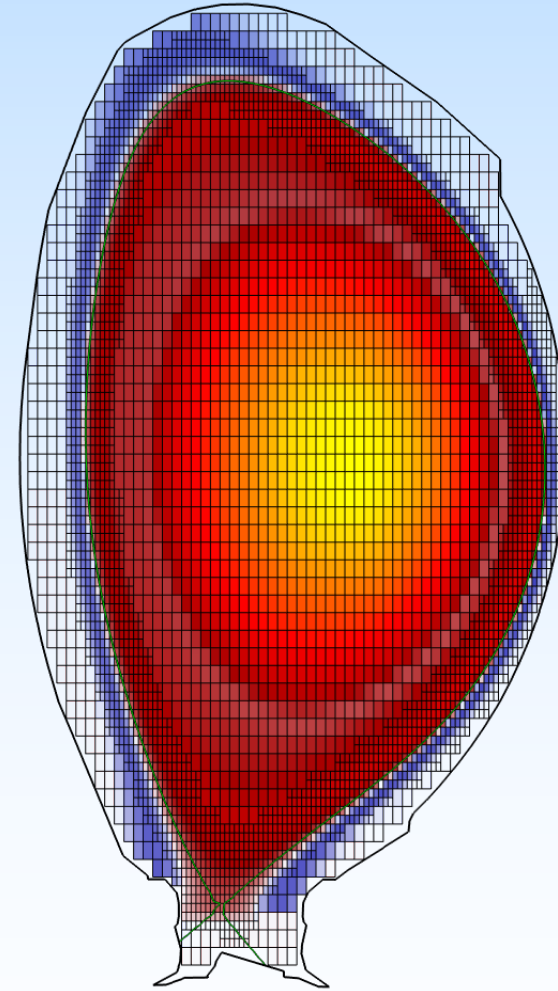
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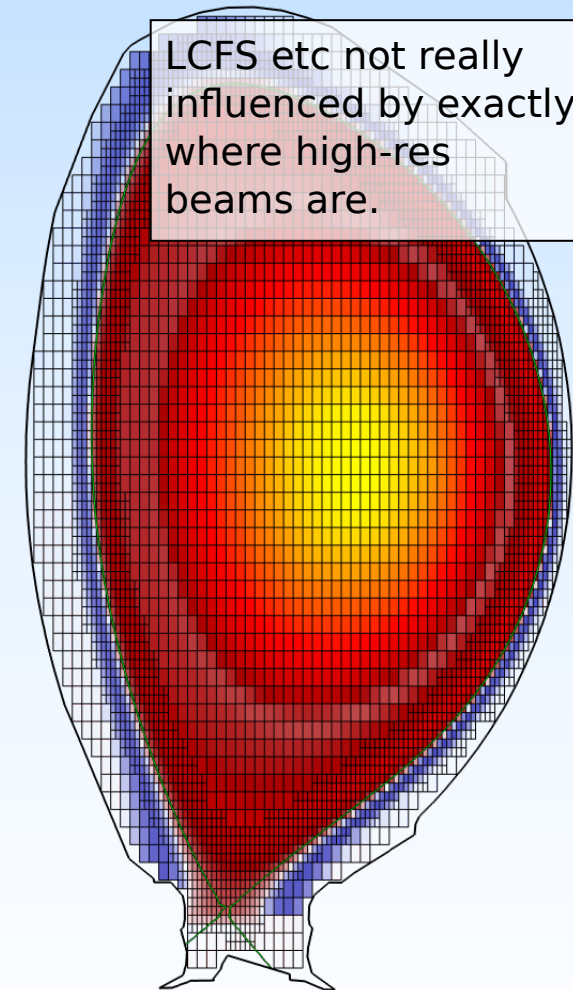
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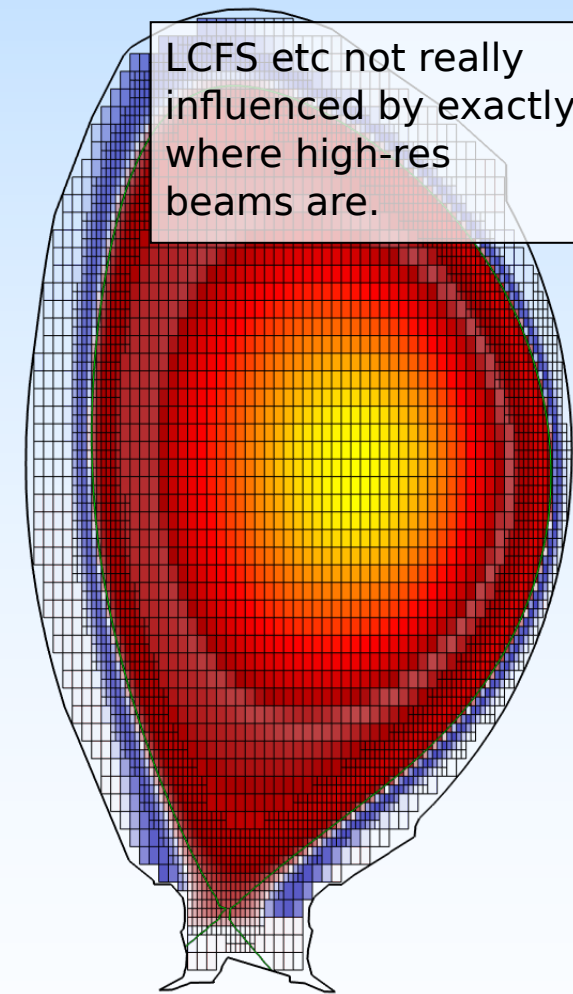
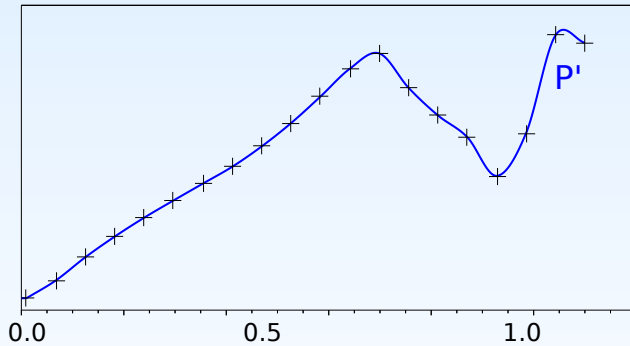


