



# Motional Stark Effect Coherence Imaging for ASDEX Upgrade and W7X.

Assesment of capabilities using Bayesian Tomography

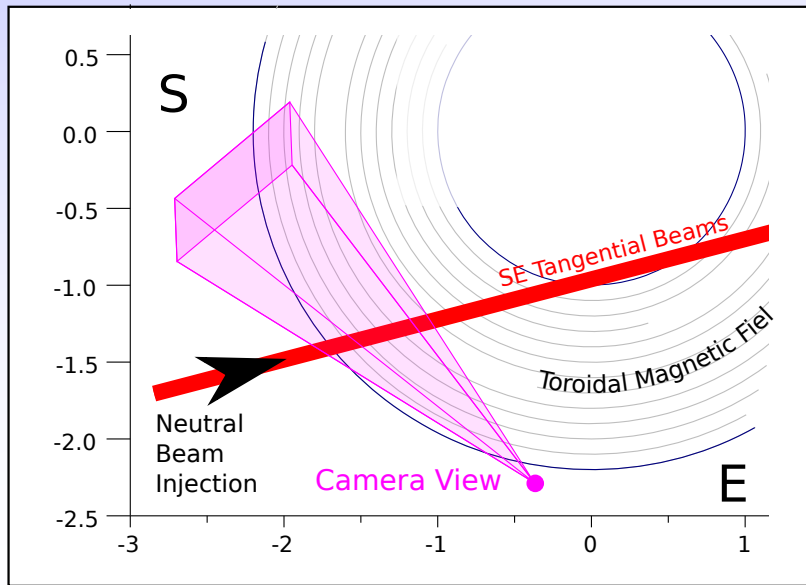
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- Introduction to IMSE.
- ASDEX Upgrade Instrument.
  
- 2D measurements with Axisymmetry.  
Mathmatically.  
Tomographically.
  
- W7X Instrument.  
Difficulites for Stellarators.  
Bayesian Inference using Funtion Parameterisation.

# Introduction - Motional Stark Effect



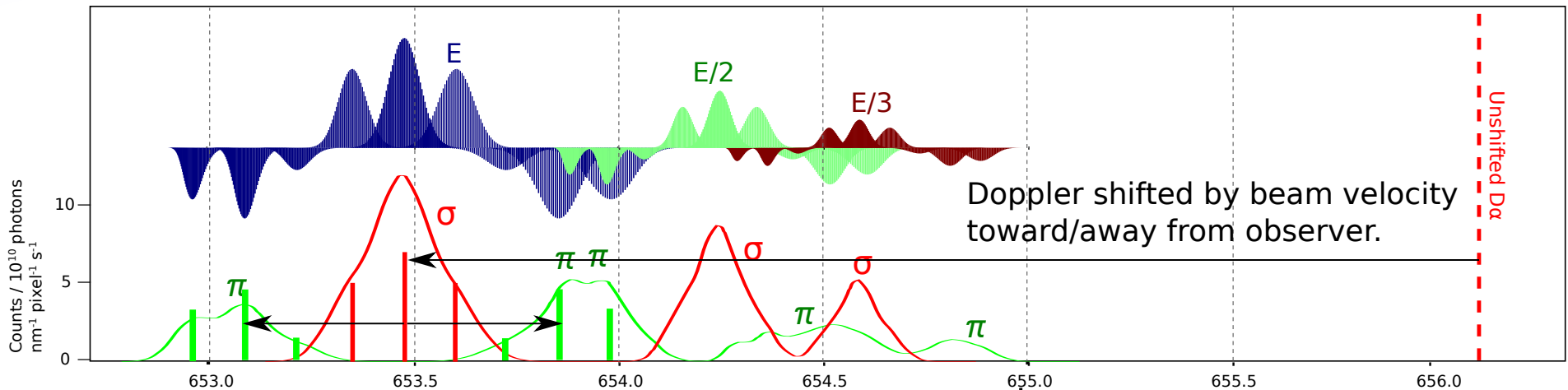
Neutral beam atoms injected into plasma.  
Excited by plasma, then emit H $\alpha$ /D $\alpha$  radiation.



Complications:

- Atoms with different injection energy: different Doppler shift.
- Doppler broadening: Beam divergence, line integration etc.
- Background D $\alpha$  (not shown).

Spectrum from a single pixel:



Stark split by electric field in rest frame of atom:

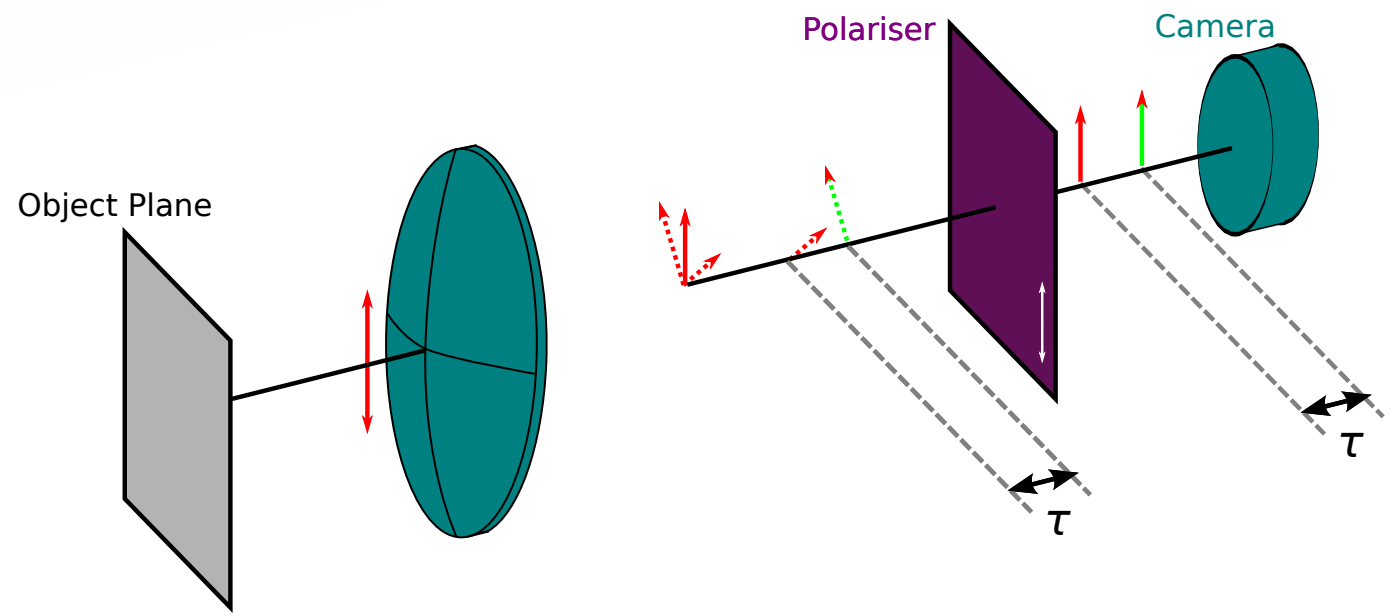
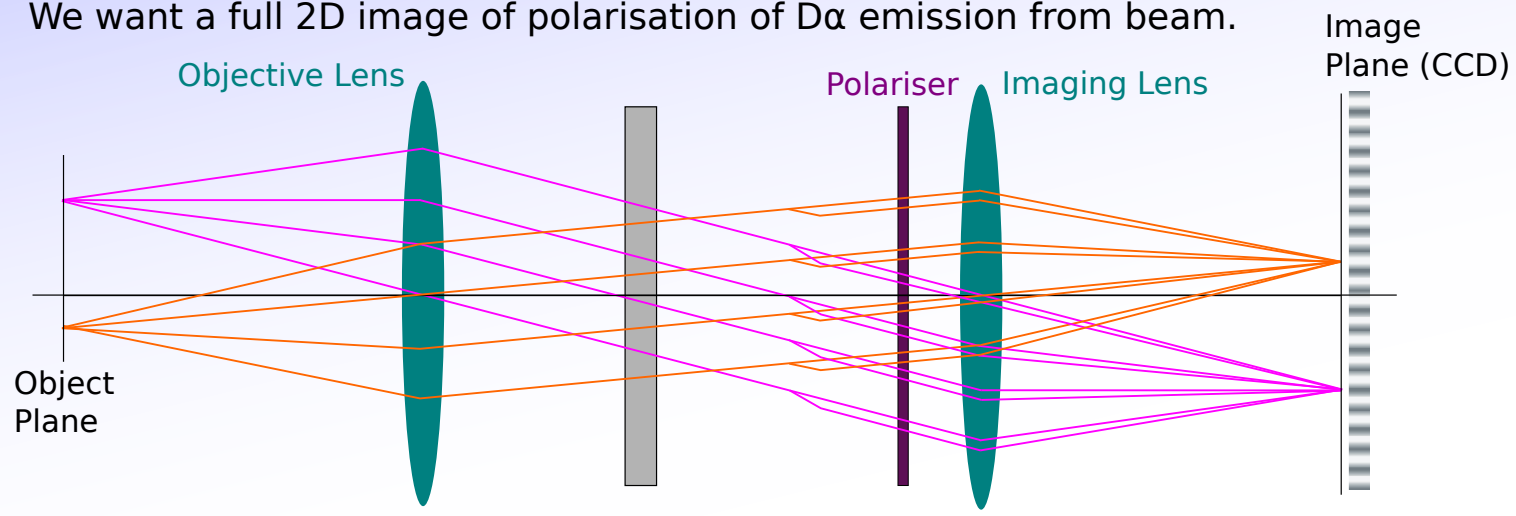
$$\mathbf{E} = \mathbf{v} \times \mathbf{B}$$

Roughly:  $\pi$  polarised parallel to E.

$\sigma$  polarised perp' to E.

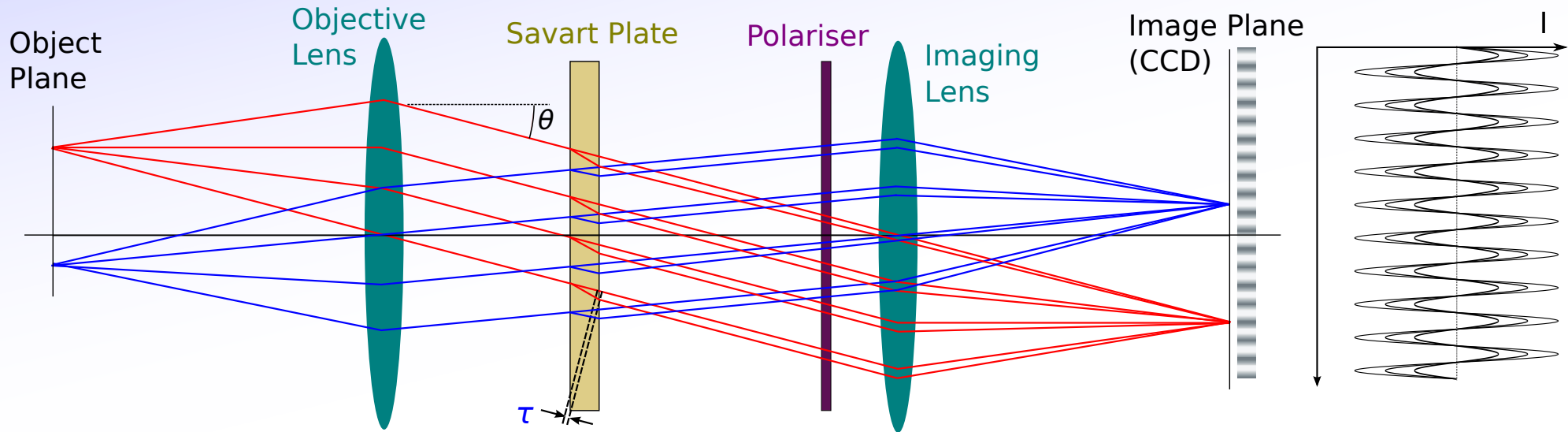
# Savart Plates

We want a full 2D image of polarisation of  $D\alpha$  emission from beam.



# Savart Plates

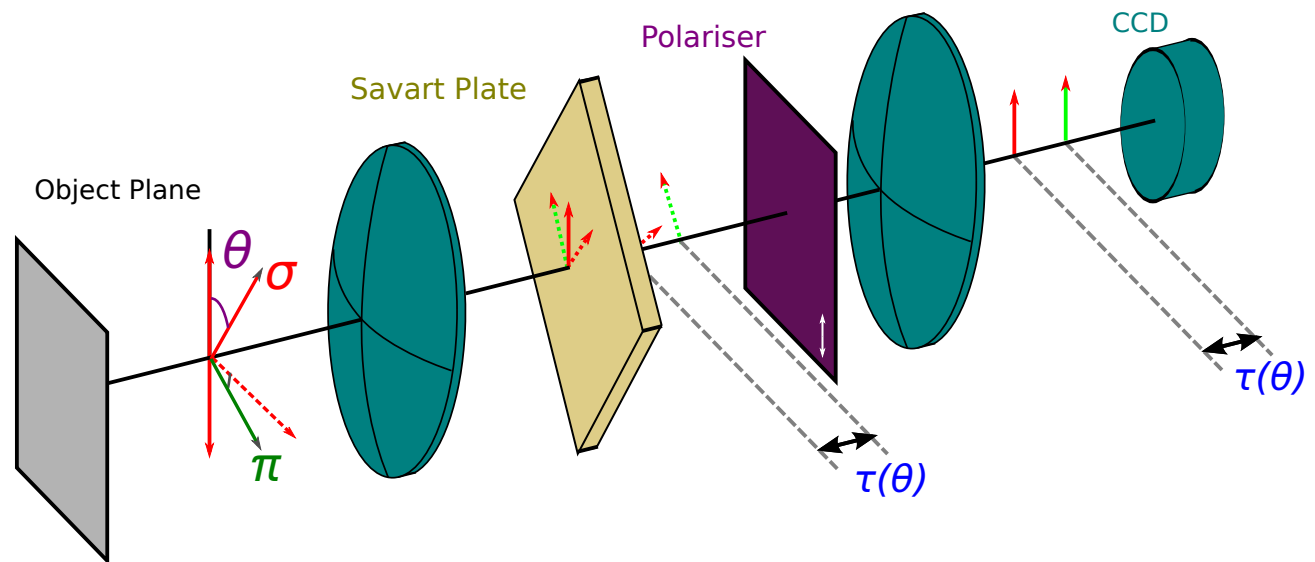
Savart Plate: Angle dependent phase shift --> Interference pattern accross image.