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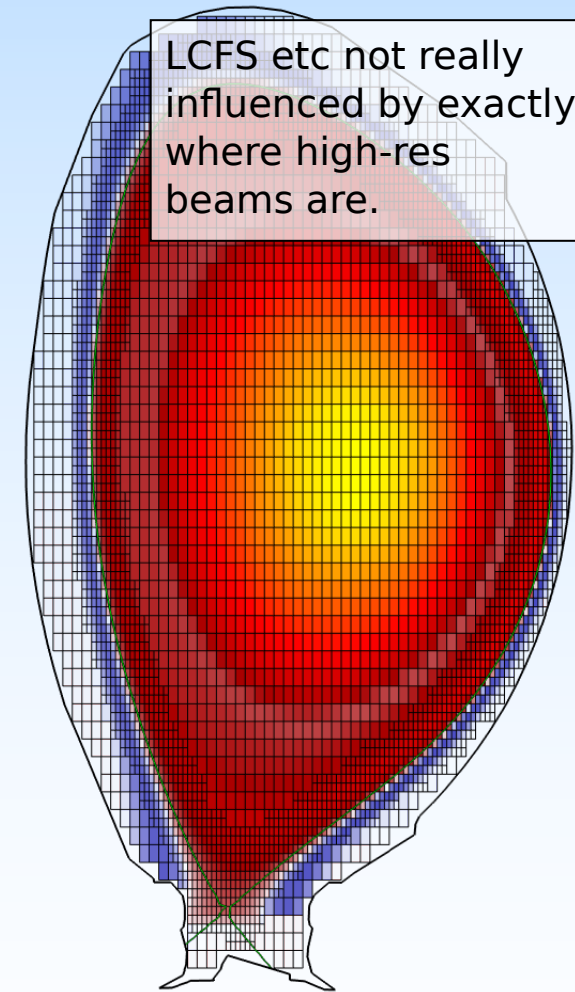
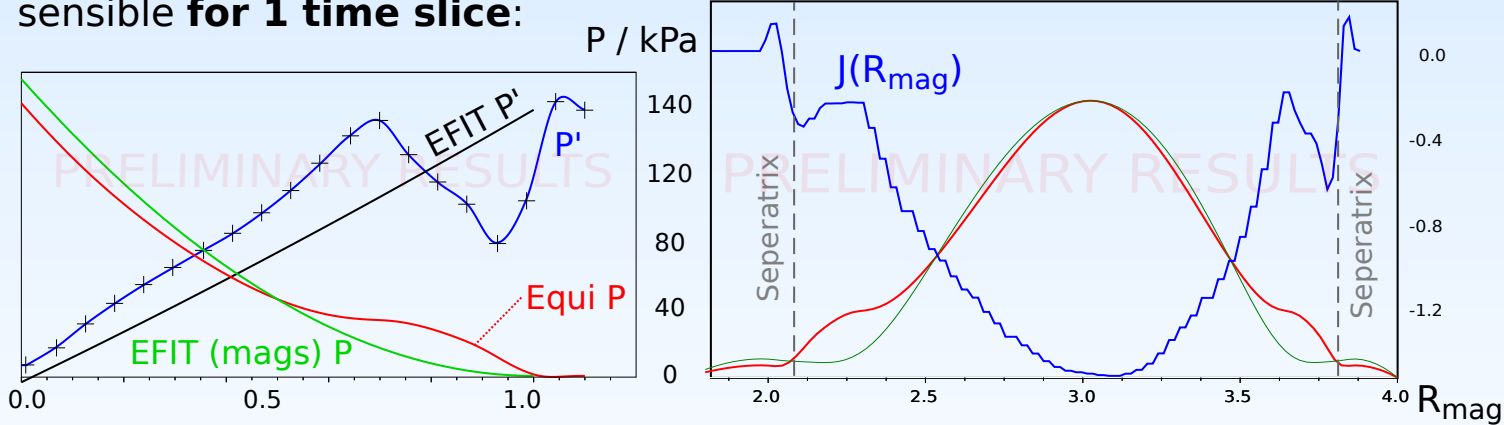
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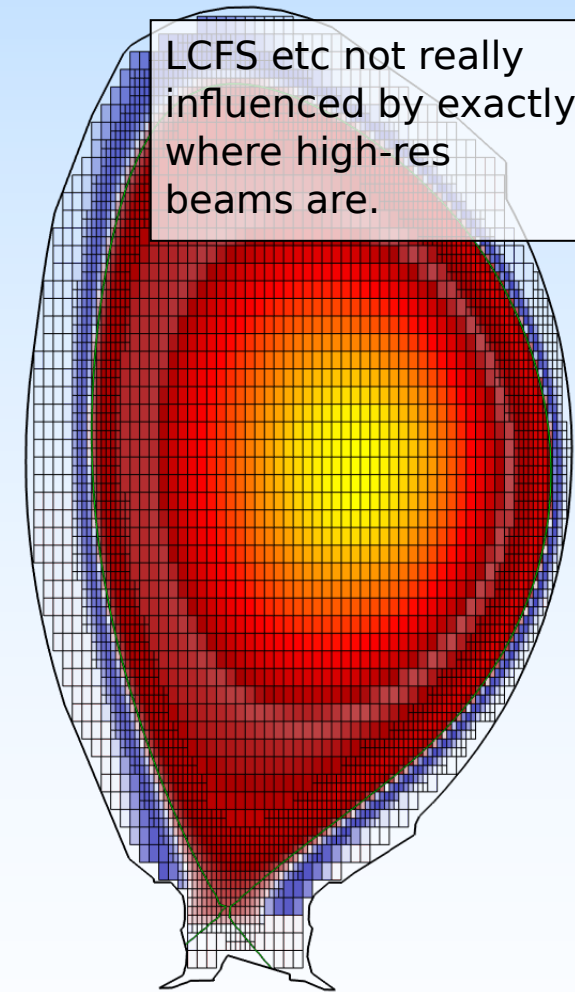
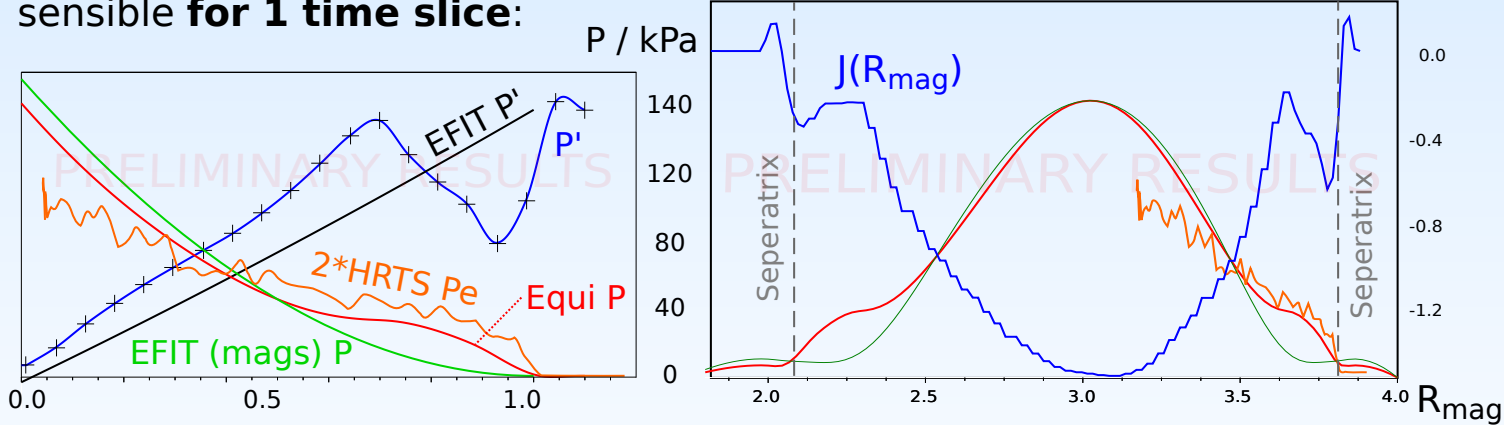
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