Oscillation amplitude proportional to polarisation angle.

$$I \propto 1 + \cos 2\theta \cos(x)$$

but  $\sigma$  and  $\pi$  are orthogonal.  
If they were monochromatic,  
they would cancel out...



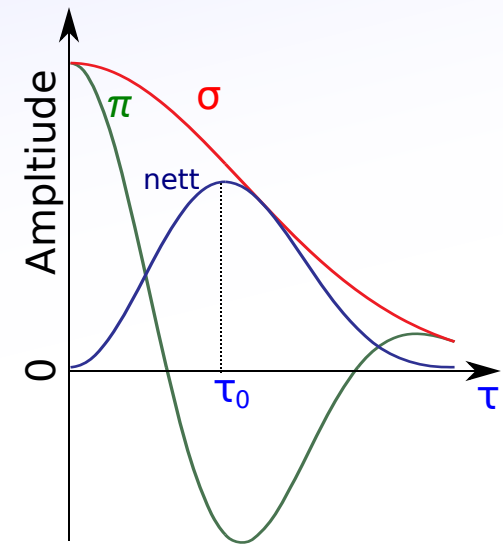
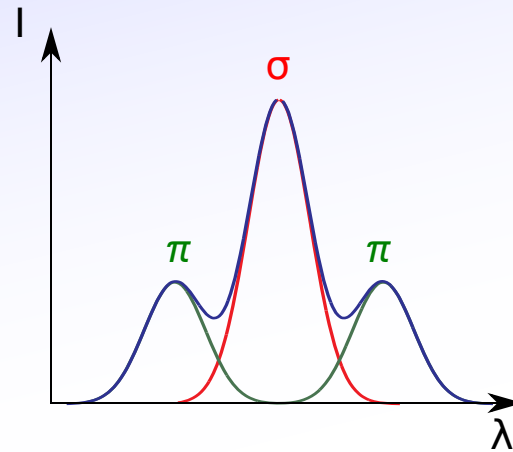
# Double Spatial Hetrodyne

MSE  $\pi$  and polarised  $\sigma$  are orthogonal and always the same intensity, but they have different spectral profiles.

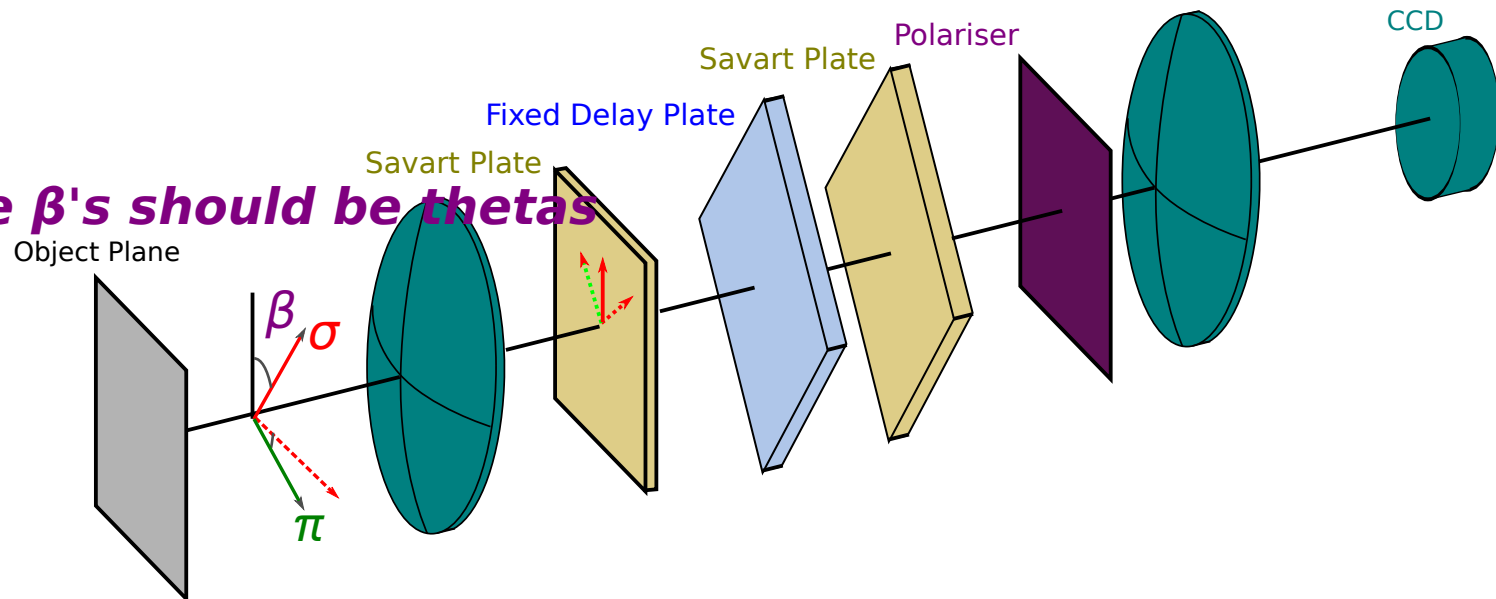
For large  $\tau$ , different wavelengths have different phases - decoherence.

Add a delay plate to introduce the best  $\tau_0$  - where  $\pi$  and  $\sigma$  combine constructively.

Amplitude dependant on contrast. To separate spectral this from  $\beta$ , add a second Savart plate at 45°, to create a 2nd carrier:



**\*\* All the  $\beta$ 's should be thetas**



# Double Spatial Hetrodyne

MSE  $\pi$  and polarised  $\sigma$  are orthogonal and always the same intensity, but they have different spectral profiles.