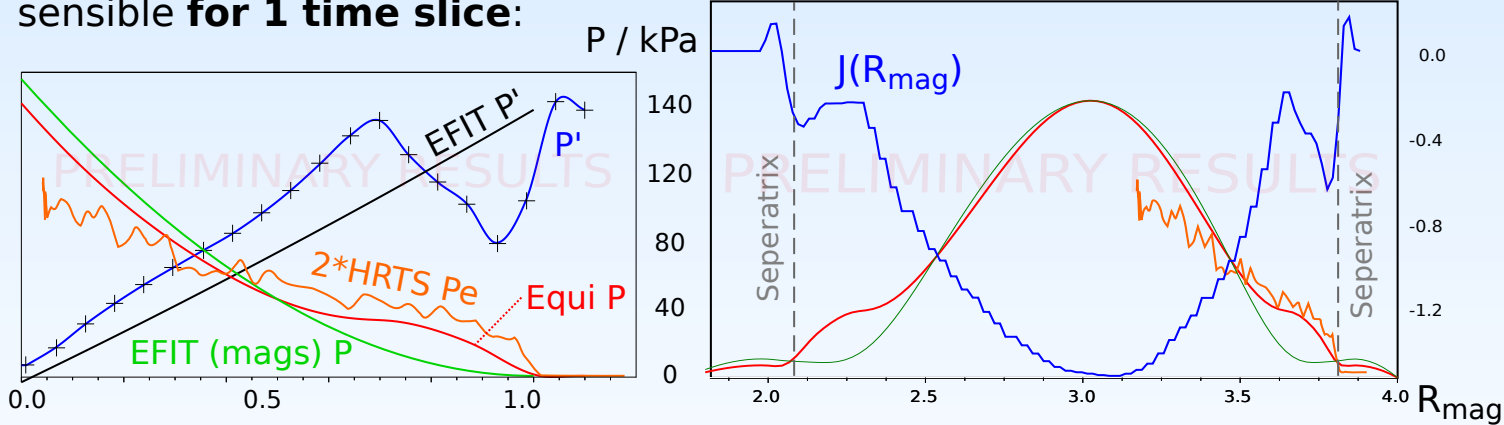
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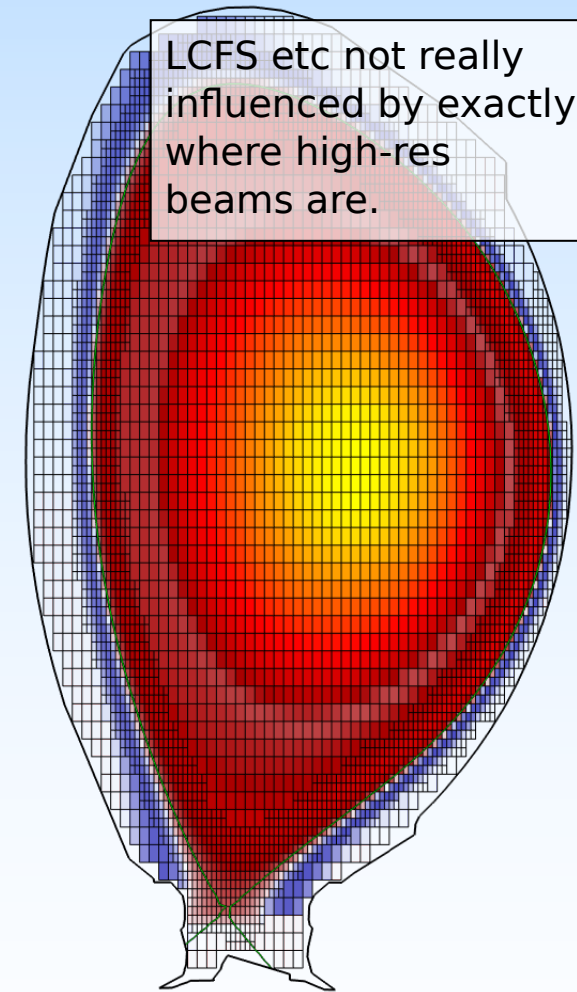
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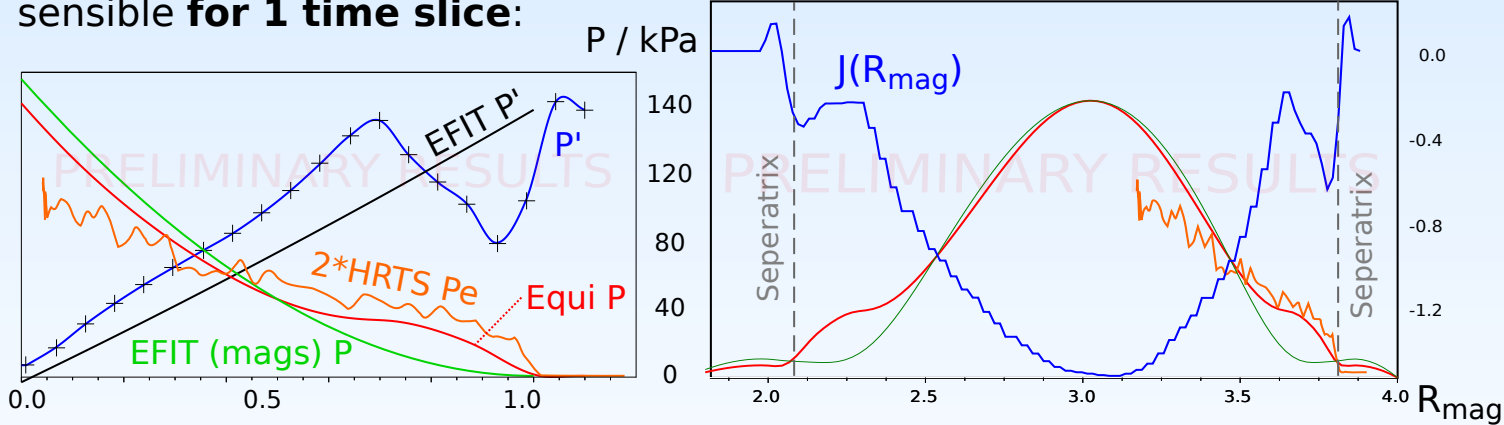
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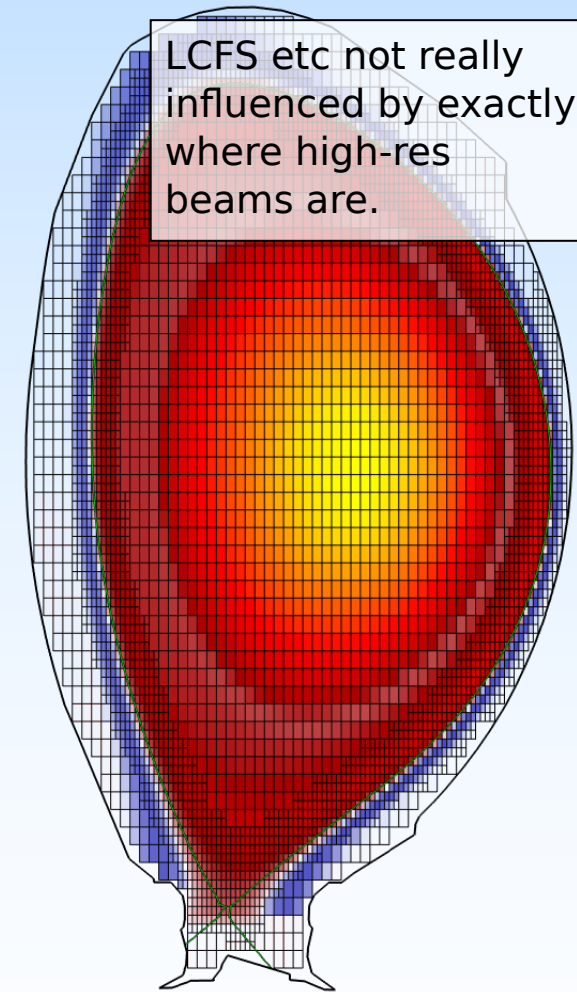