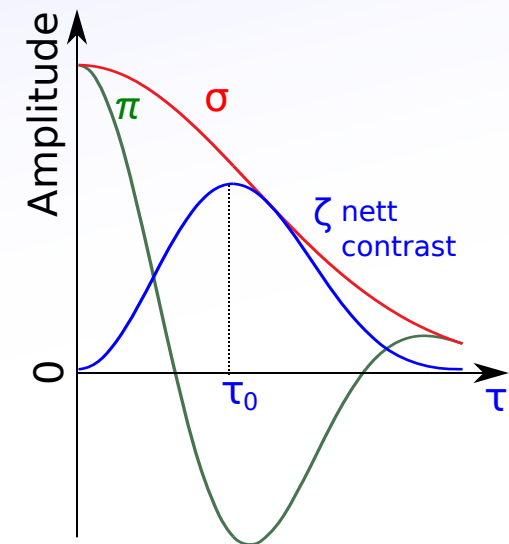
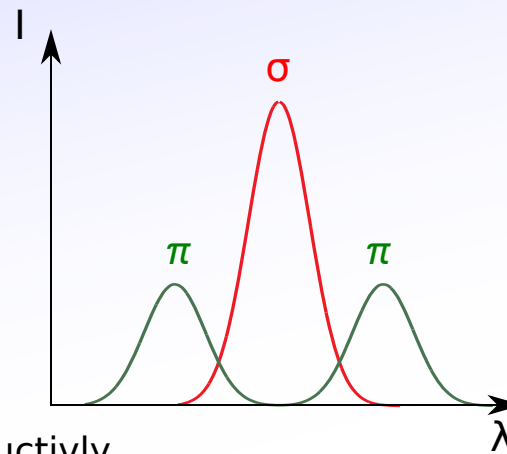
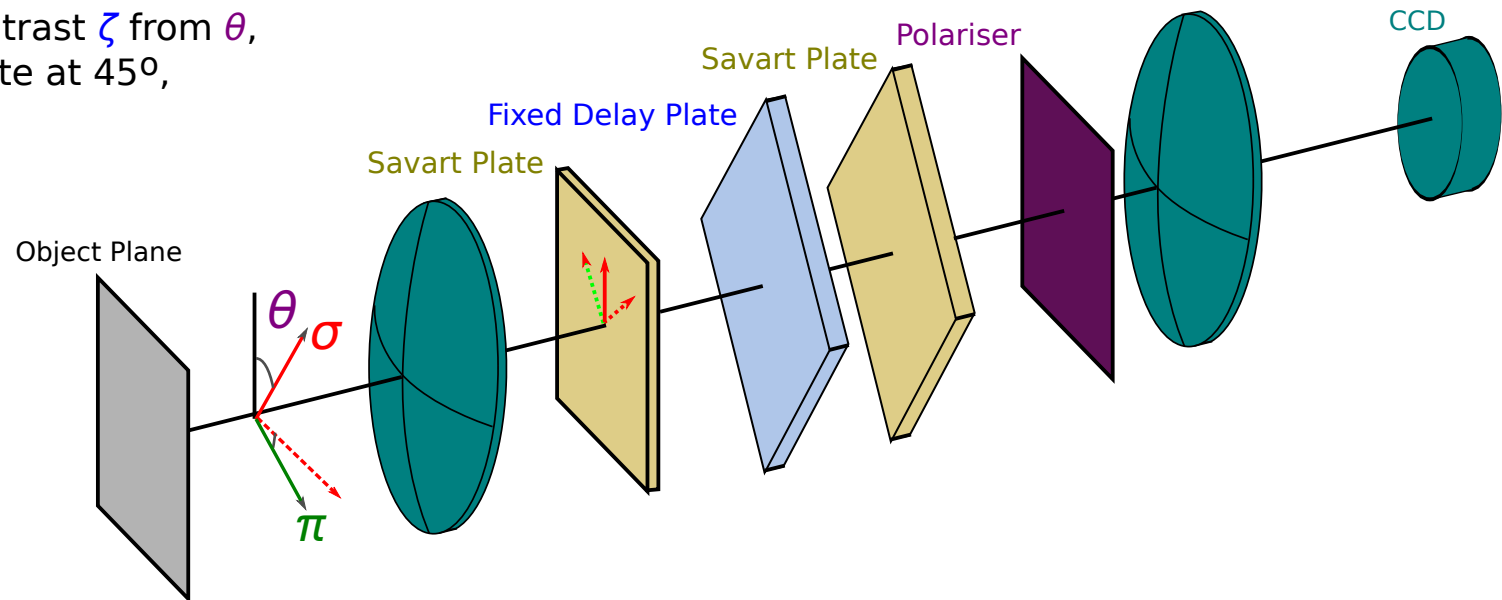
For large  $\tau$ , different wavelengths have different phases - decoherence.

Add a delay plate to introduce the best  $\tau_0$  - where  $\pi$  and  $\sigma$  combine constructively.

Amplitude also dependent on contrast.

$$I \propto 1 + \zeta \cos 2\theta \cos(x)$$

To separate spectral contrast  $\zeta$  from  $\theta$ , add a second Savart plate at  $45^\circ$ , to create a 2nd carrier:





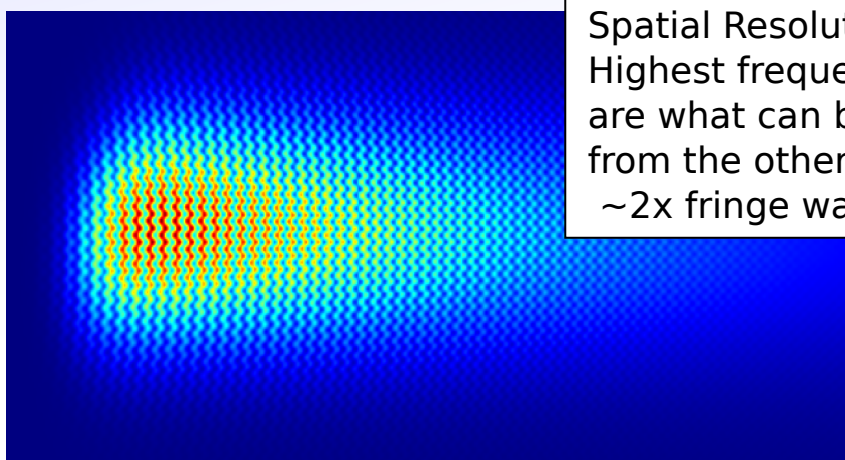
# Savart Plates

The equation for the image is now:

$$I = I_0 \left[ 1 + \zeta \left( \cos 2\theta \cos(x) + \frac{1}{2} \sin 2\theta \cos(x - y) - \frac{1}{2} \sin 2\theta \cos(x + y) \right) \right]$$

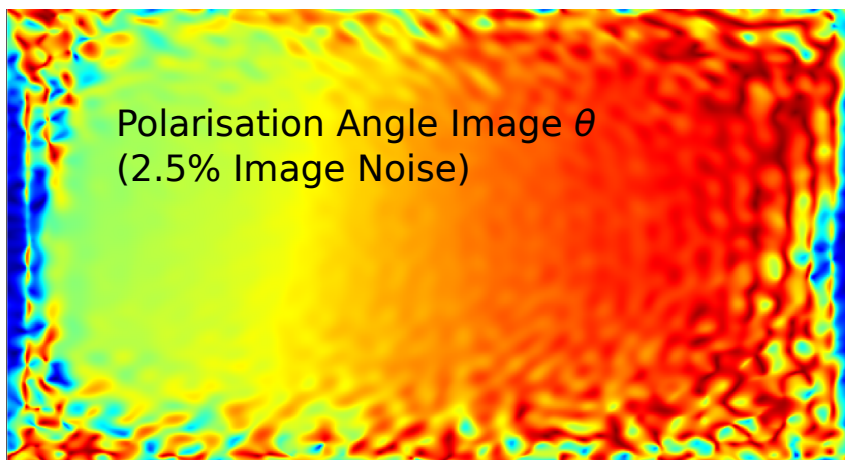
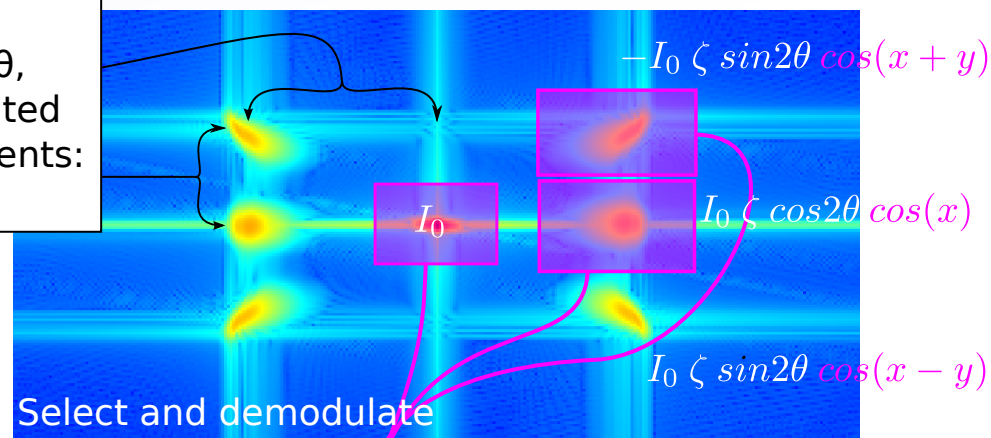
Intensity    Contrast    Polarisation Angle

By demodulating the image in x and y, we can find  $\theta$ ,  $I_0$  and  $\zeta$ .



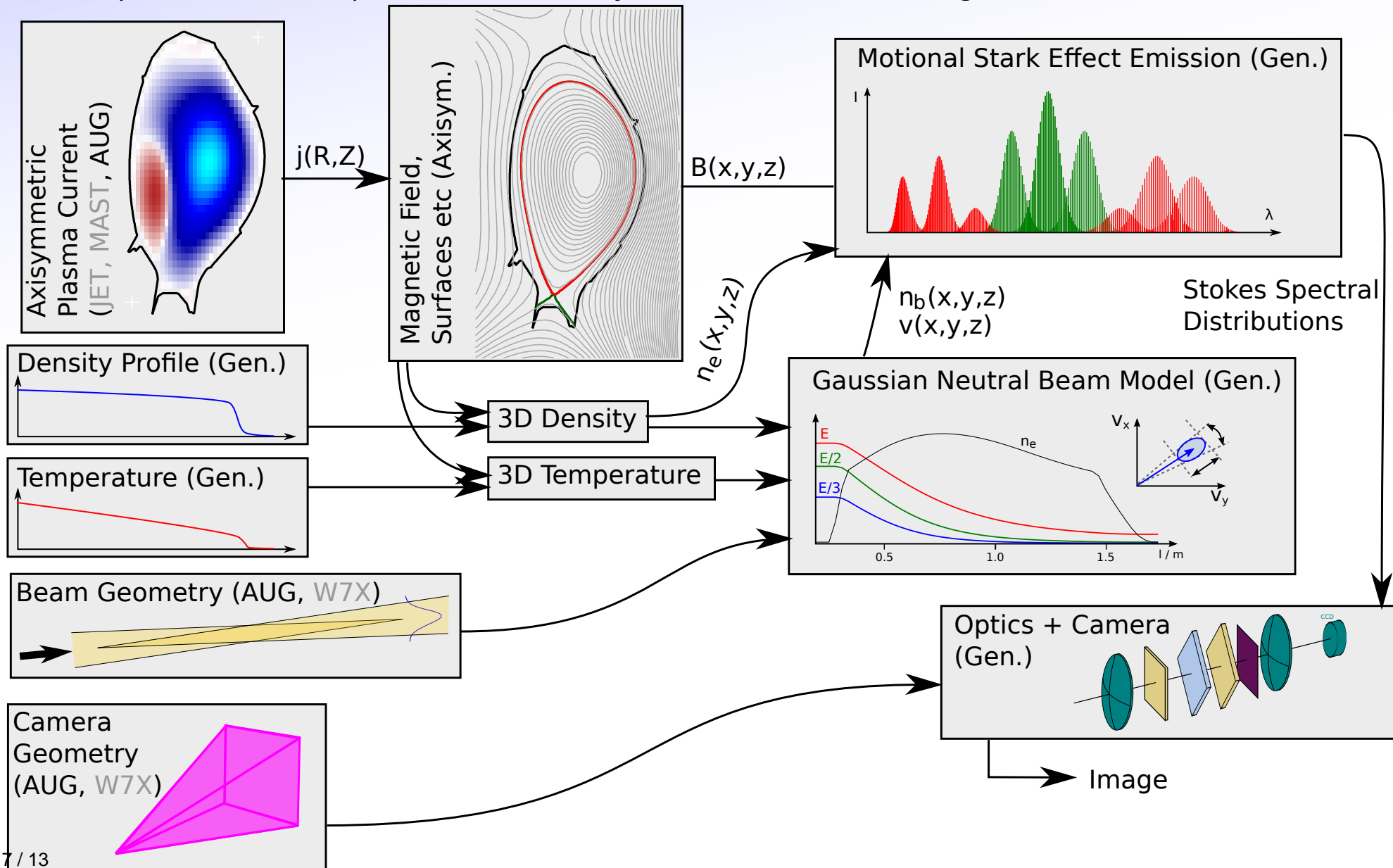
Spatial Resolution:  
Highest frequencies in  $\theta$ ,  
are what can be separated  
from the other components:  
~2x fringe wavelength