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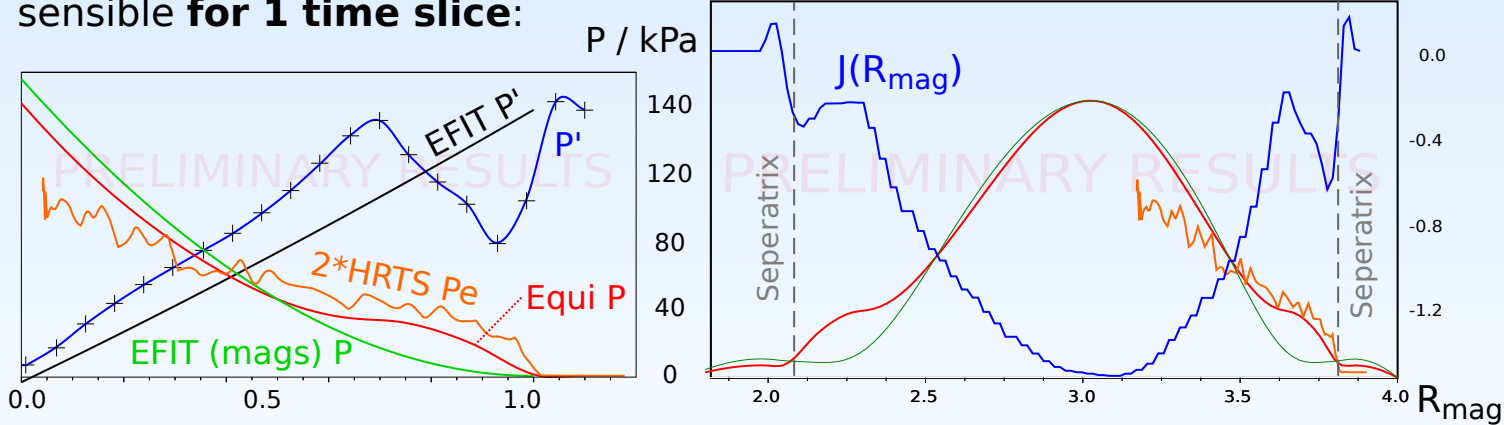
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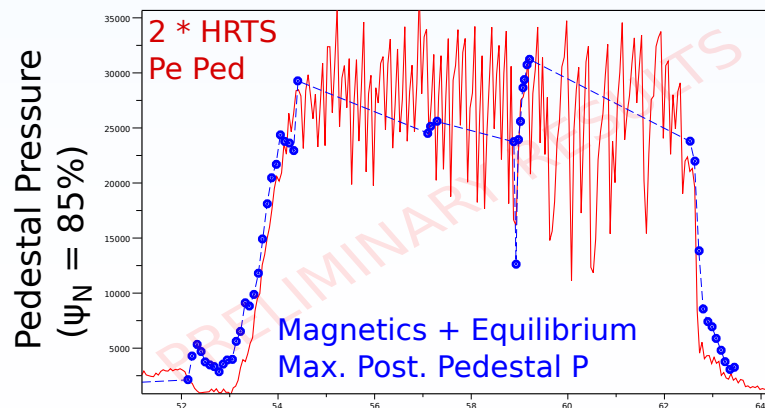
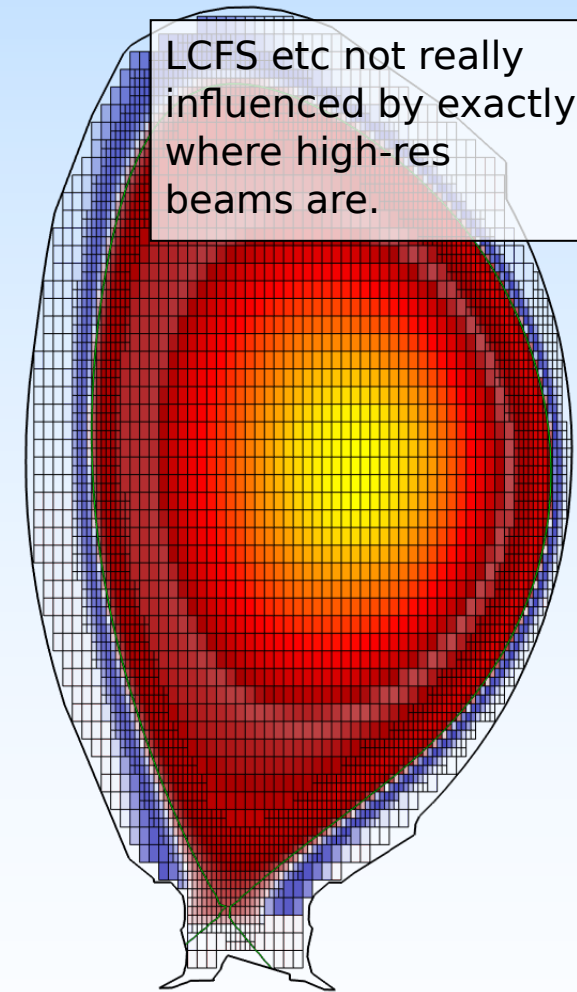