FT  
→



# Forward Model

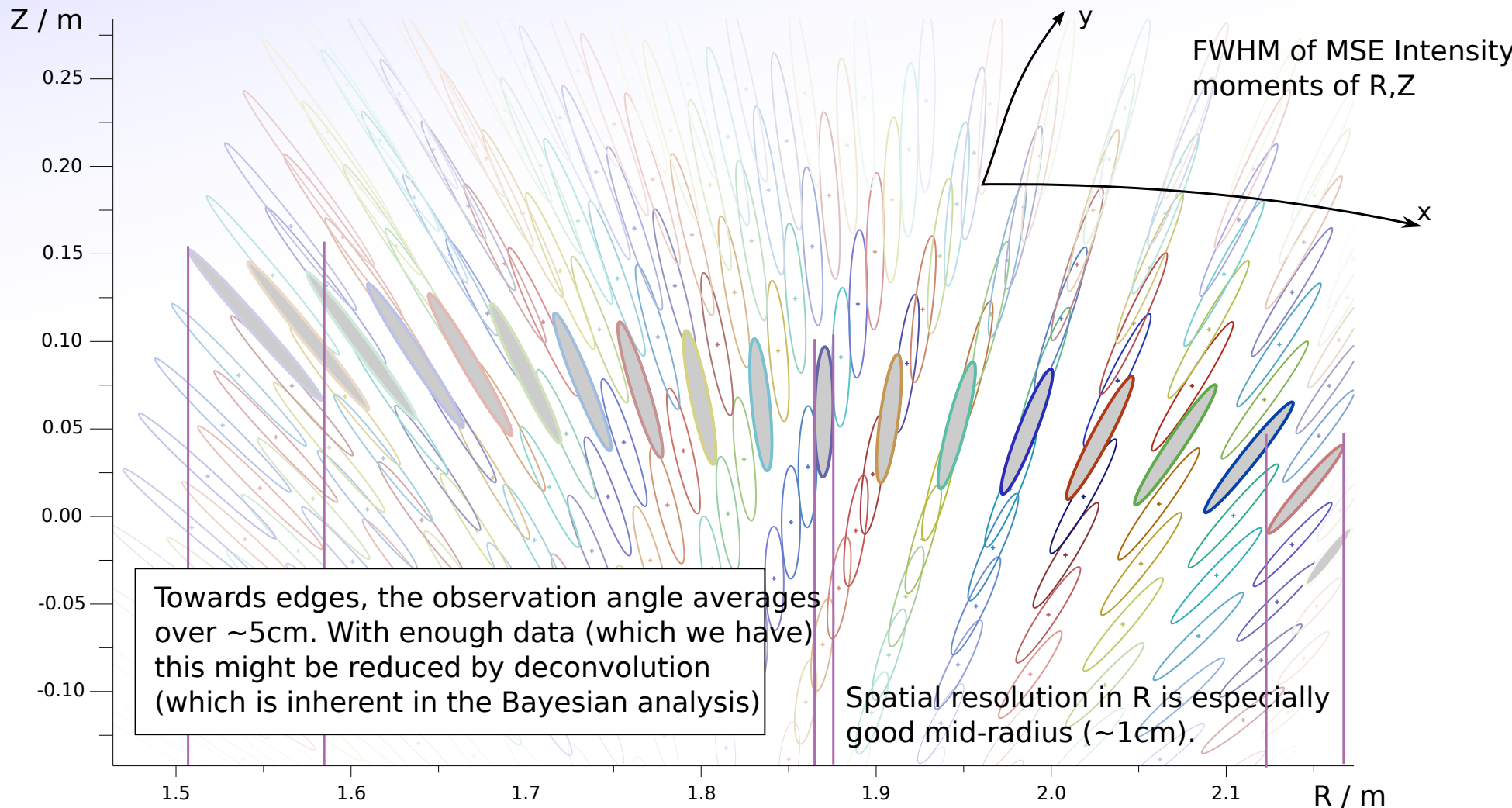
Developed several components for the Bayesian/Forward modelling framework





## AUG: $\theta$ Spatial Resolution

The recovered  $\theta$  are really  $\langle \theta \rangle$  over the LOS. Spatial resolution is a combination of pixel-pixel averaging due to modulation (1cm) and the LOS averaging. The LOS averaging varies over image (x,y):





# Recovery of plasma current - Axisymmetric

To final objective is to measure plasma current  $j$ .

For normal 1D measurements: not possible so  $\theta$  used as a constraint for equilibrium.

Does having 2D measurements make it possible to calculate  $j$  without equilibrium?

Assuming toroidal symmetry, the current is:

$$-\mu_0 j_\phi = \frac{\partial B_z}{\partial R} + \frac{1}{R} \frac{\partial^2}{\partial Z^2} \int_0^R R' B_z(R', Z) dR'$$

Assume we know  $B_\phi$  as the vacuum field, then we can calculate  $B_z$  from  $\theta$ .

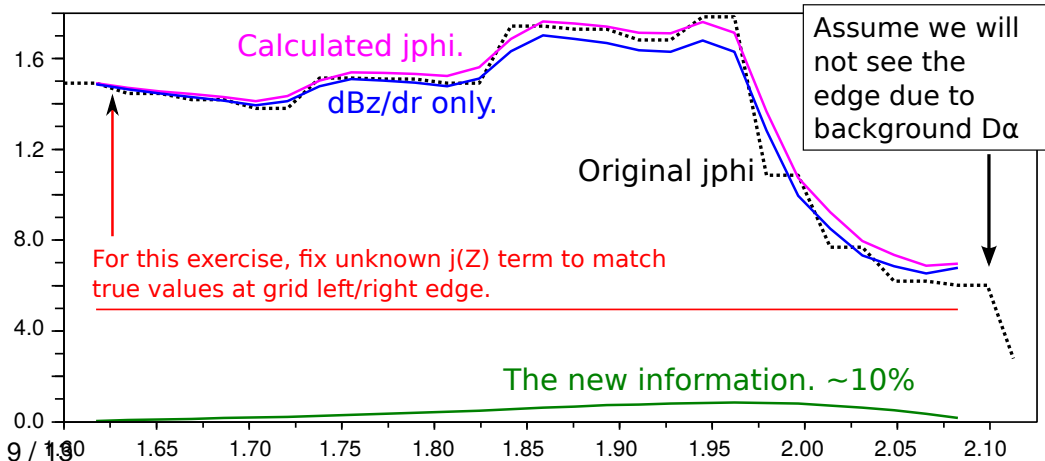
However, we only see where the MSE emission is, so can only integrate from some  $R = R_0$ :

$$-\mu_0 j_\phi = \underbrace{\frac{\partial B_z}{\partial R}}_{\text{This we have with 1D MSE.}} + \underbrace{\frac{1}{R} \frac{\partial^2 \psi(R_0, Z)}{\partial Z^2}}_{\text{Function of Z that we cannot know.}} + \underbrace{\frac{1}{R} \frac{\partial^2}{\partial Z^2} \int_{R_0}^R R' B_z(R', Z) dR'}_{\text{The new term gives localisation of current in Z (~via curvature of field).}}$$

With the **new term**, we can in theory calculate  $j_\phi$  profiles except for a fixed constant (because the **f(Z)** term is still not known).

In practice,  $d^2B/d^2$  is much too noisy.

However, we also gain  $dB_z/dR$  at different  $Z$ s. Together with normal coil measurements, it is now part of a complex tomography problem



$$\psi(R, Z) = \int_0^R R' B_z(R', Z) dR'$$

$$-\mu_0 j_\phi = \frac{\partial B_z}{\partial R} + \frac{1}{R} \frac{\partial^2 \psi}{\partial Z^2}$$

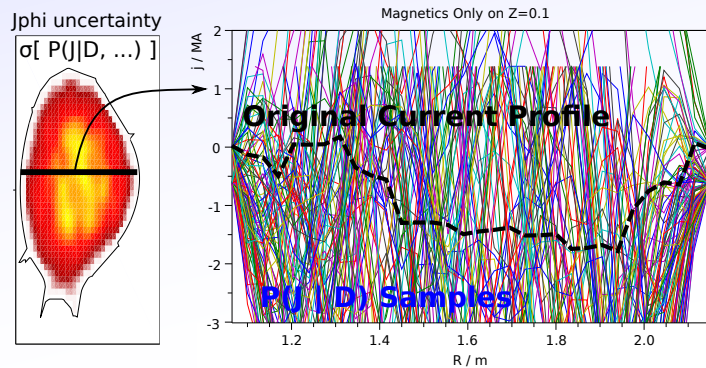
$$-\mu_0 j_\phi = \frac{\partial B_z}{\partial R} + \frac{1}{R} \frac{\partial^2}{\partial Z^2} \int_{R_0}^R R' B_z(R', Z) dR'$$

$$-\mu_0 j_\phi = \frac{\partial B_z}{\partial R} + \frac{1}{R} \frac{\partial^2}{\partial Z^2} \left( \int_0^{R_0} R' B_z(R', Z) dR' + \int_{R_0}^R R' B_z(R', Z) dR' \right)$$

# By current tomography...

Add model for AUG PF coils, pickups etc to Minerva. Can now do Current Tomography and Bayesian Equilibrium for AUG.

**1) Magnetics only:** We have the usual tomography situation:



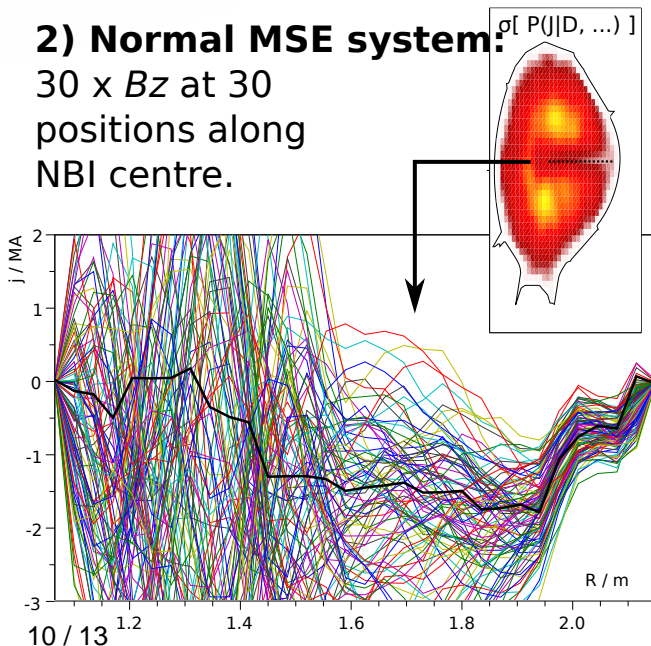
(Almost) no prior/regularisation

(Almost) infinite uncertainty  
(but B and flux still good)

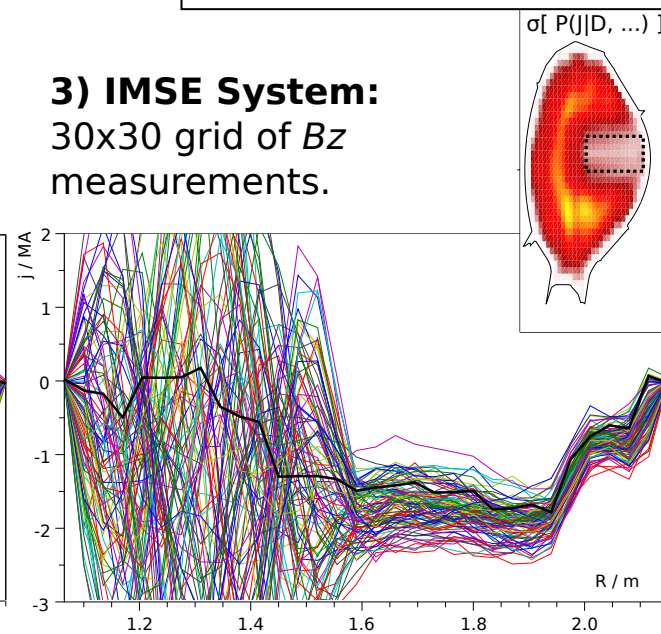
Each case has 900 measurements at  $\sigma = 10mT$ .  
So difference is only in the **type** of information.

**2) Normal MSE system:**

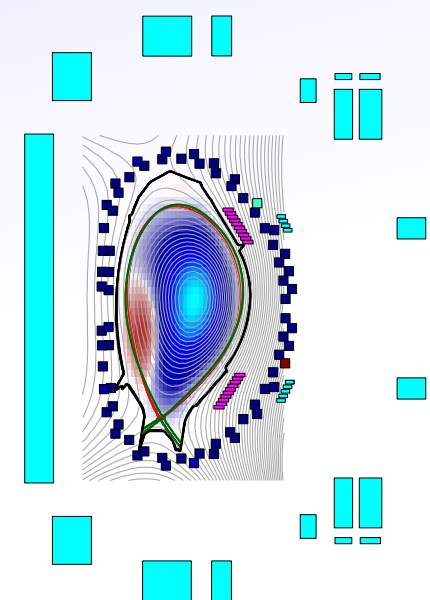
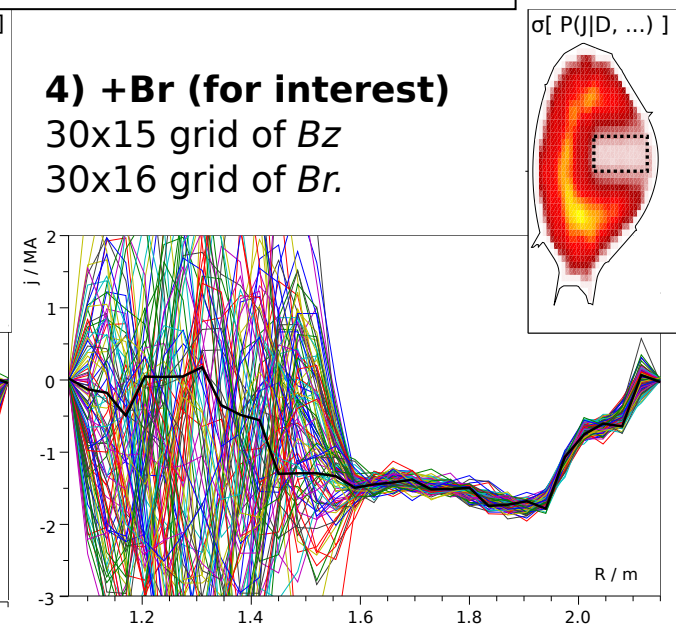
30 x  $B_z$  at 30  
positions along  
NBI centre.