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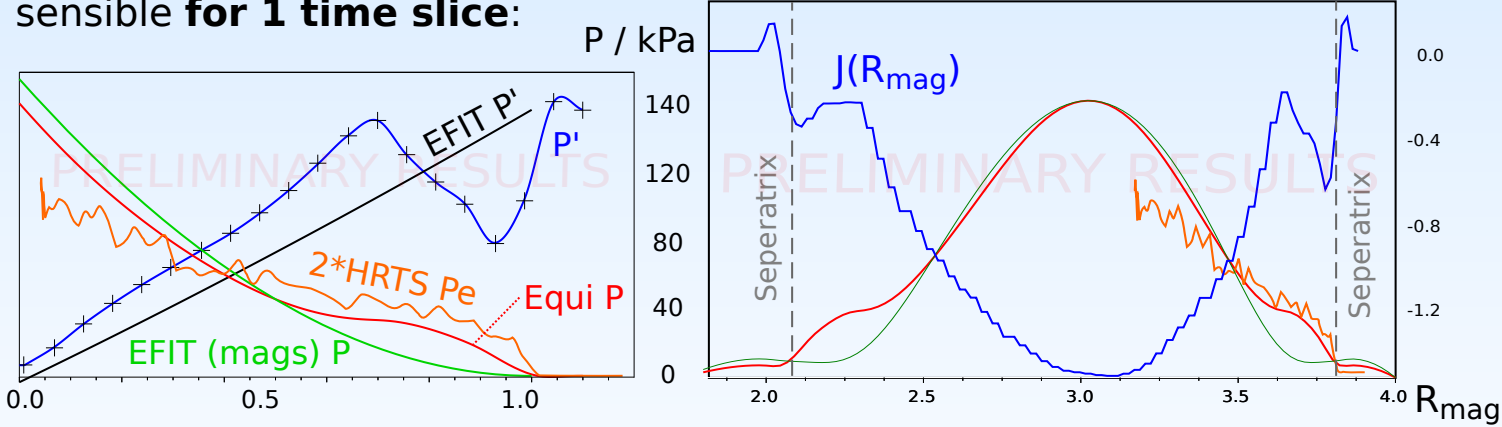
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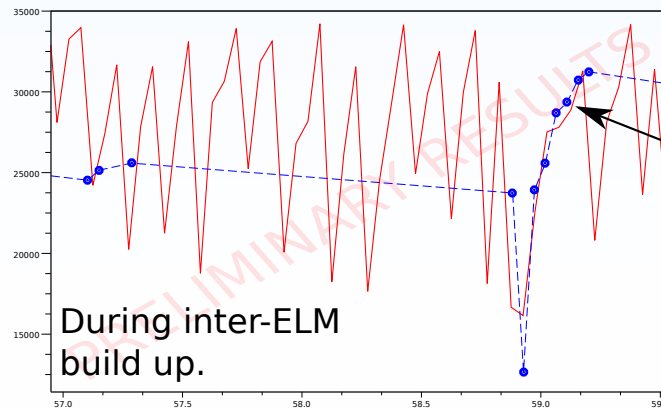
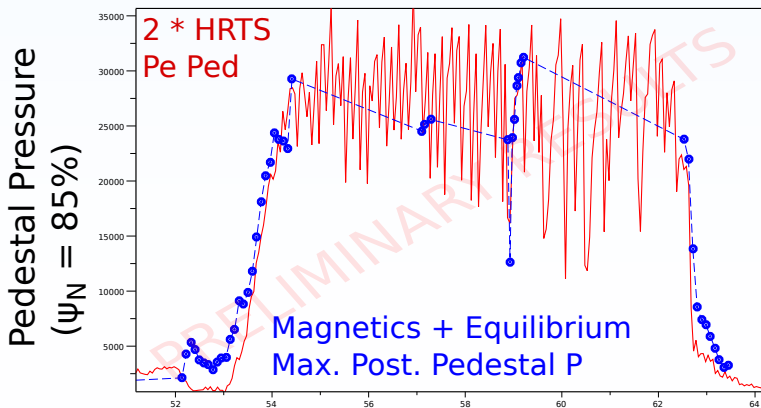
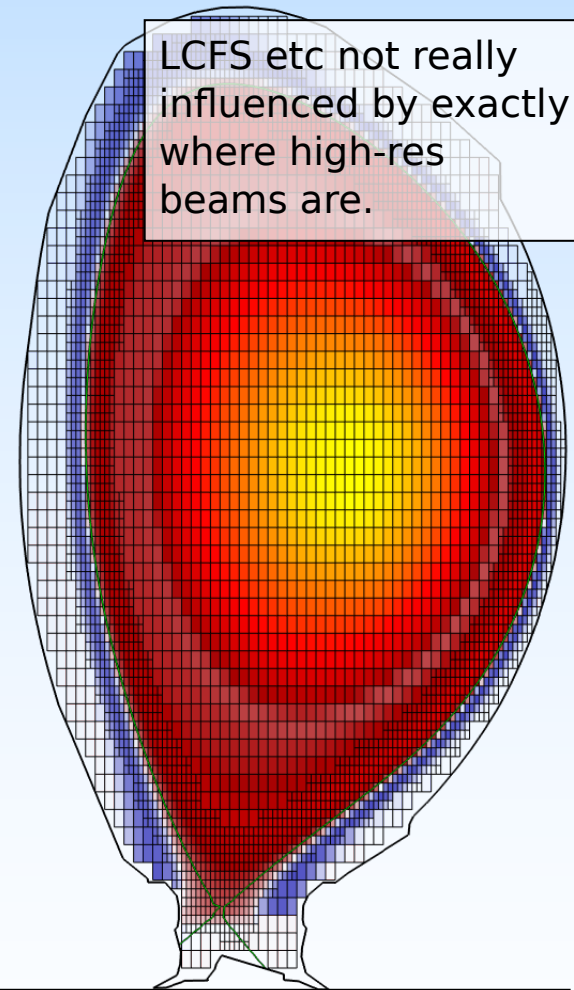
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Follows trends AND maintains surprisingly good magnitude. Suggests there is a quite lot of info in magnetics!  
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- ✓ Have a framework for analysing diagnostics which not only can cope with mapping uncertainty, but also automatically feeds back information from diagnostic to make inference on the mapping (currents).

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- ✓ Have a framework for analysing diagnostics which not only can cope with mapping uncertainty, but also automatically feeds back information from diagnostic to make inference on the mapping (currents).
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  - Do we get enough info to test current models at edge? - more use of the 'lots of stats'.
  - Can we see  $\nabla P / J_{||}$  evolution inter-ELM without assuming **anything** of where  $J_{||}$  comes from?