**3) IMSE System:**  
30x30 grid of  $B_z$   
measurements.

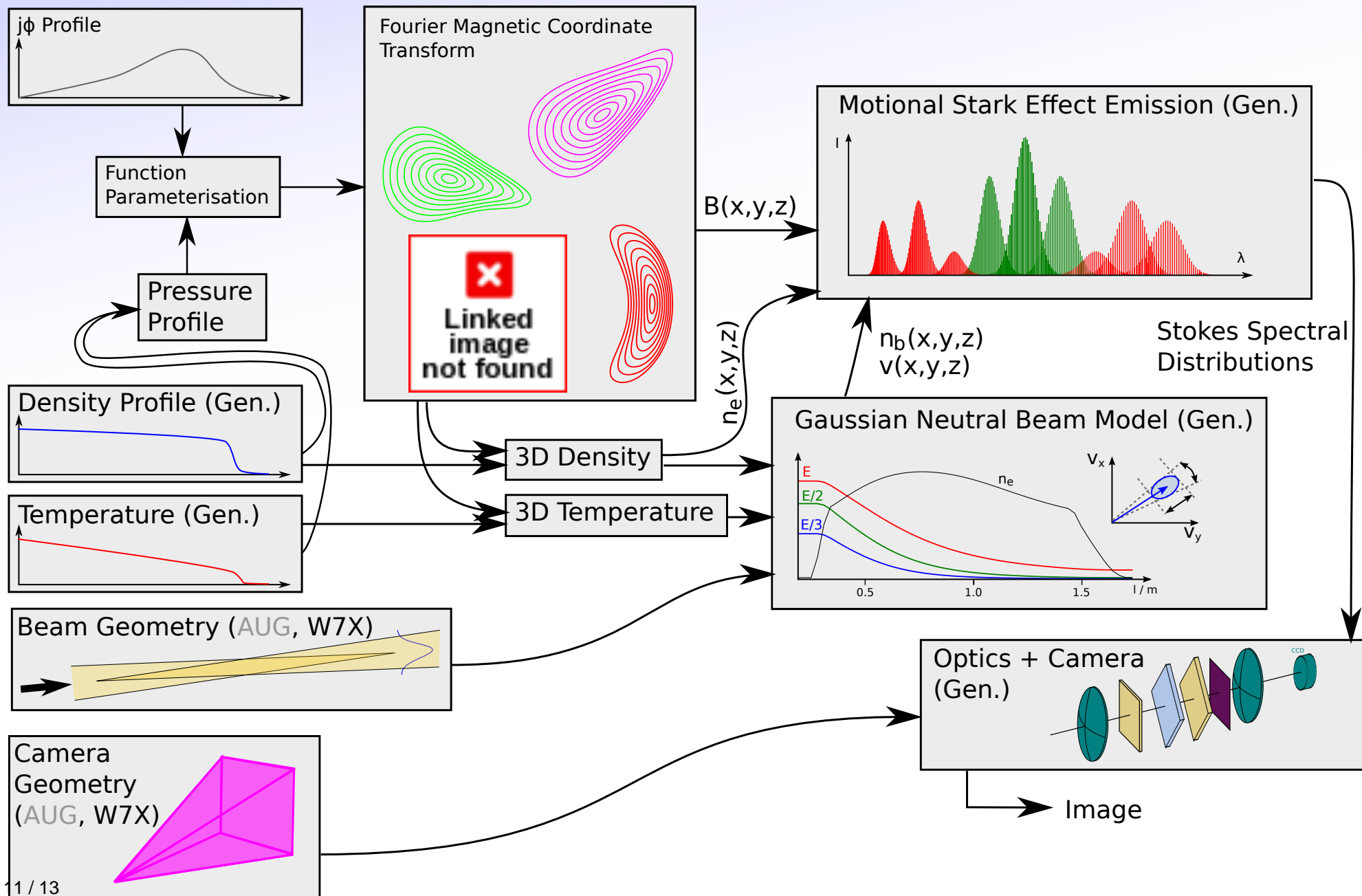


**4) +Br (for interest)**  
30x15 grid of  $B_z$   
30x16 grid of  $Br$ .



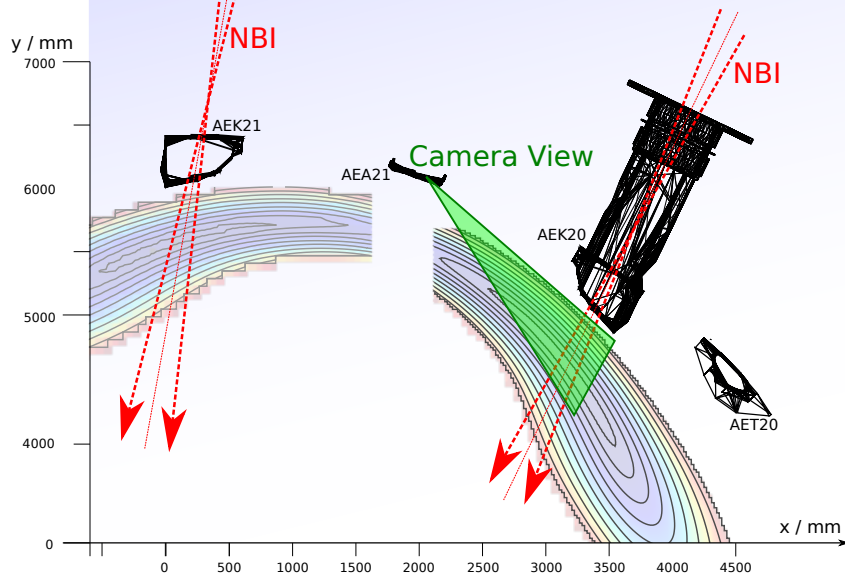


# Forward Model (W7X)



## Geometry (W7X)

Best view of NBI to reduce cross-surface integration: from port AEA21, looking along const Z plane.  
More tangential lower beam gives best Doppler shift --> Better image fringe contrast.



View is almost to surfaces here --> Reasonable flux surface resolution:  
Beam attenuation is rapid due to high electron density so only outboard side is seen: