



3rd IAEA Technical Meeting on Fusion Data Processing, Validation and Analysis

Forward modelling for the design and analysis of polarisation imaging diagnostics.

Oliver. P. Ford¹

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ASDEX-Upgrade Team¹

1: Max-Planck Institut für Plasmaphysik, Greifswald/Garching, Germany

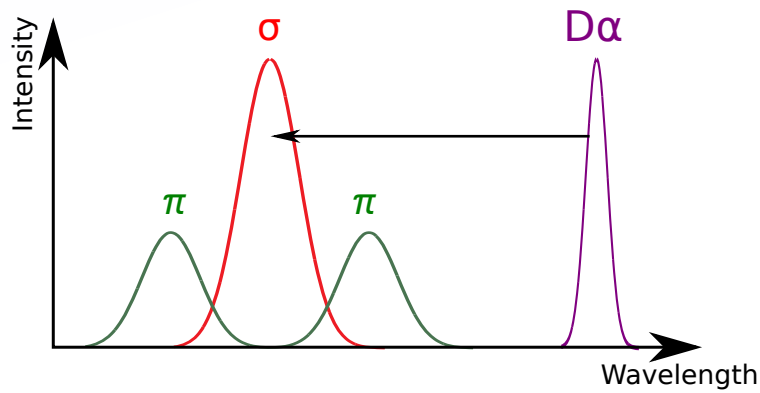
2: Australian National University, Canberra, Australia

3: UKAEA Fusion Association, Culham Science Centre, OX14 3DB, UK

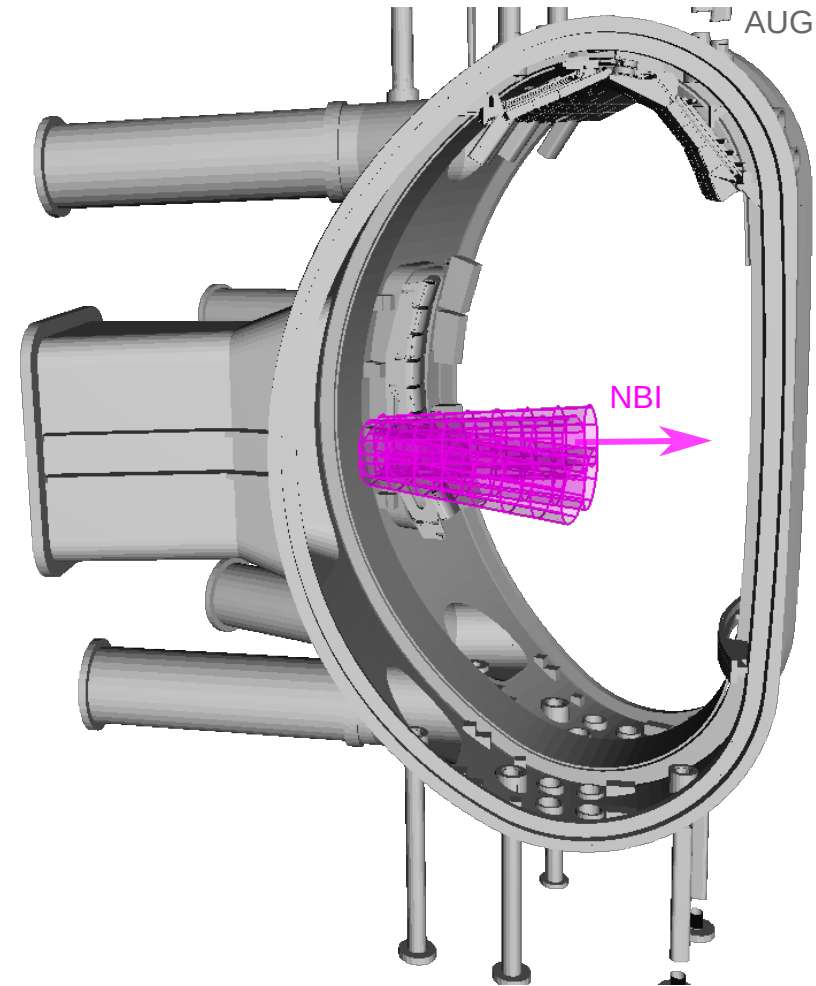
(Imaging) Motional Stark Effect at AUG

ASDEX Upgrade has an existing 10-channel MSE system.

- H α /D α beam emission is Doppler shifted and split by the Motional Stark Effect into π and σ components.



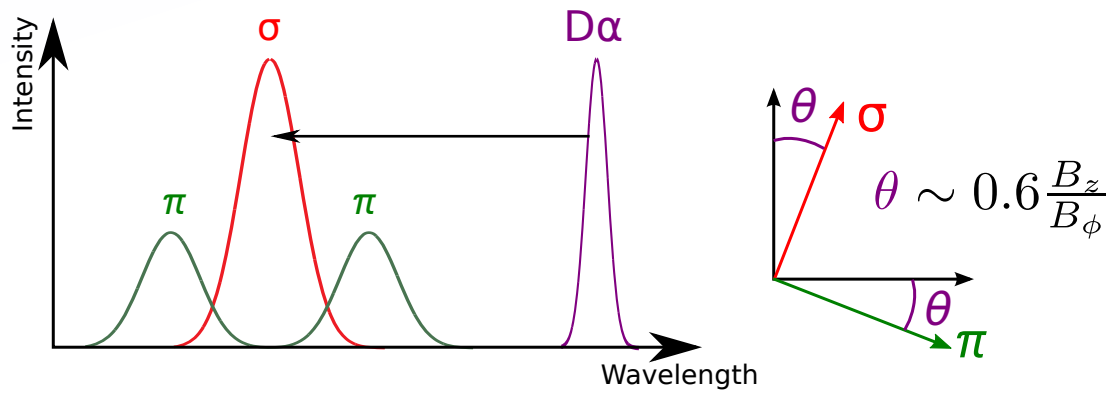
Conventional MSE



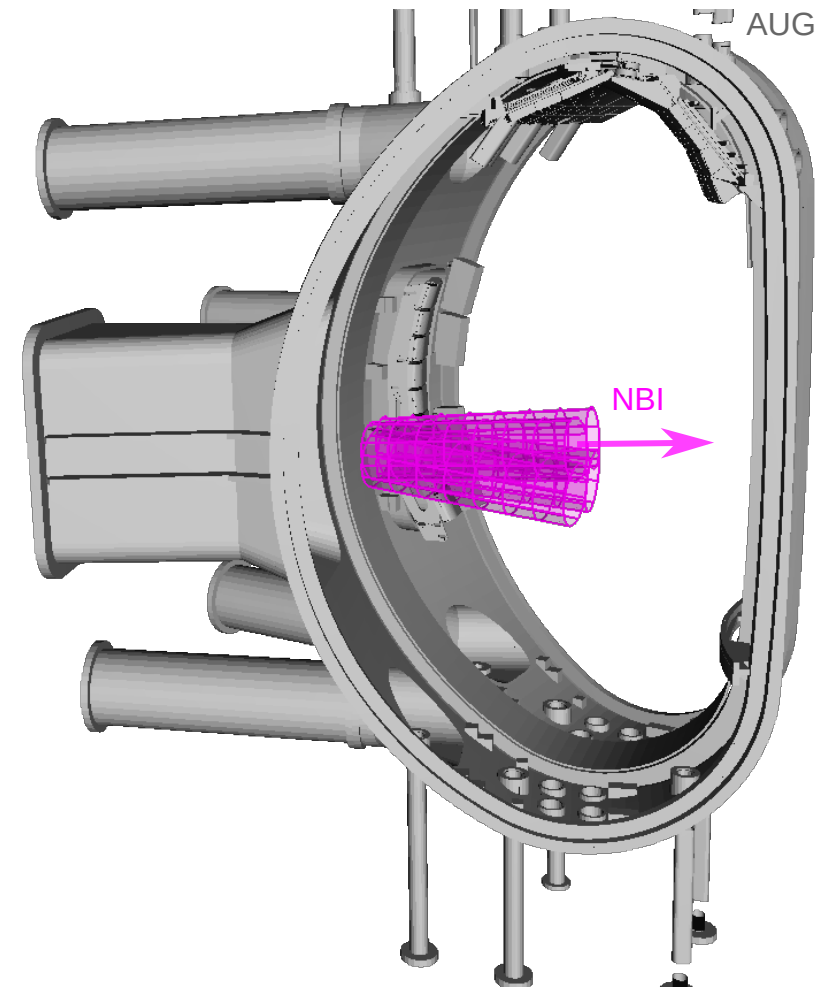
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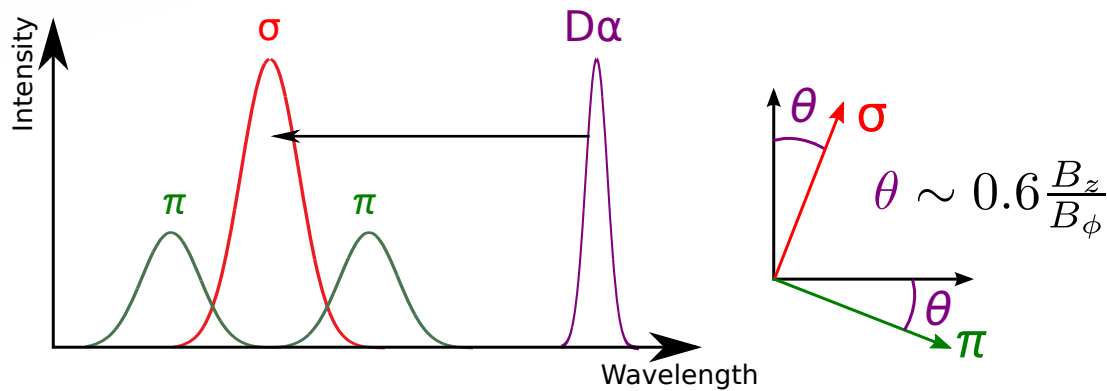
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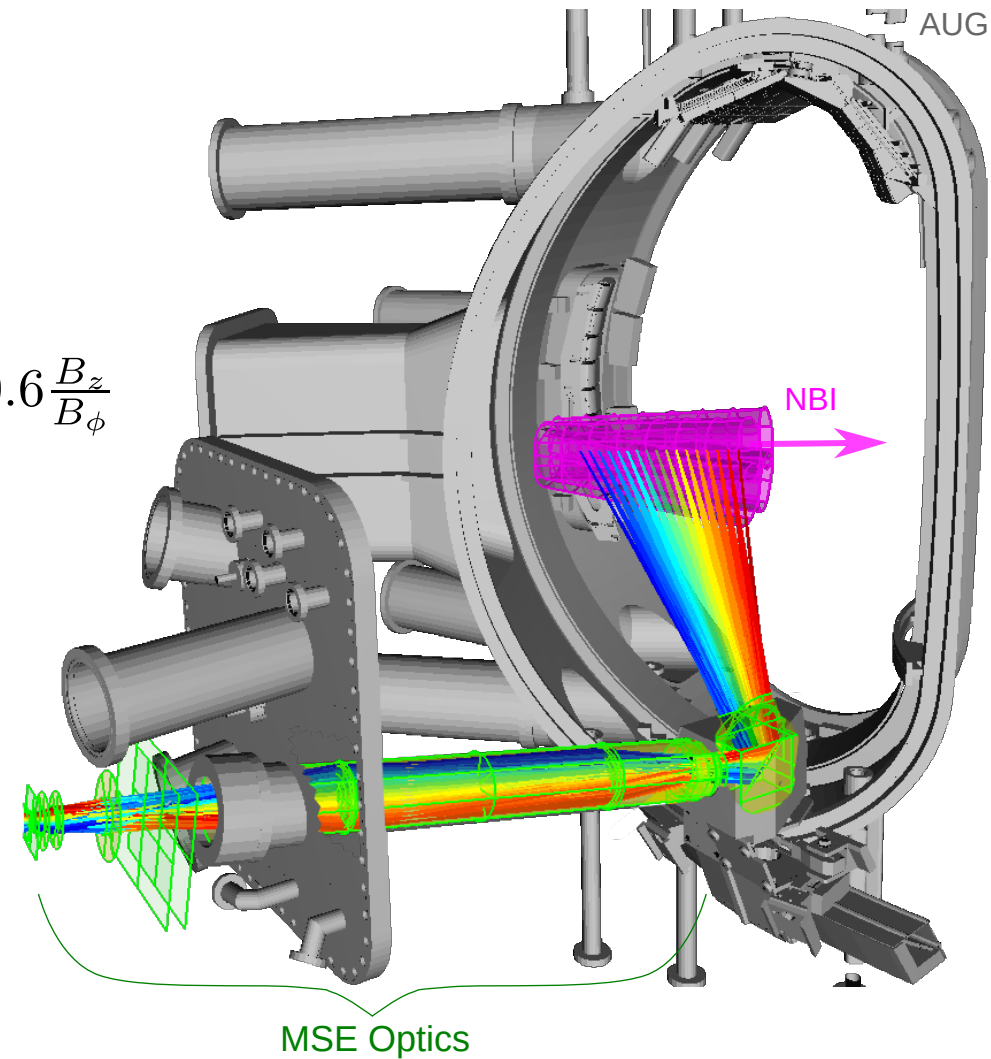
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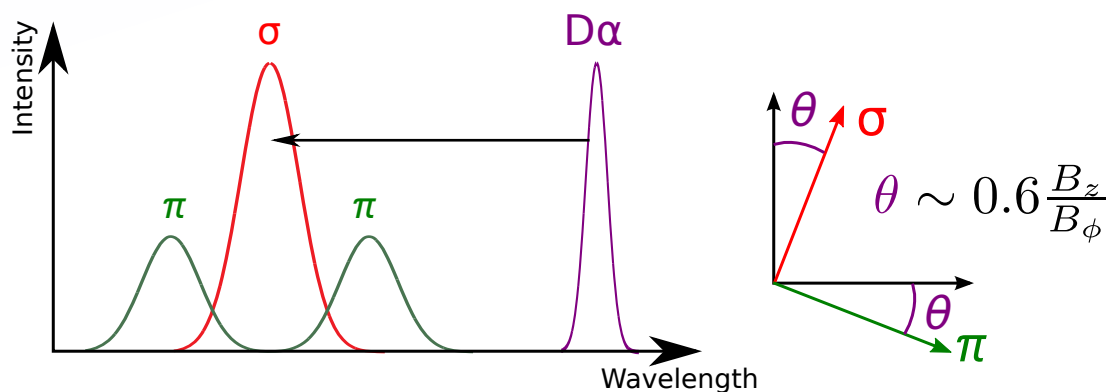
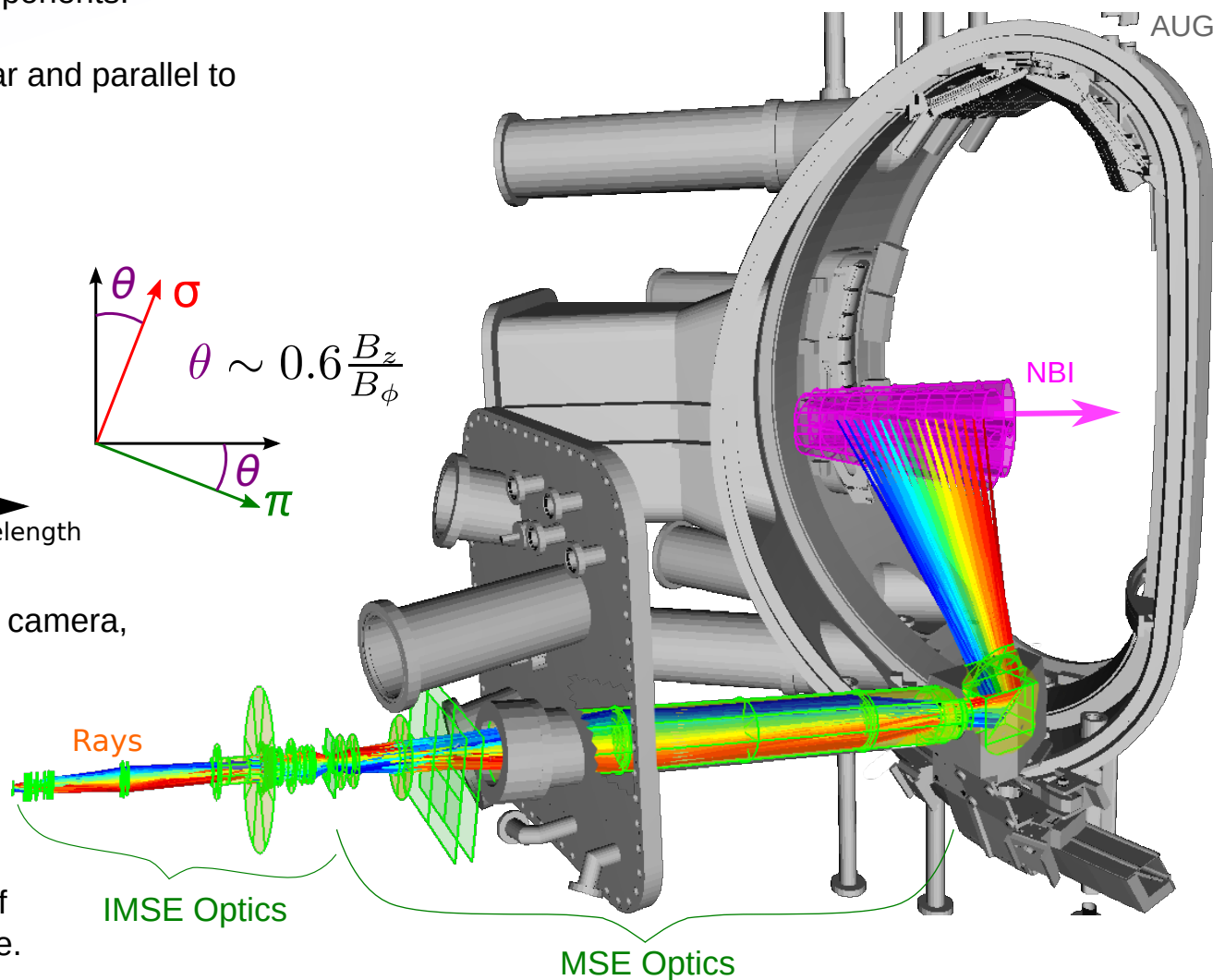


Image of the beam emission using a CCD camera,
> 60x60 θ measurements.

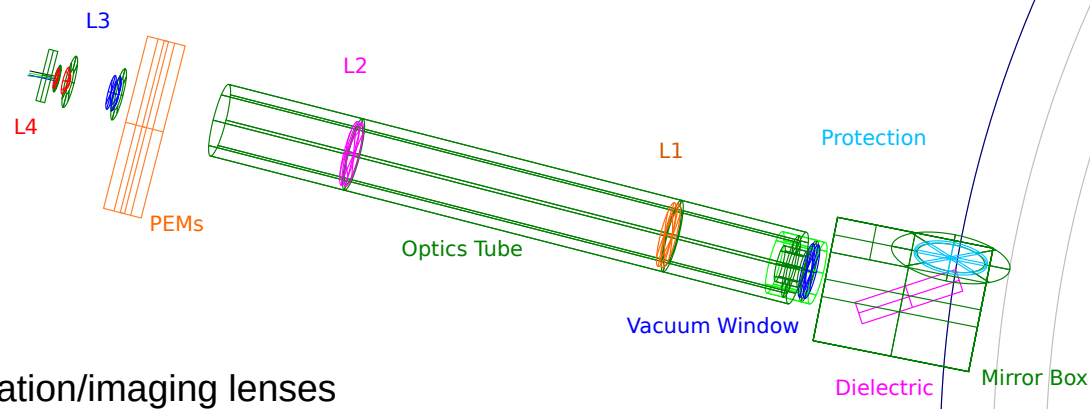


Replaced the MSE for two short periods of
plasma operation to test the basic principle.

Prototype IMSE Design

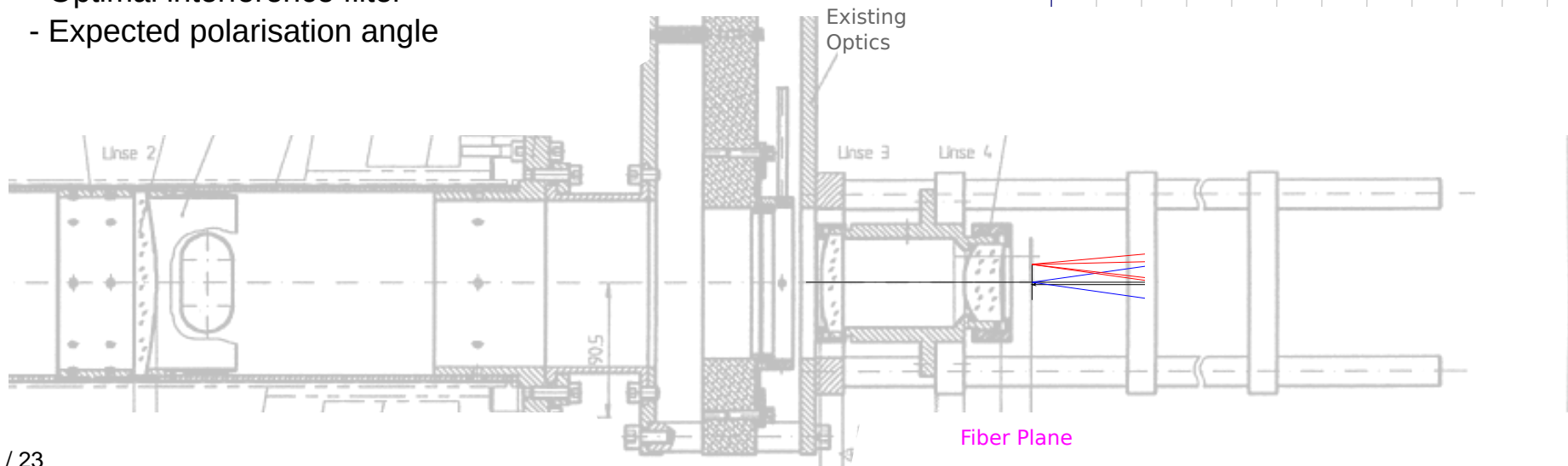
Prototype IMSE designed to match end of existing optics.

- Ray tracing of existing optics performed in 3D.
- New optical system matched to light delivered by existing optics.



Determination of:

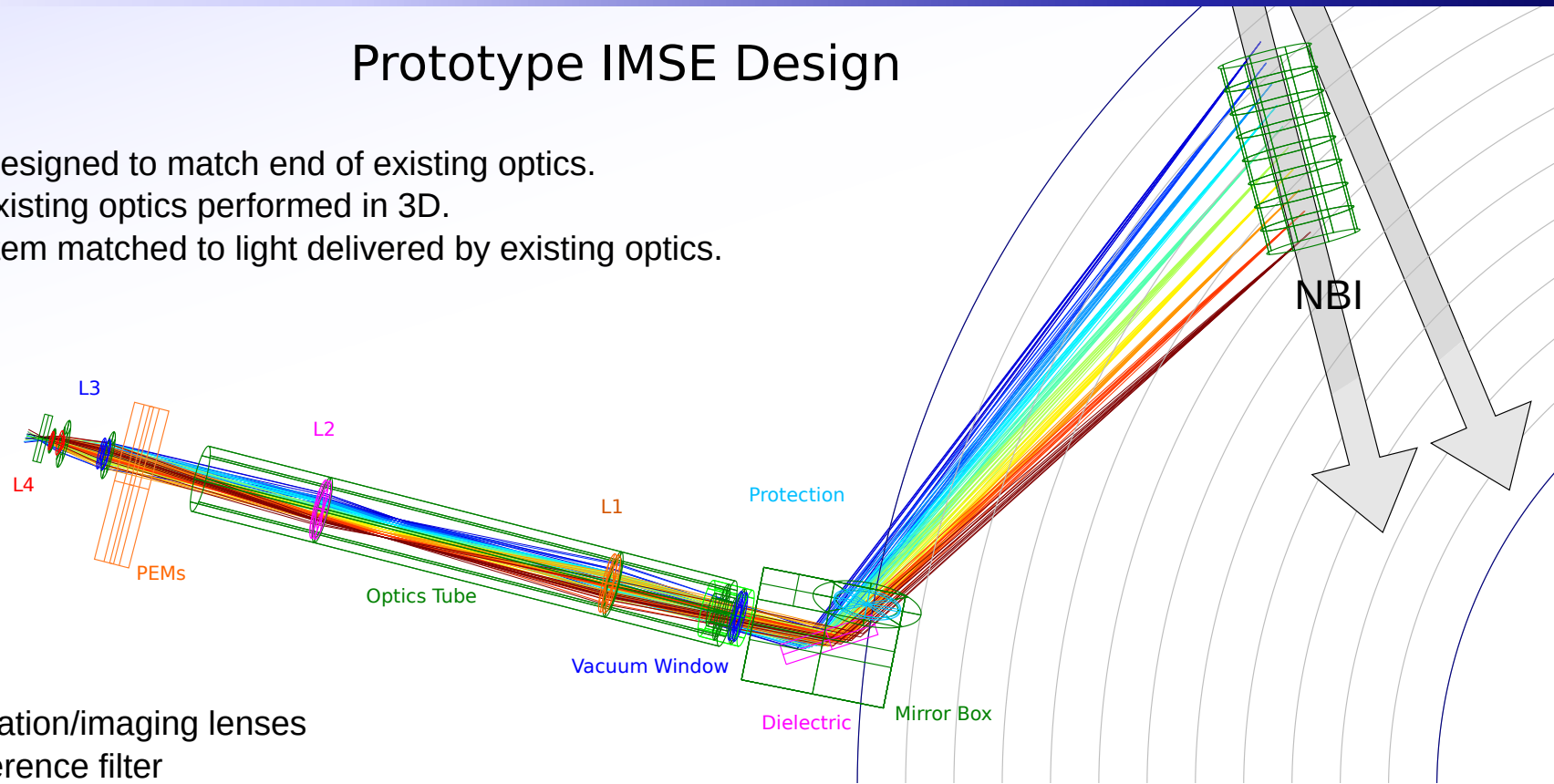
- Optimal collimation/imaging lenses
- Optimal interference filter
- Expected polarisation angle



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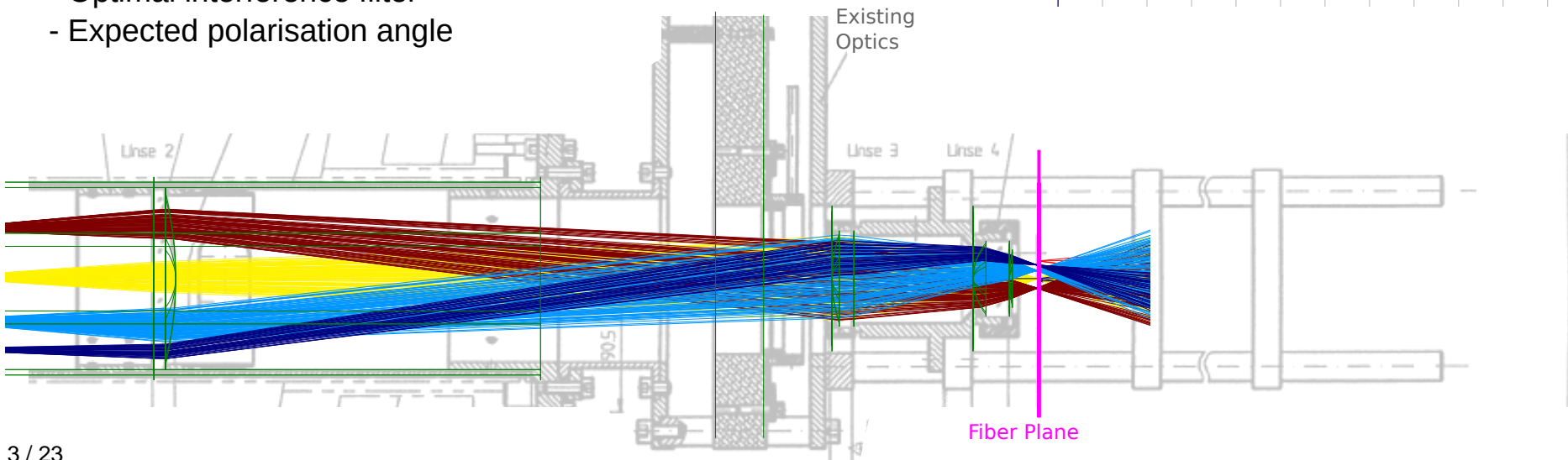
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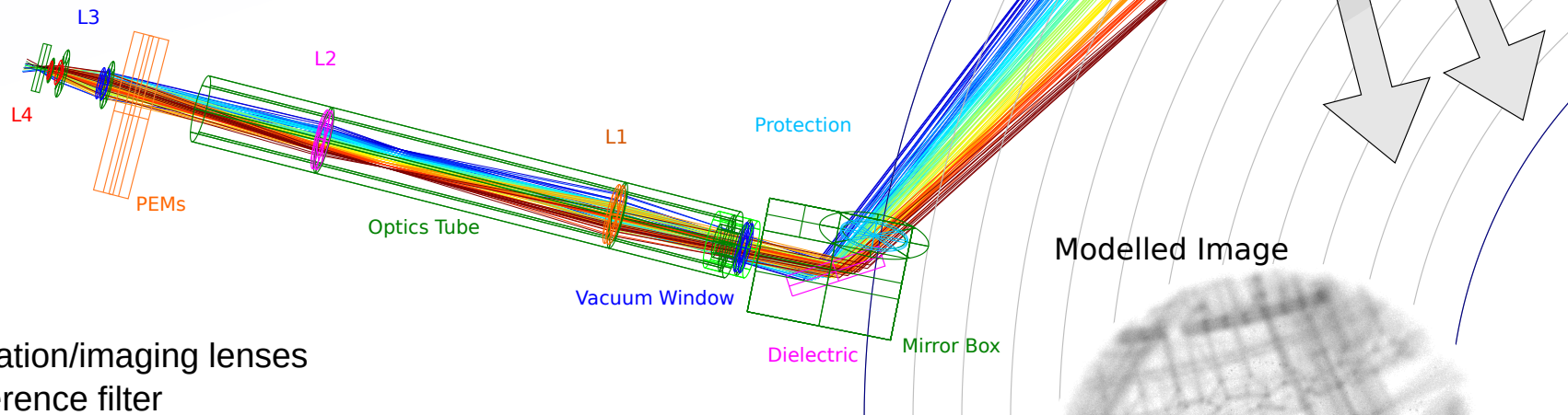
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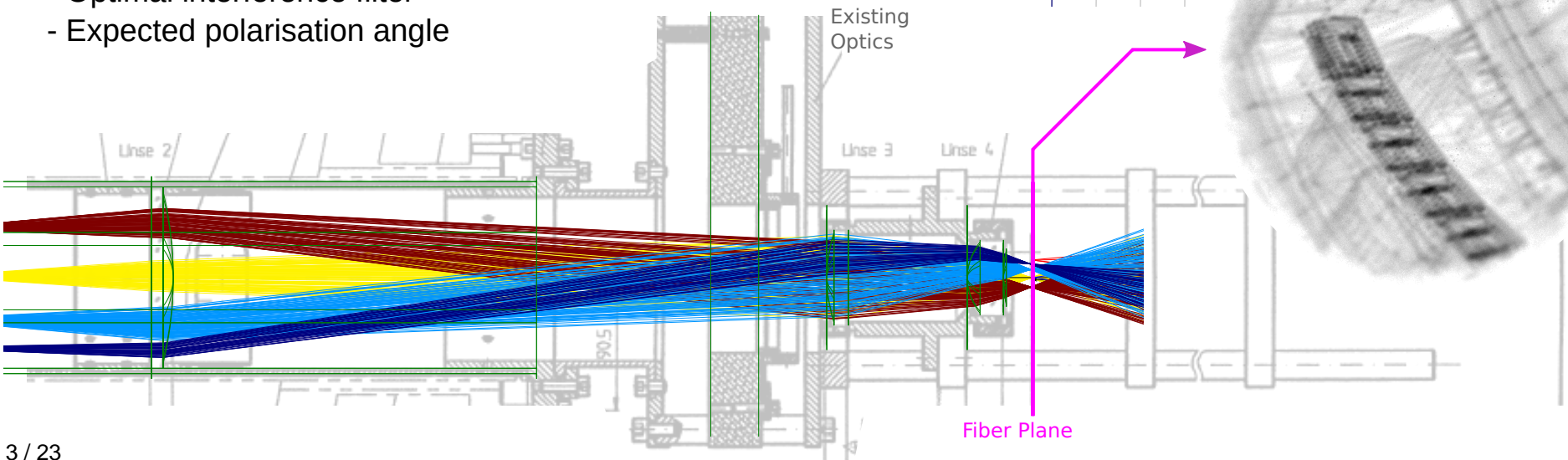
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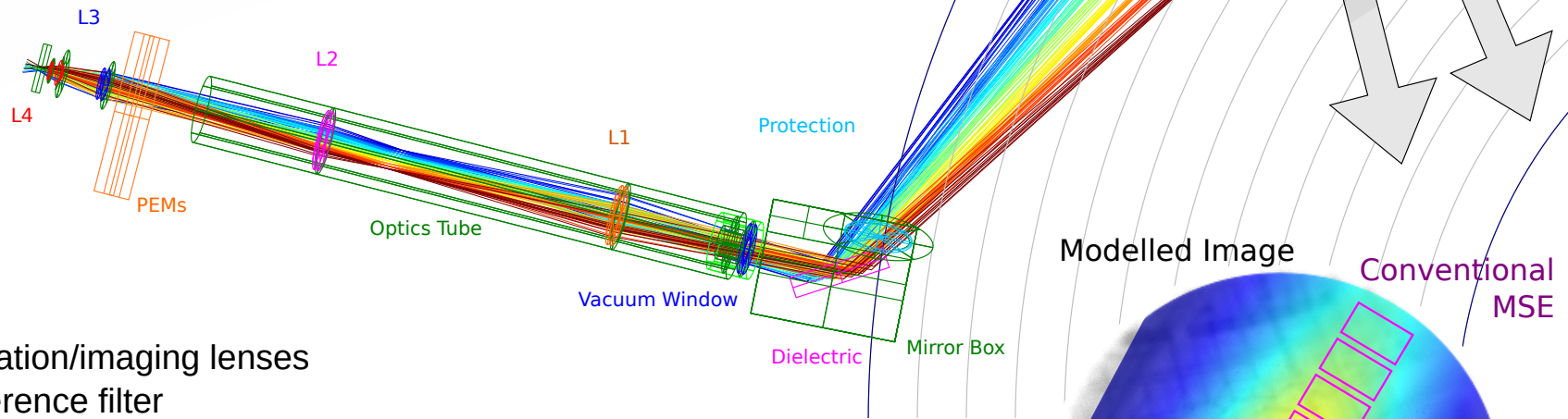
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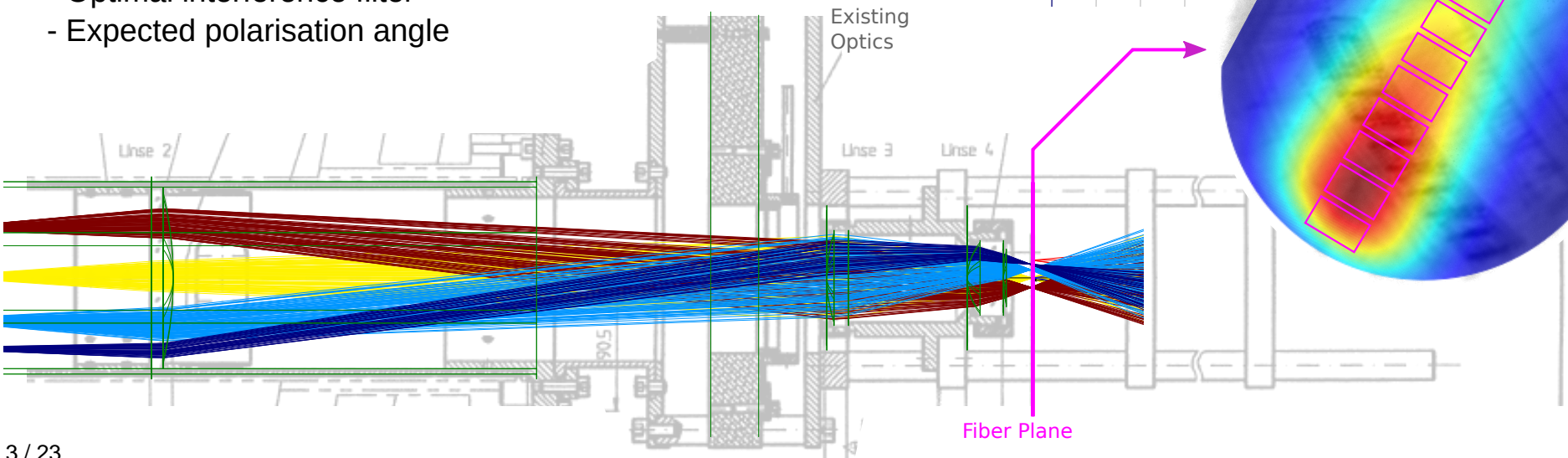
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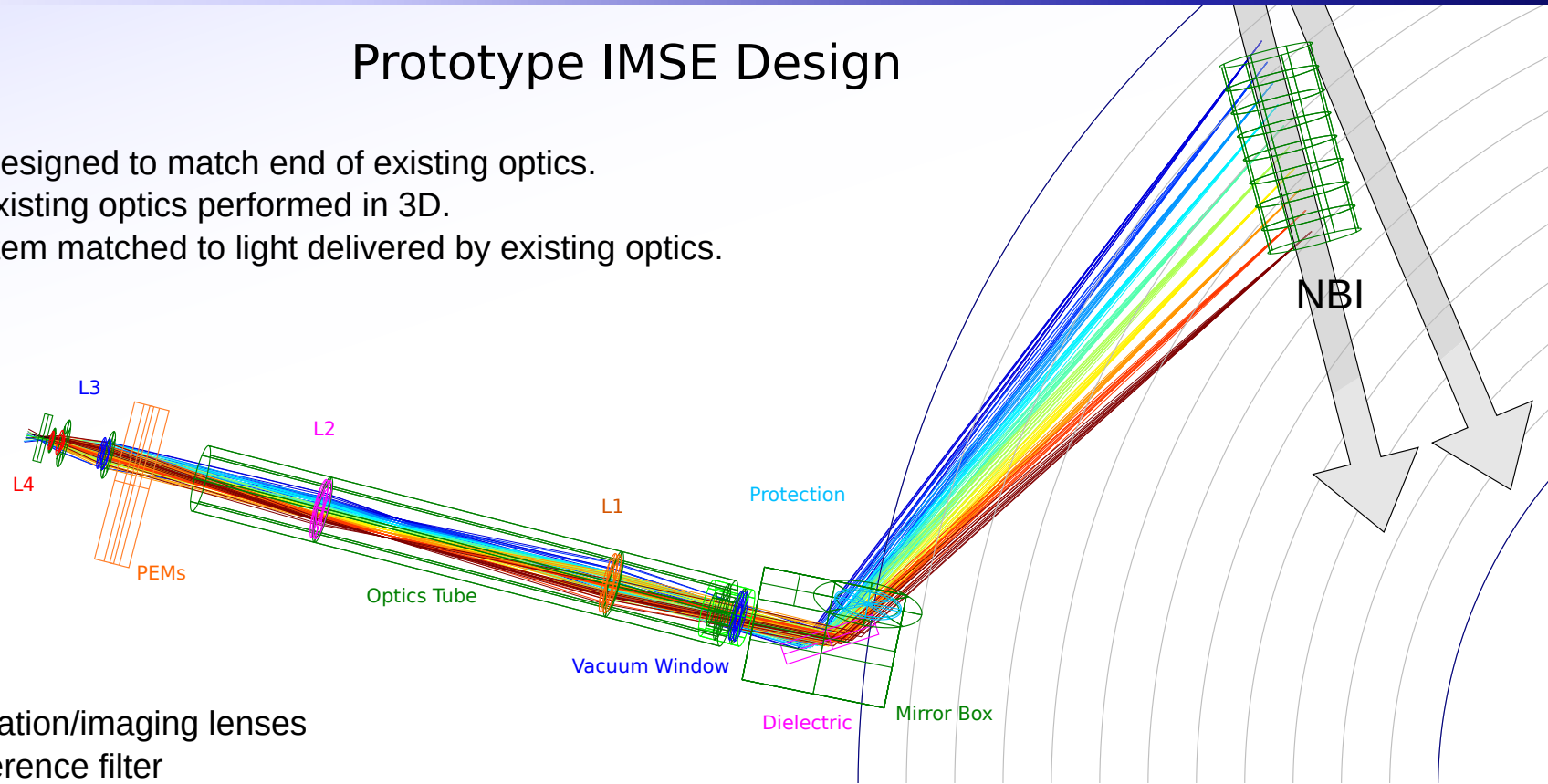
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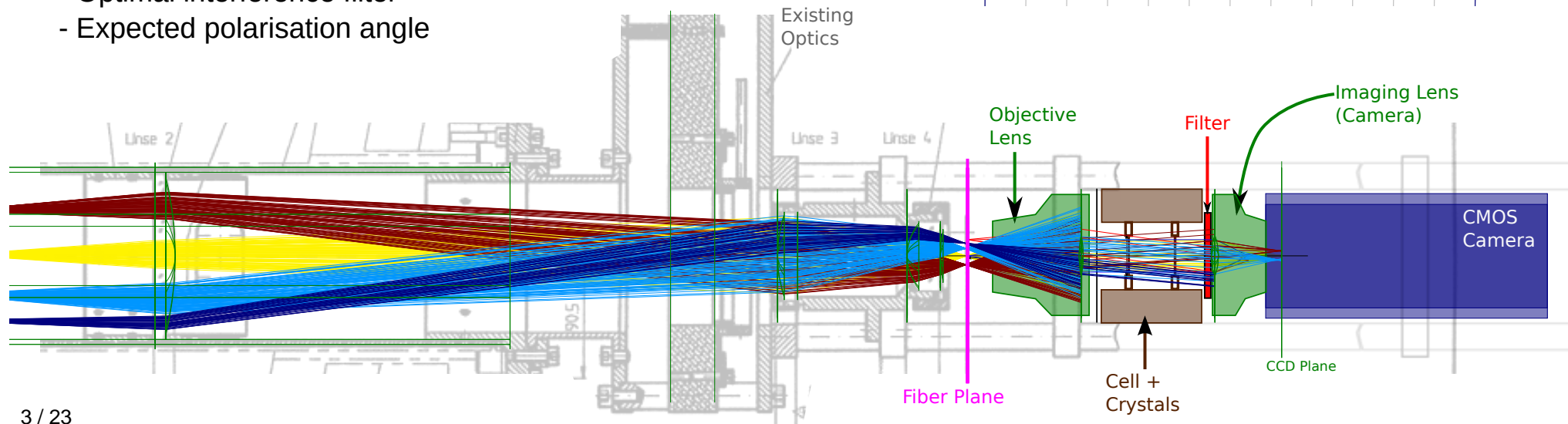
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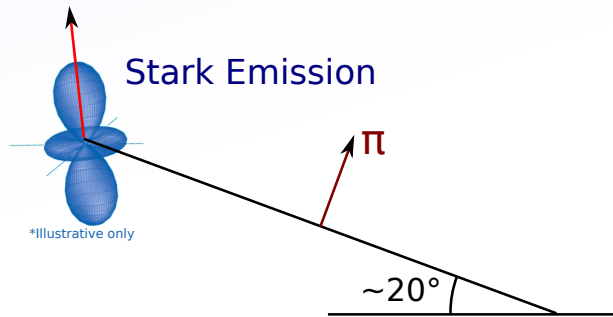
Ray-traced forward model

To fully understand effects of optics, everything put into ray-tracing model:

1) Field of view effects:

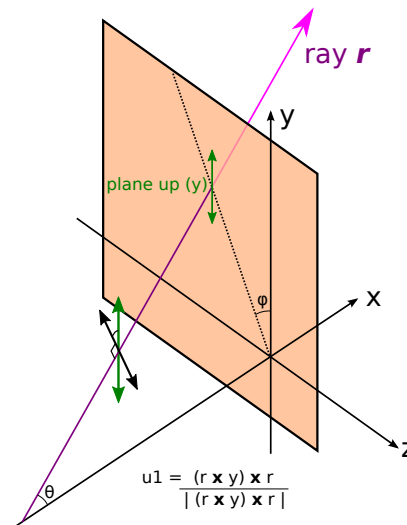
- Subtlety of how polarisation is created, defined and measured.

$$E = V \times B$$



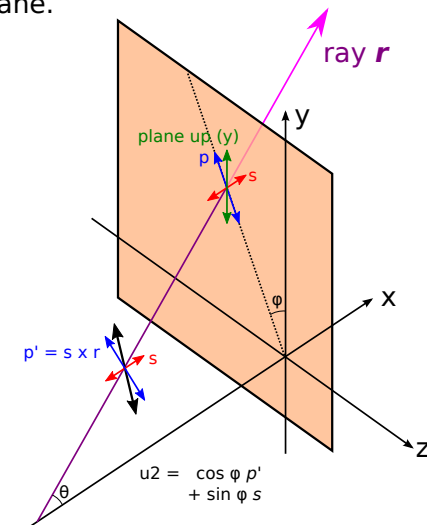
POLAR consistent

$u1 =$ Nearest vector to 'up' \neq



PLANAR consistent

$u2 =$ Same p/s ratio as 'up' has in the plane.



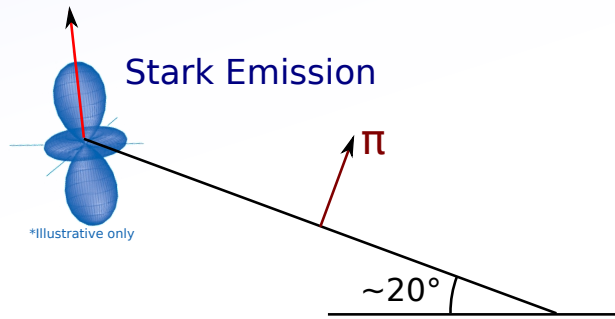
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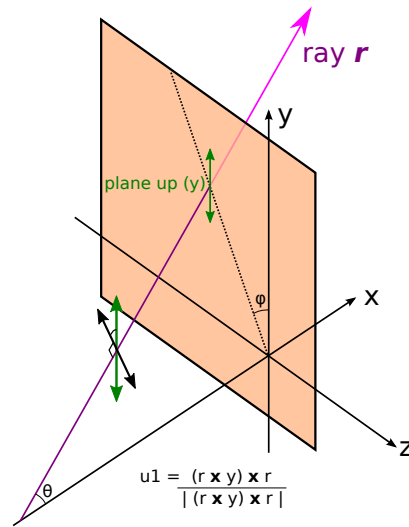
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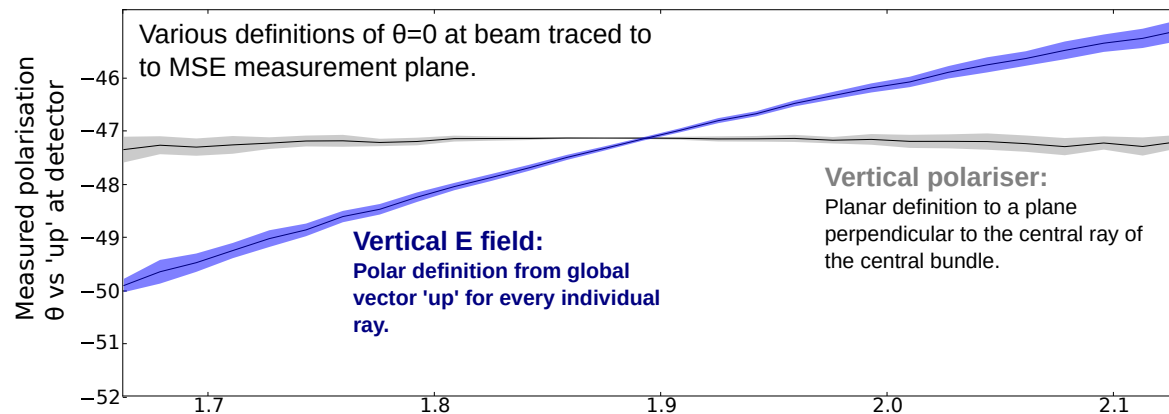
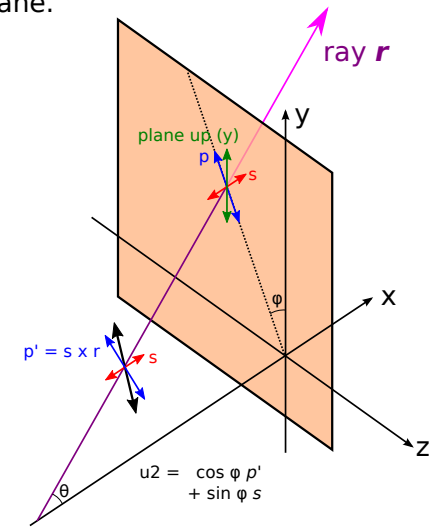
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Polarisation effects

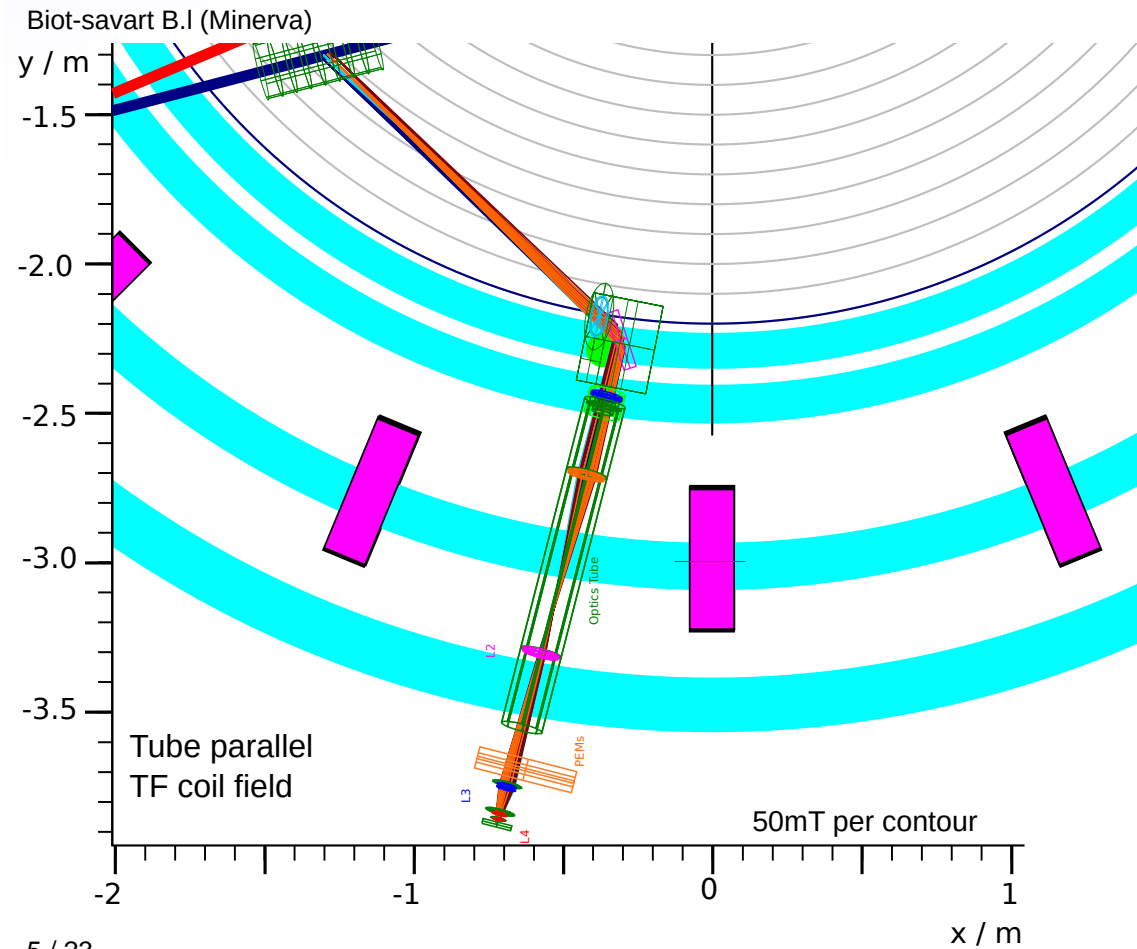
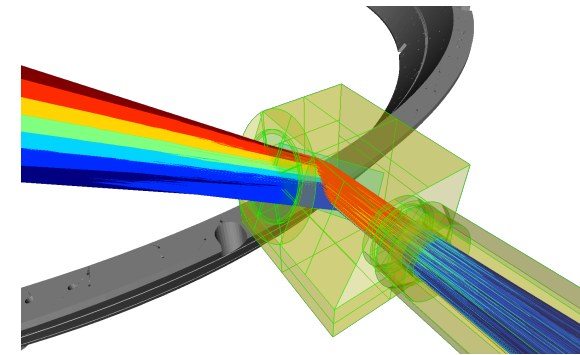
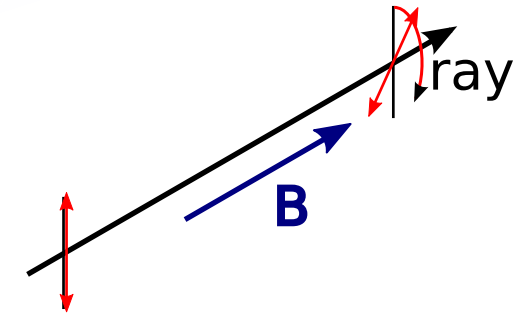
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2) Faraday rotation

- Fields due to both:

- TF coils: Strong, but static

- PF coils. Weak, but time-varying.



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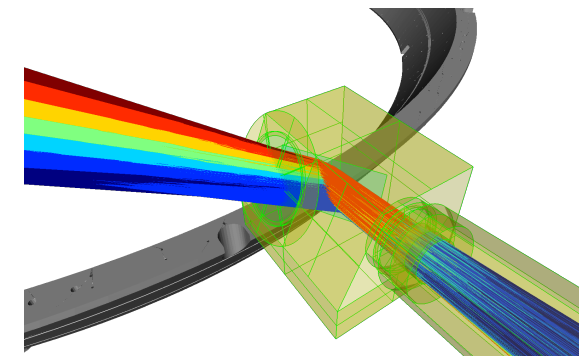
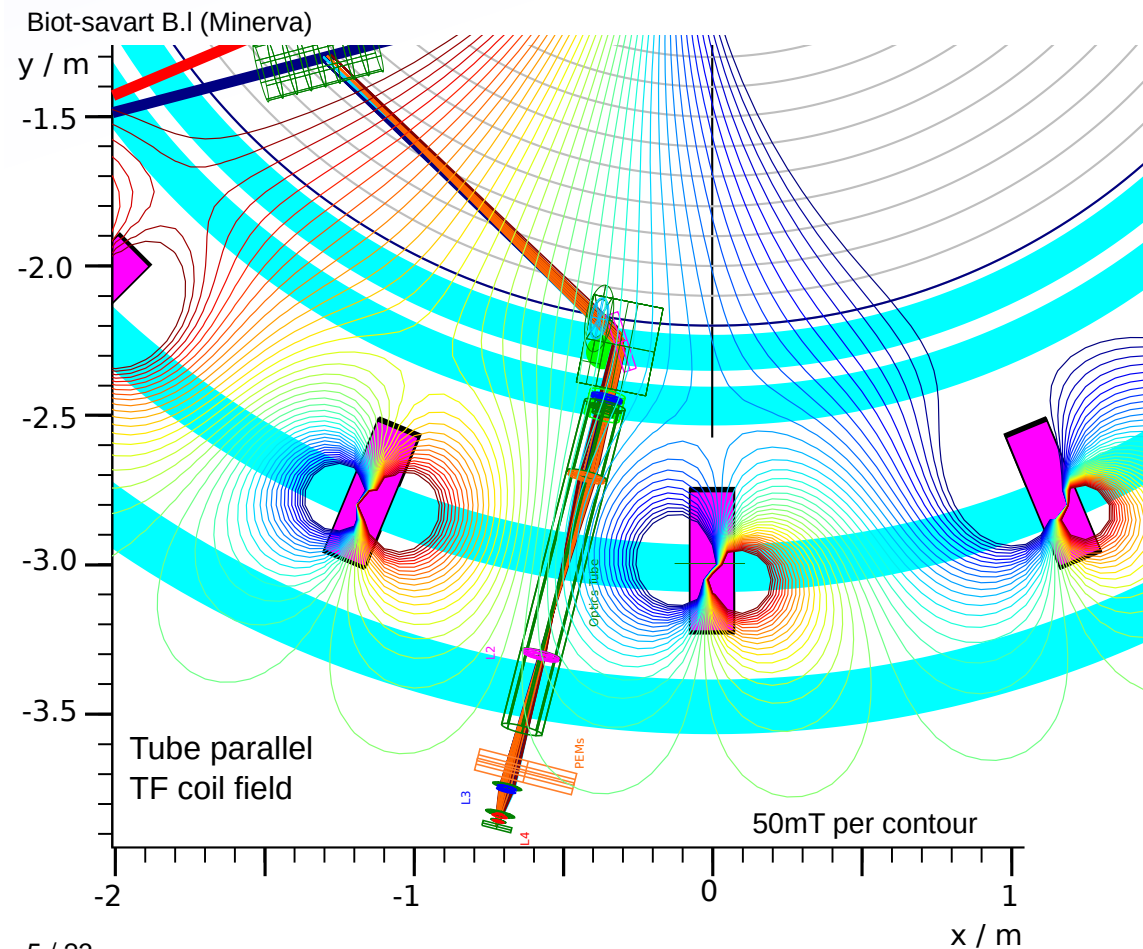
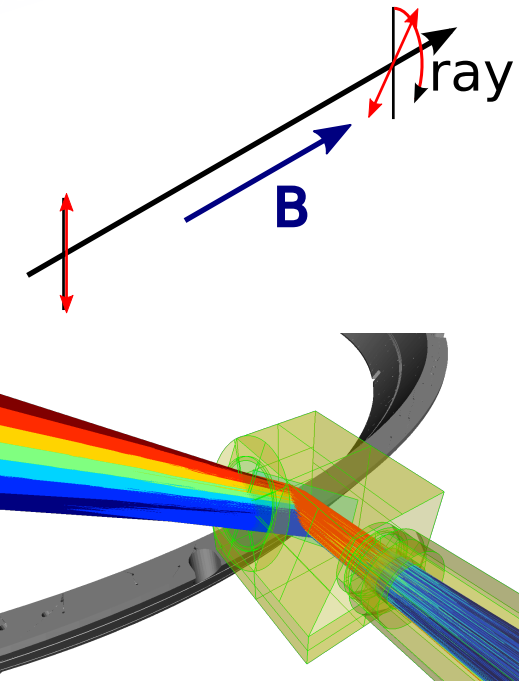
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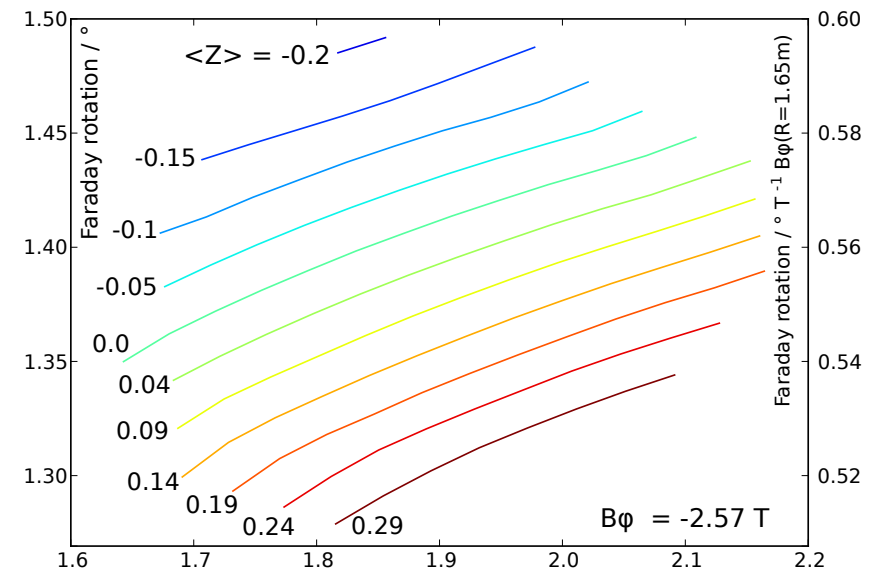
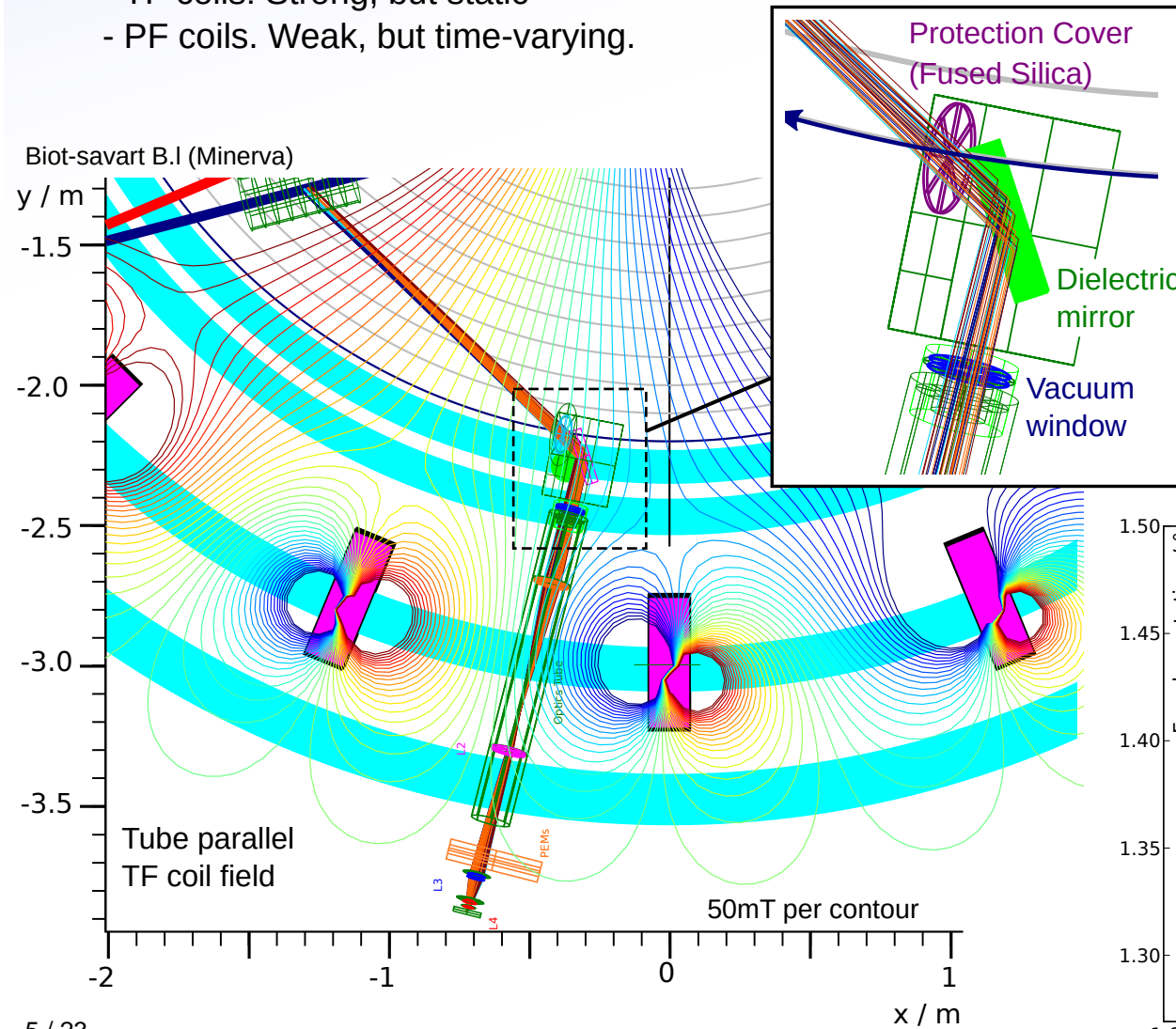
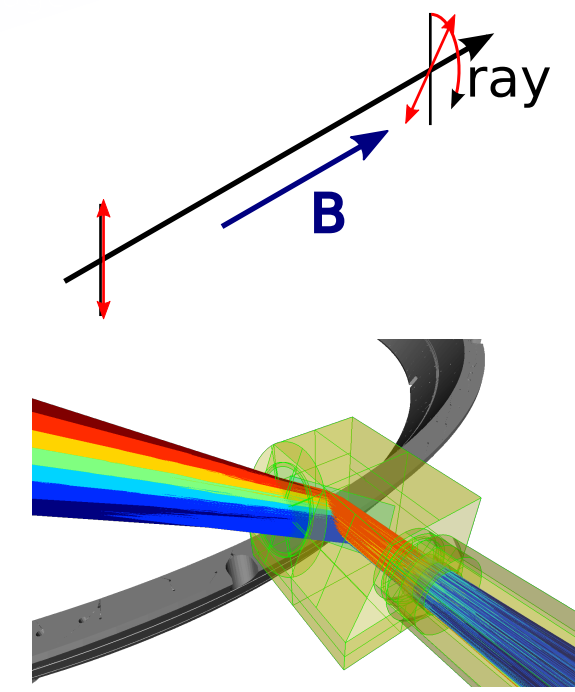
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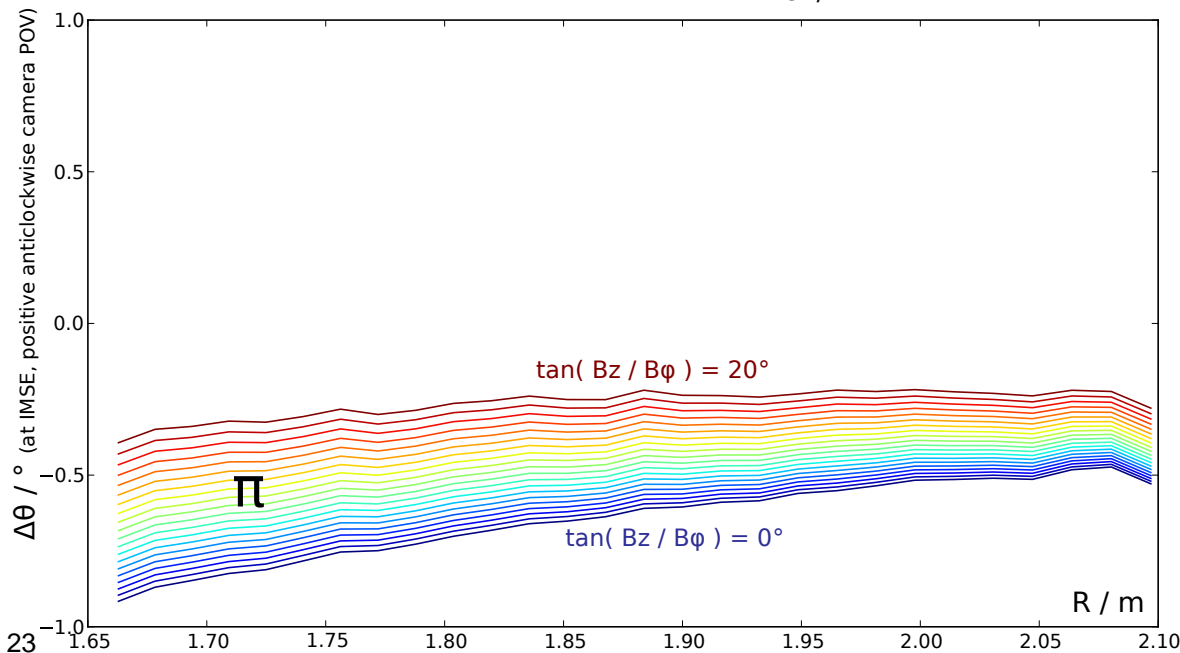
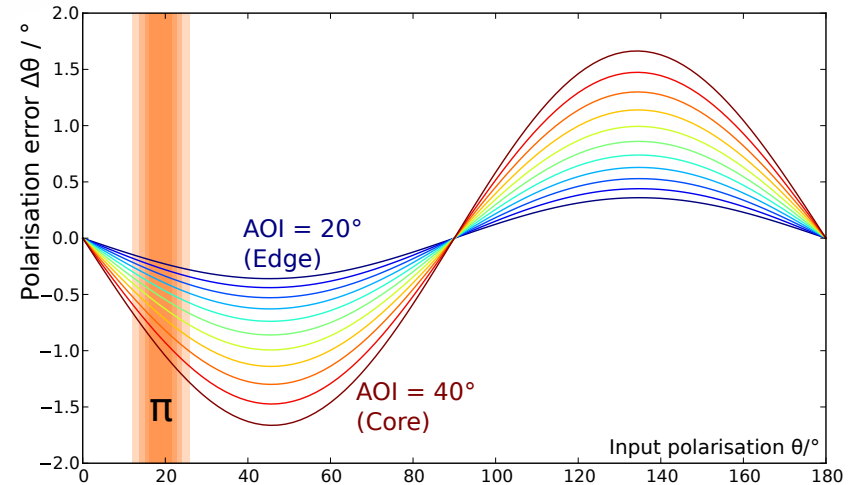
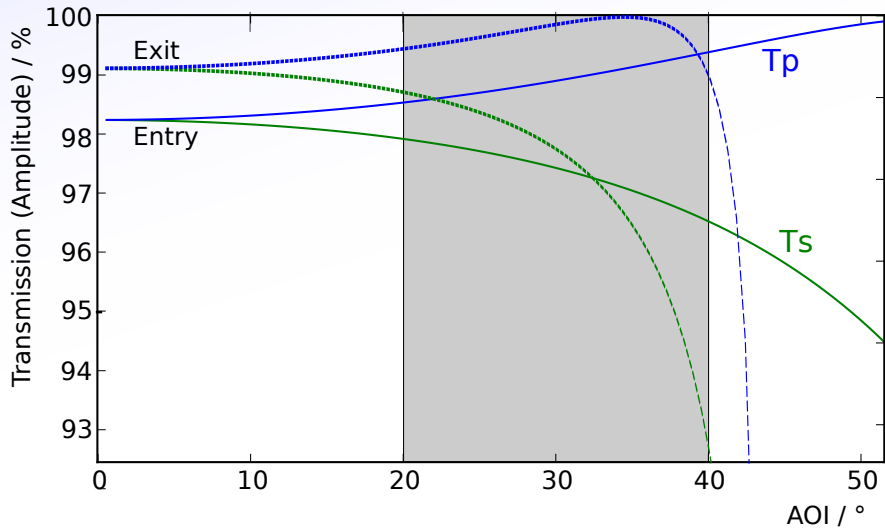
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Polarisation effects

3) Fresnel coefficient effects (e.g. uncoated protection cover)

- Variation of transmission/reflectance with AOI --> Non-linear rotation of polarisation

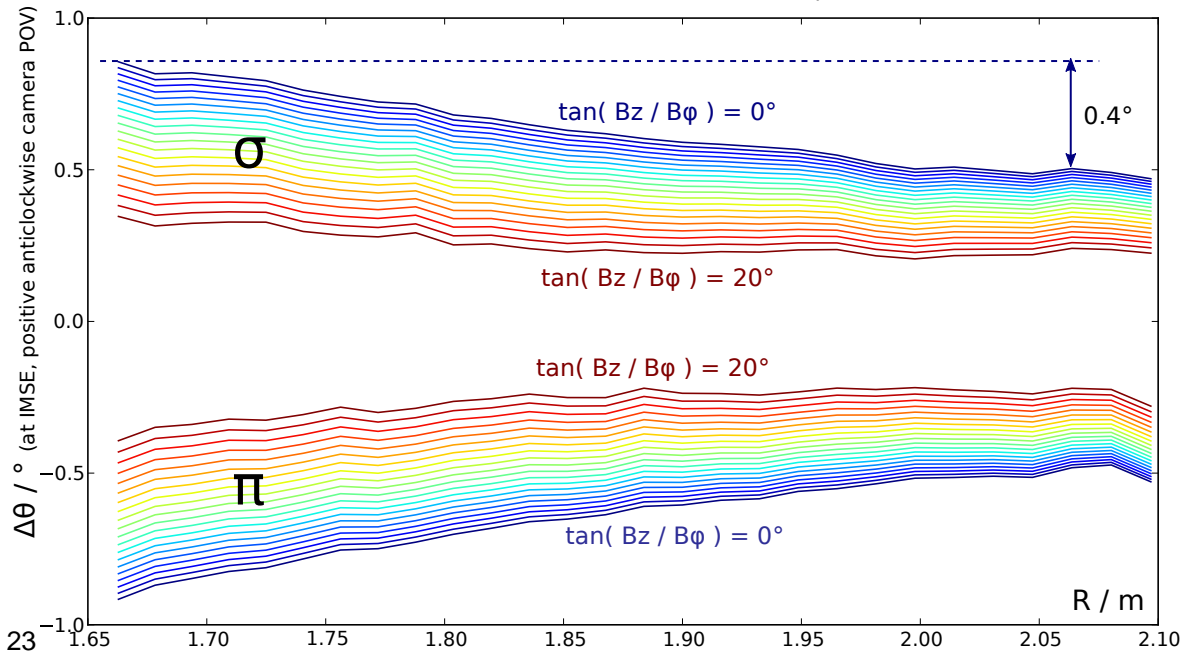
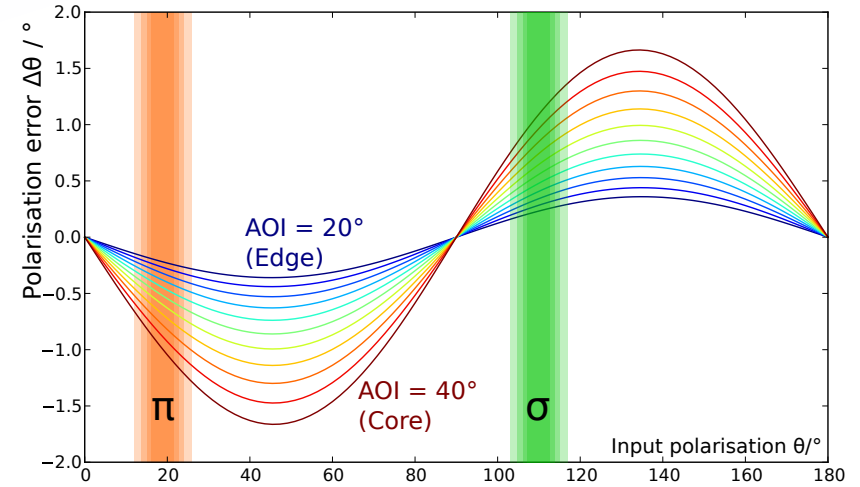
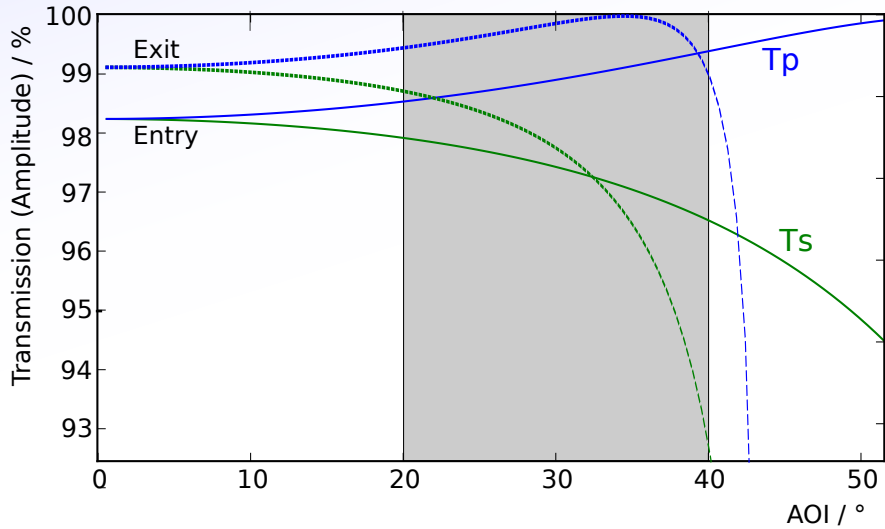


Mostly cancels for $\sigma+\pi$ (IMSE), but is important for MSE

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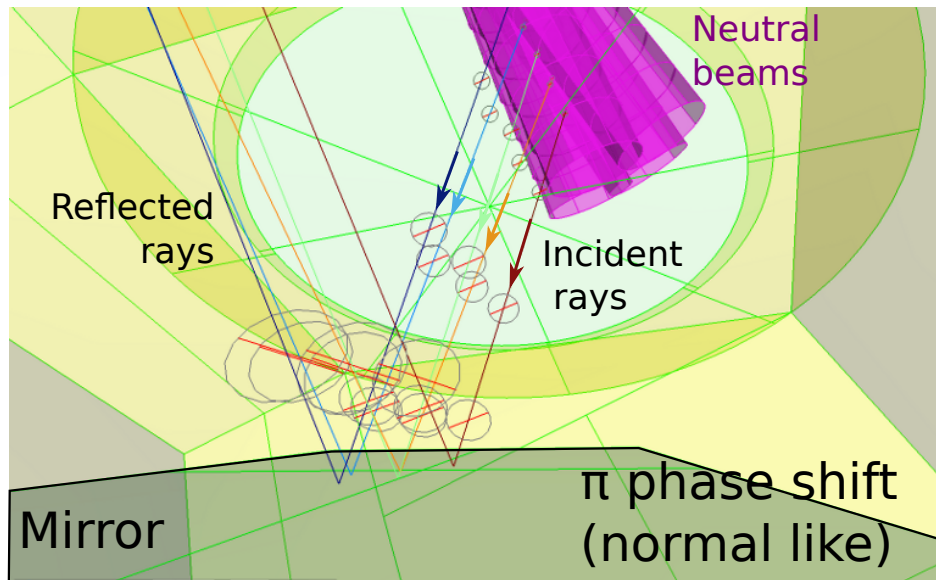
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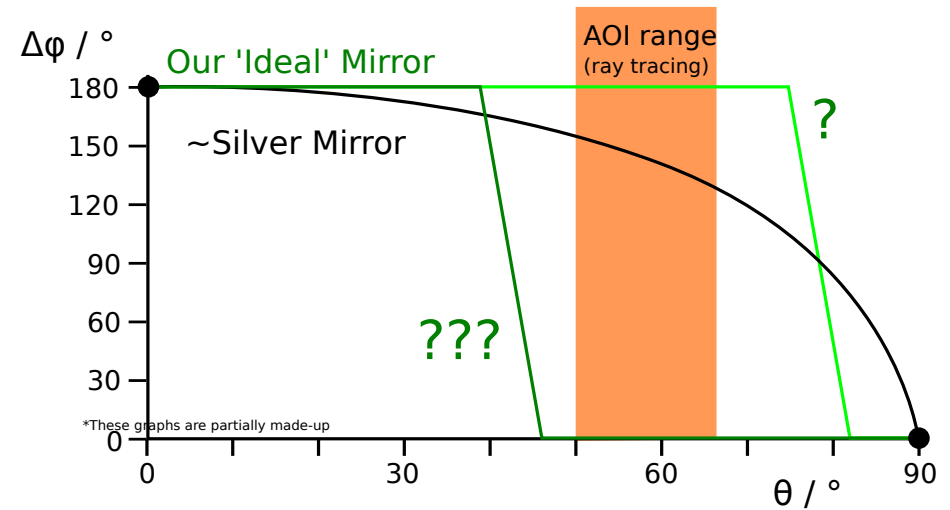
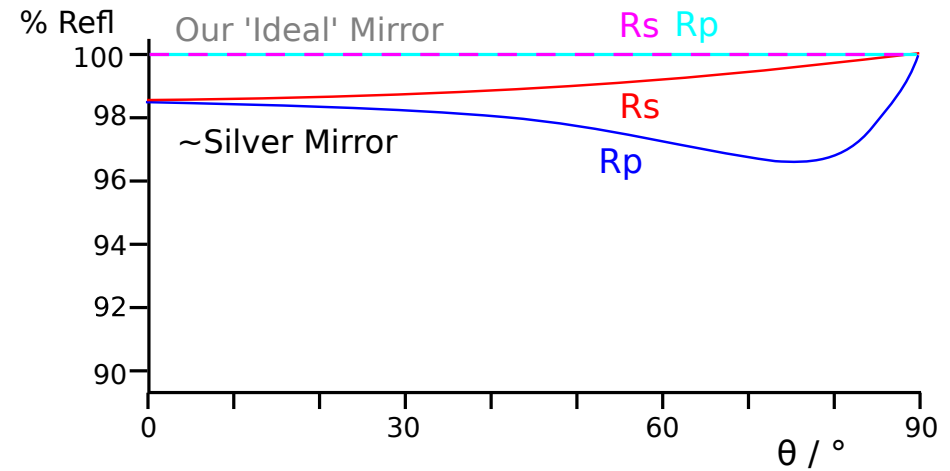
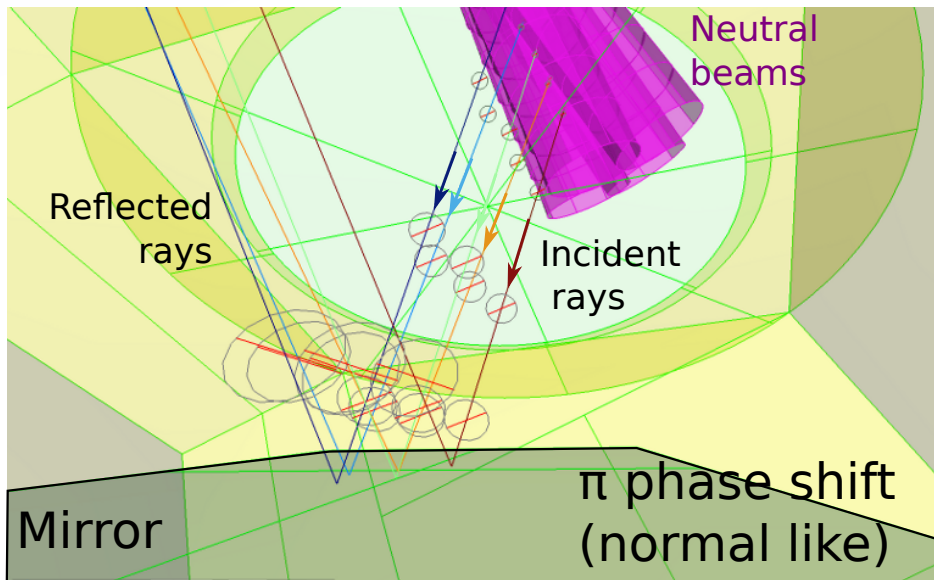
4) Mirrors



Polarisation effects

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- Simple 'ideal π phase shift' for dielectric mirror.
- Later with measured spectro-polarisation transfer properties of mirror.

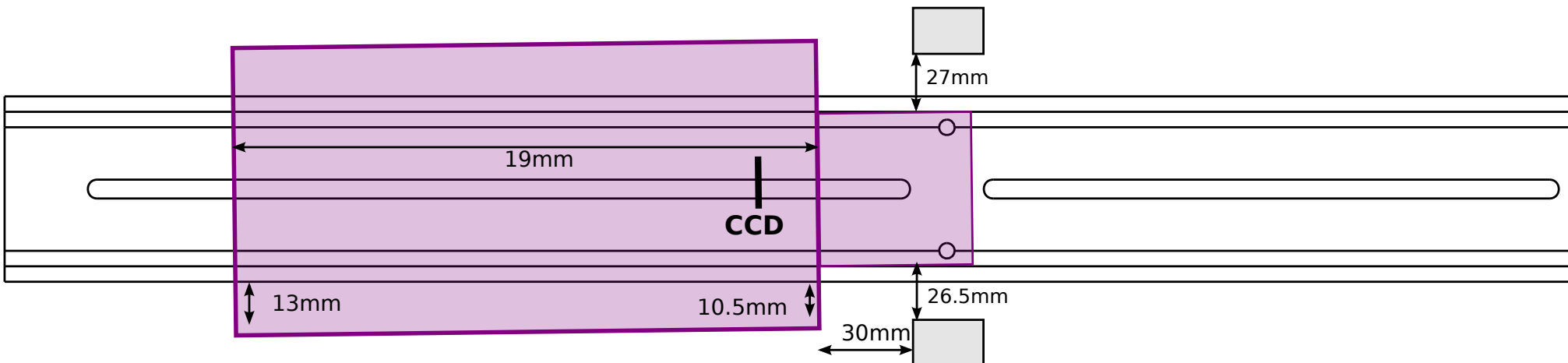
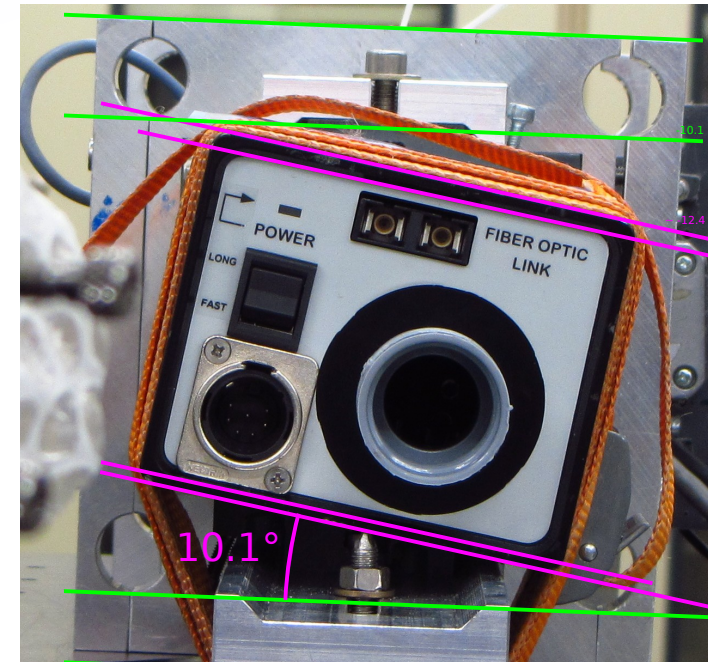


*These graphs are partially made-up

Polarisation effects

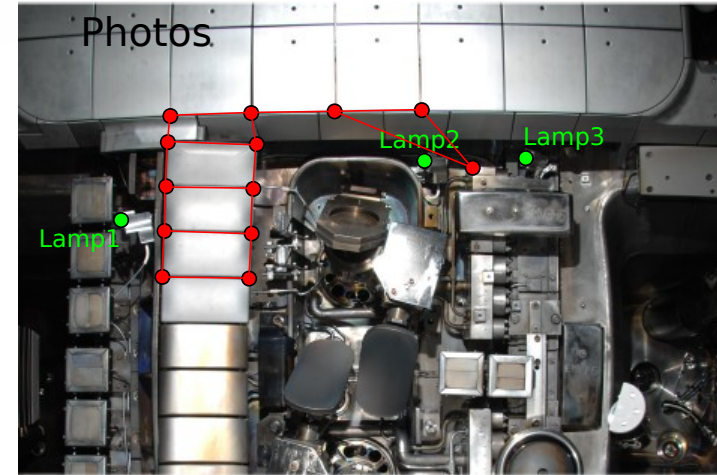
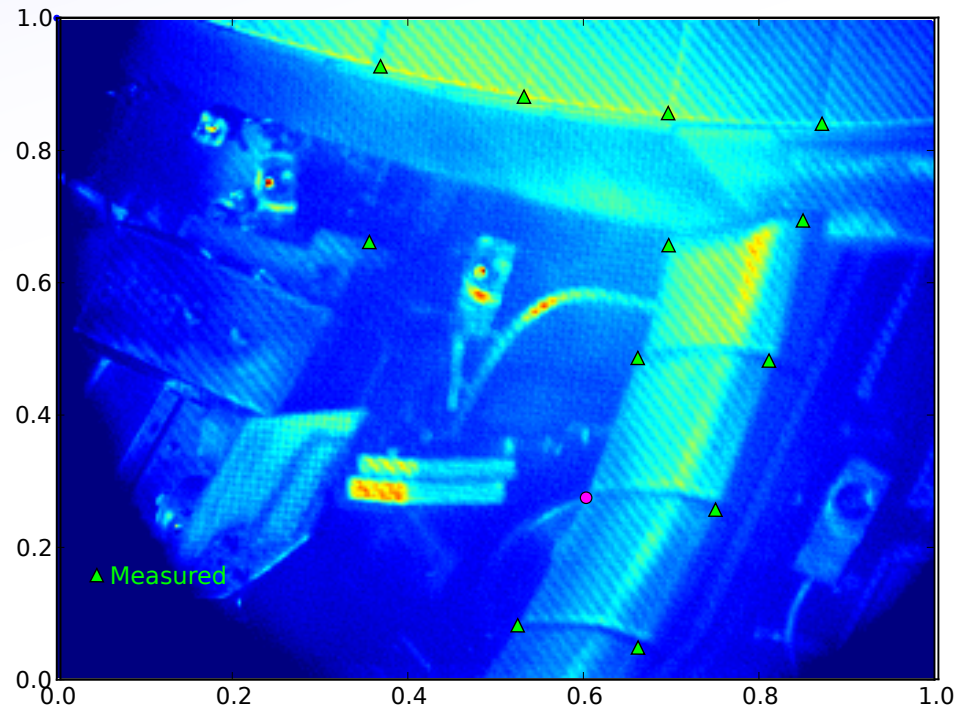
5) Mechanical angles/positions

- Angle/position of camera - Measured with uncertainties
- Small inaccuracies in lens/mirror positions - fitted...



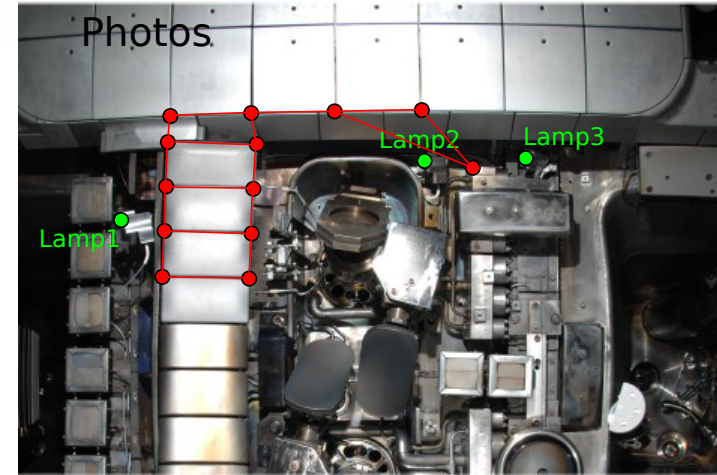
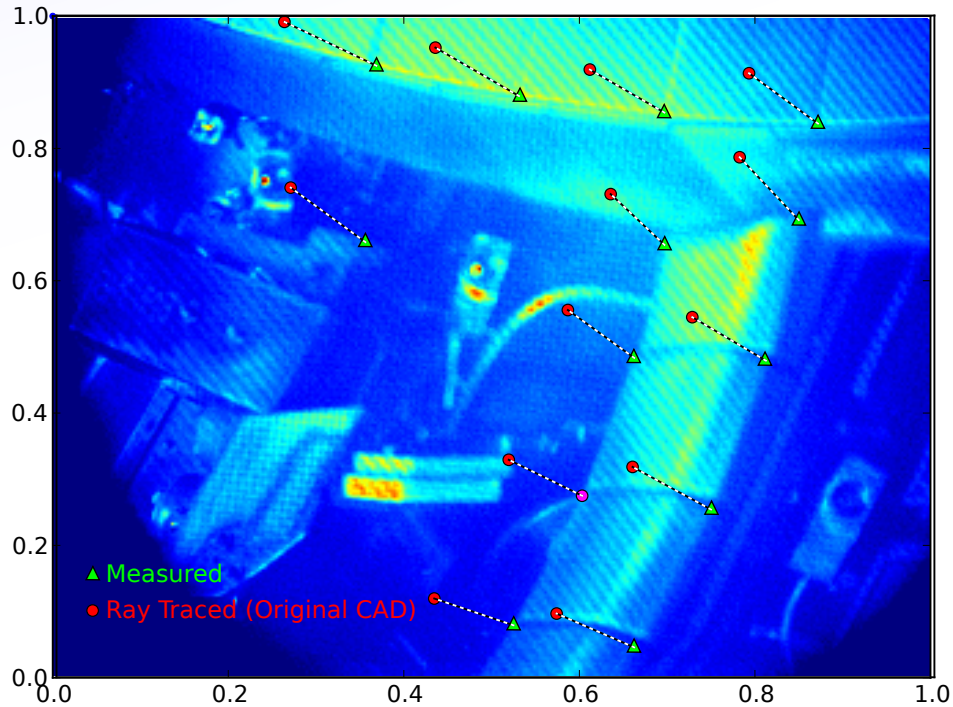
Ray-tracing match

- Fit mechanical model parameters to match ray-traced CAD 3D points.
- Match vignetting curves from different stages in system
--> Determines most mechanical parameters.



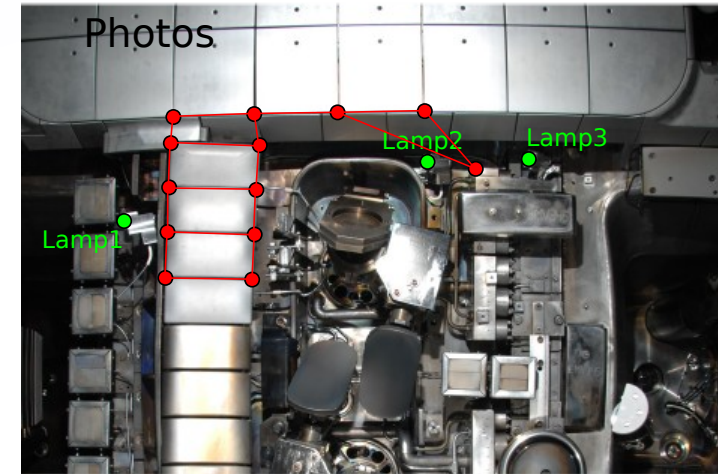
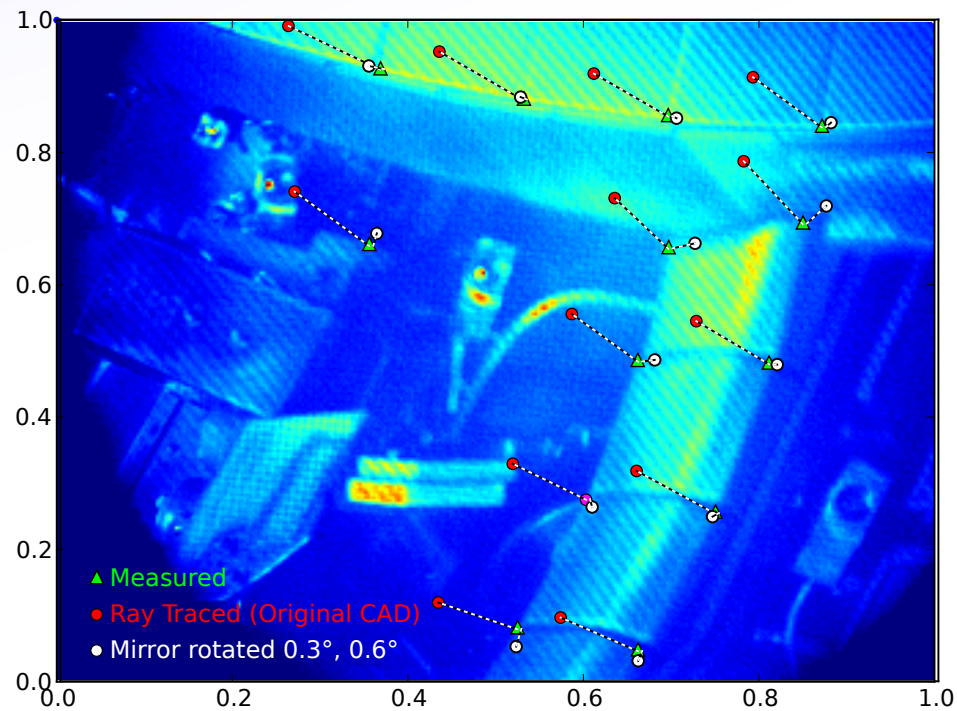
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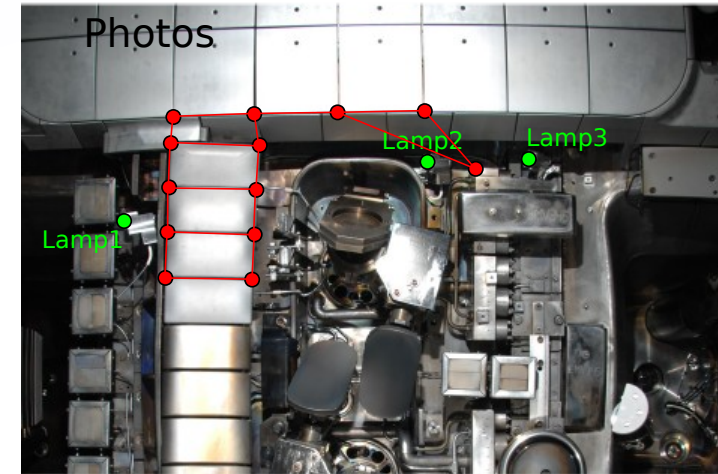
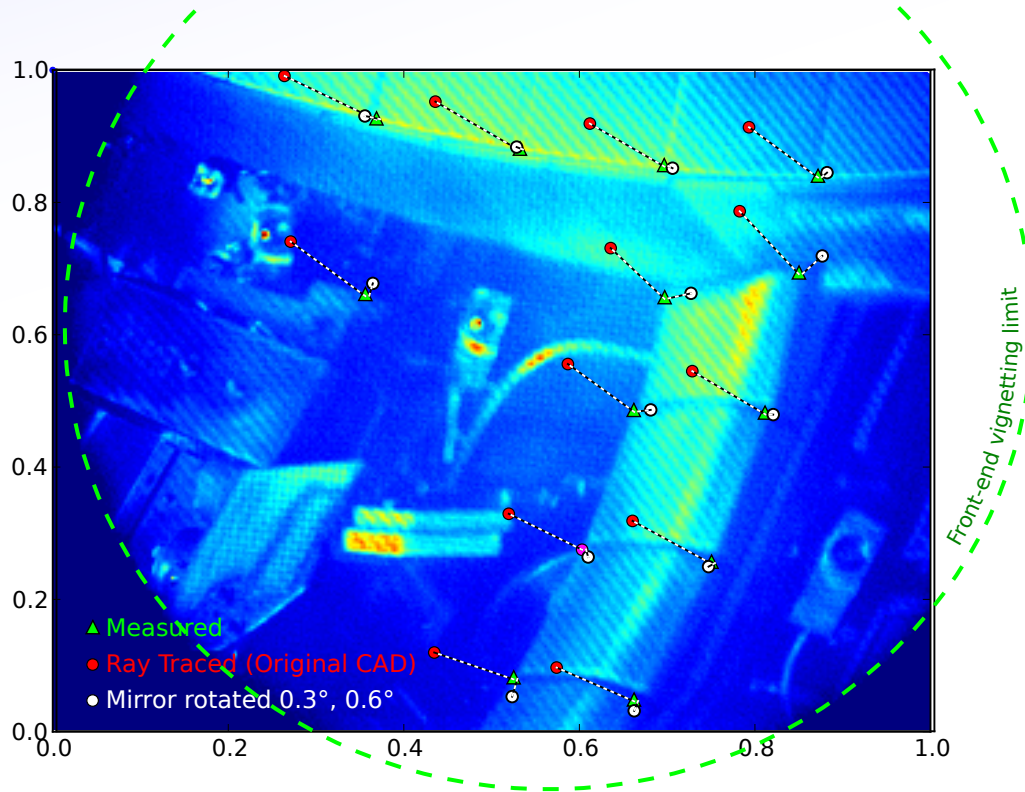
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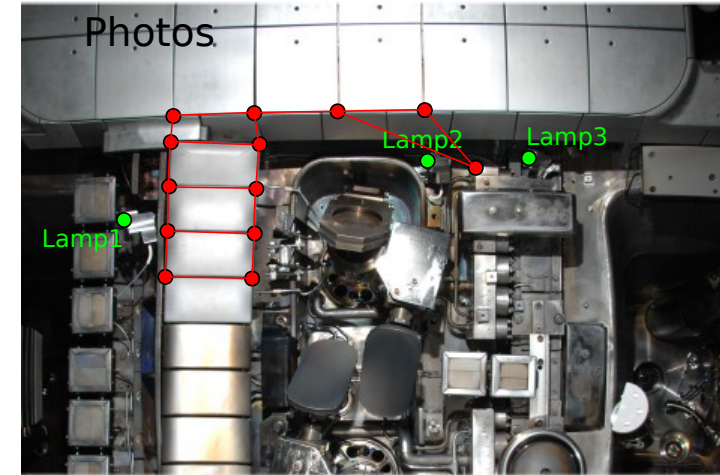
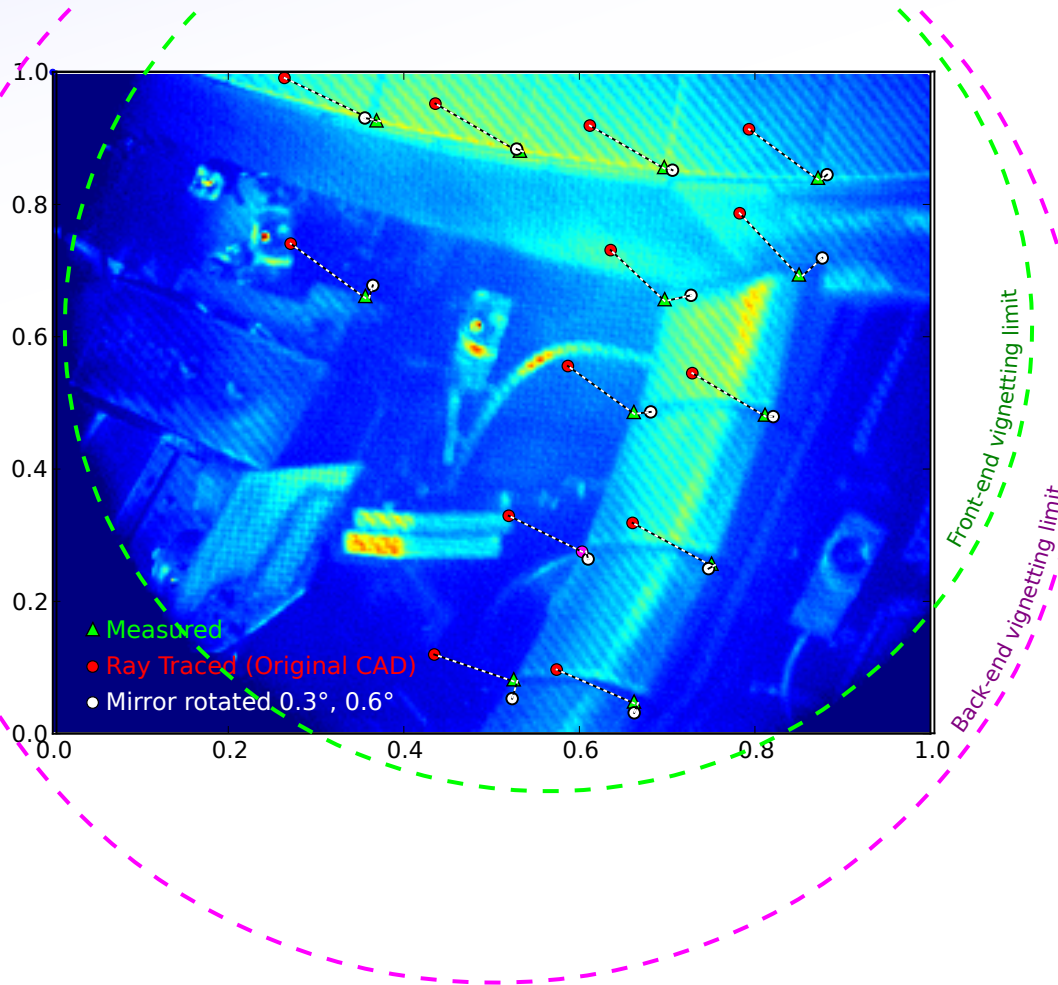
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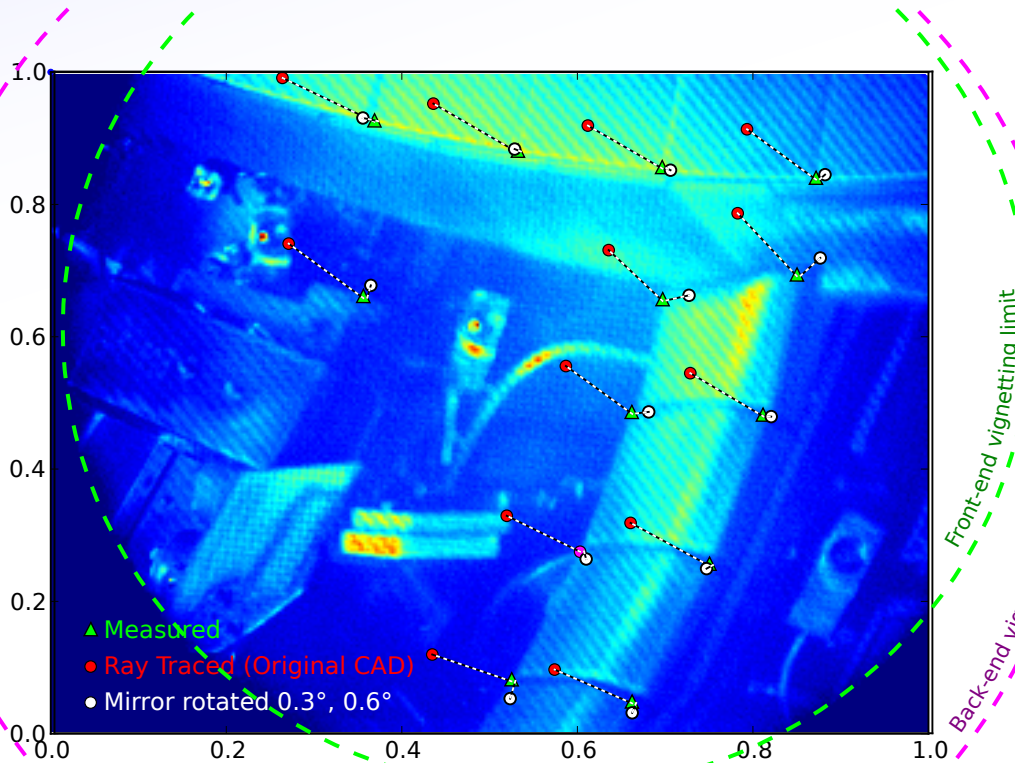
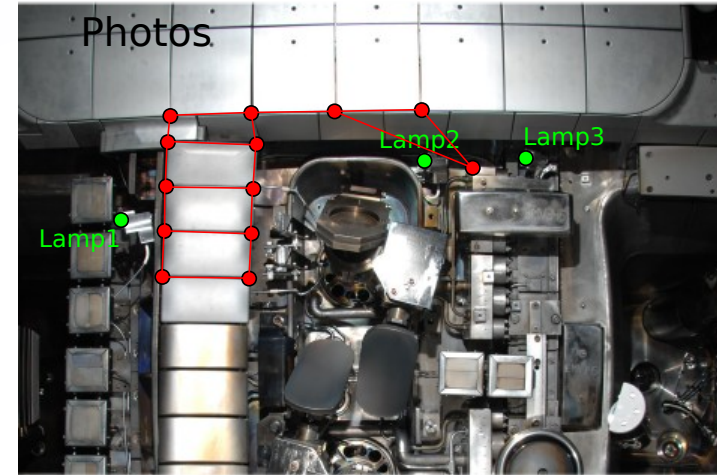
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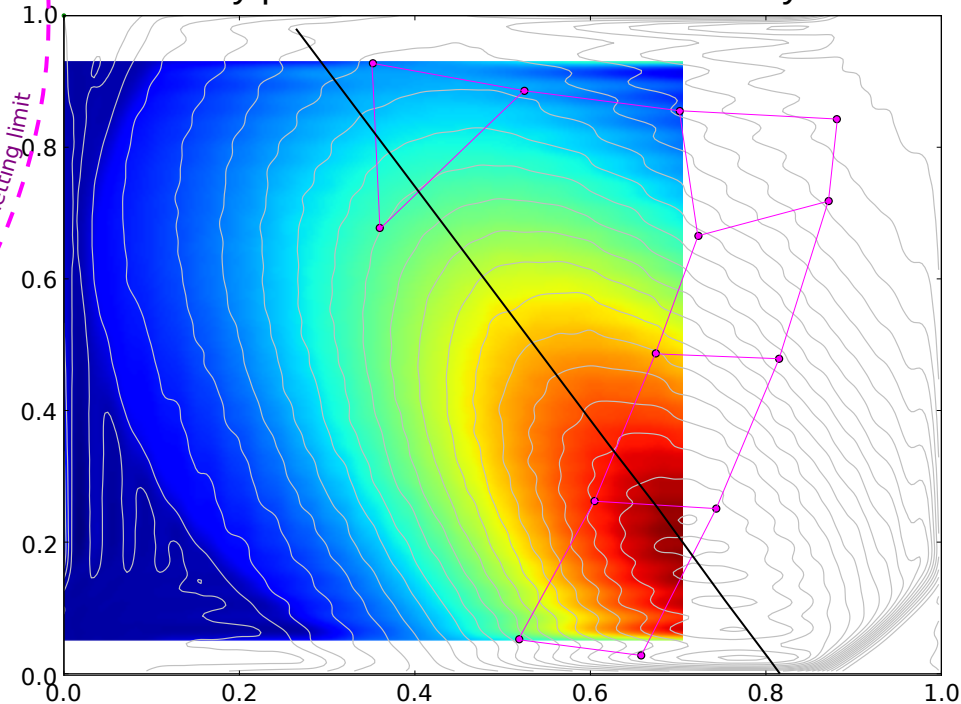


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Correctly predicts beam emission intensity axis:





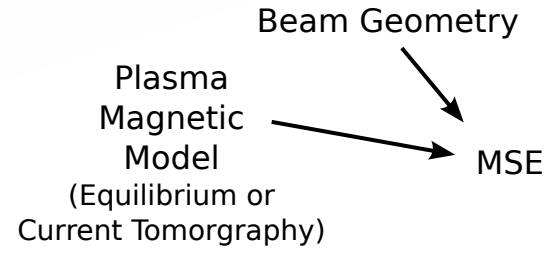
Model agreement

- Final prediction entirely without calibration



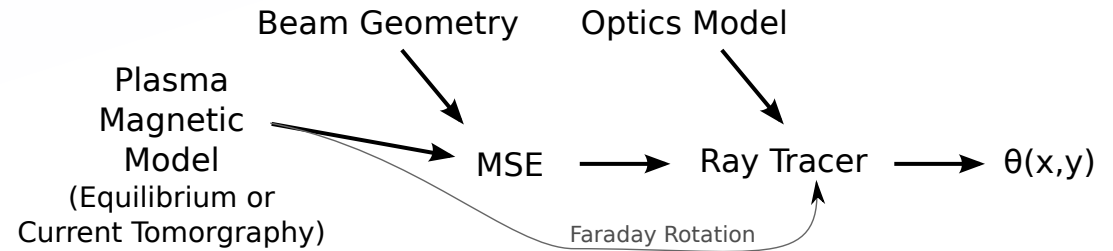
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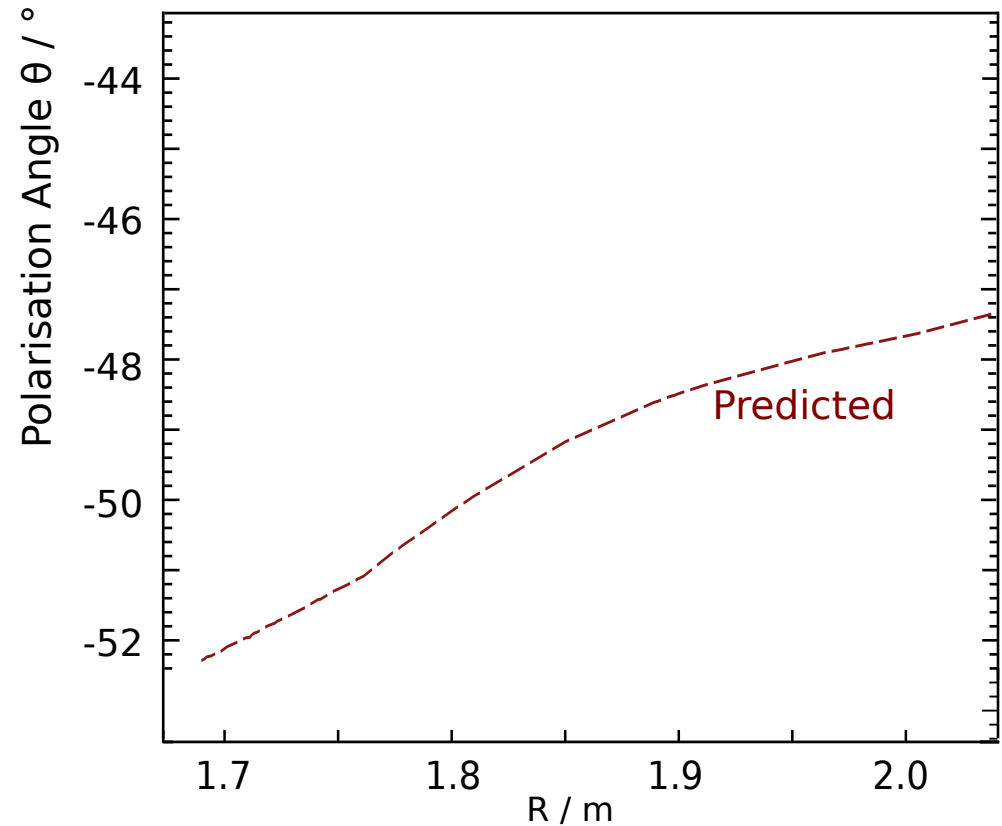
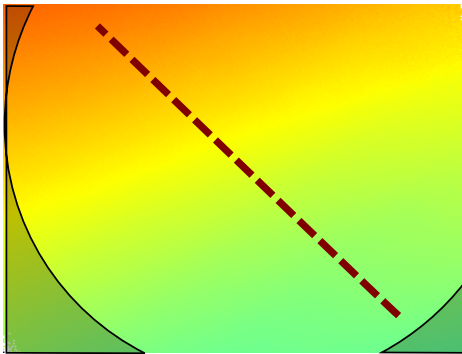


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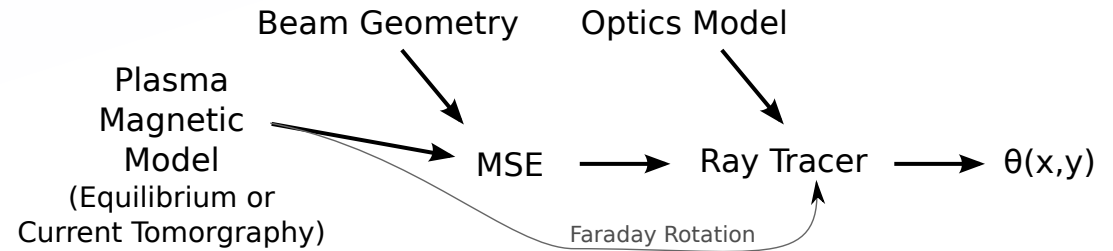


Forward Model

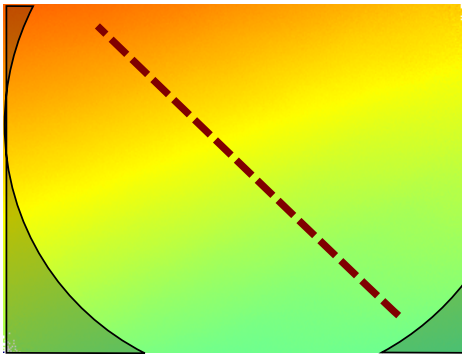


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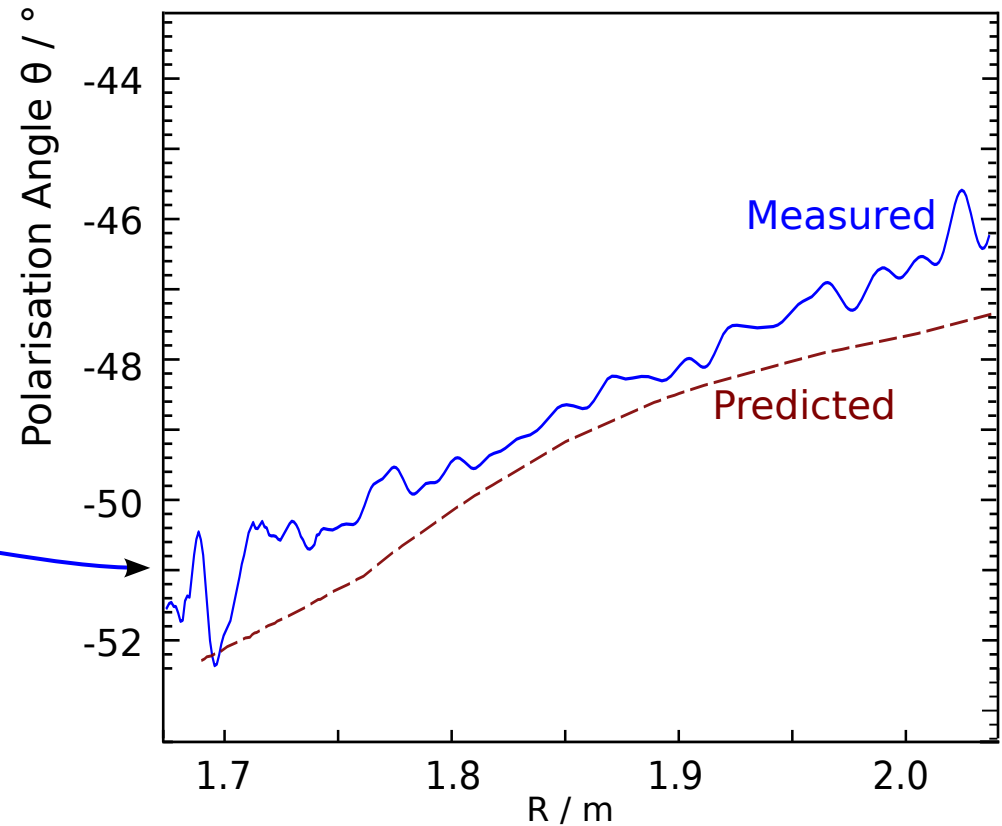
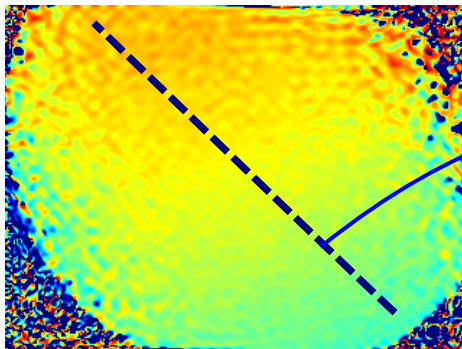
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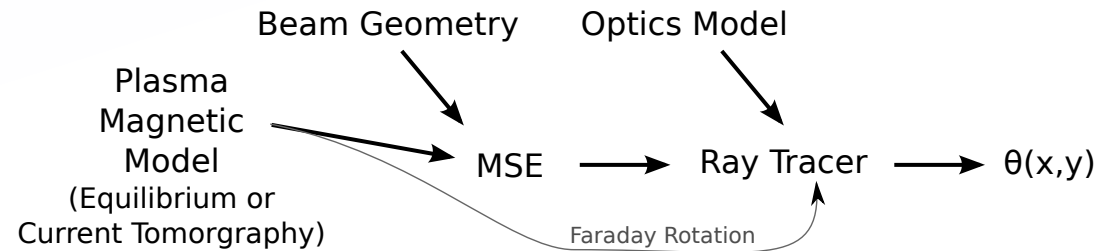


Measurement

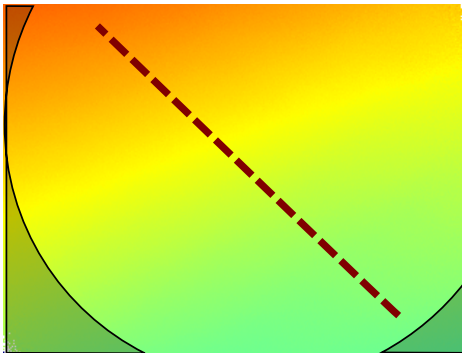


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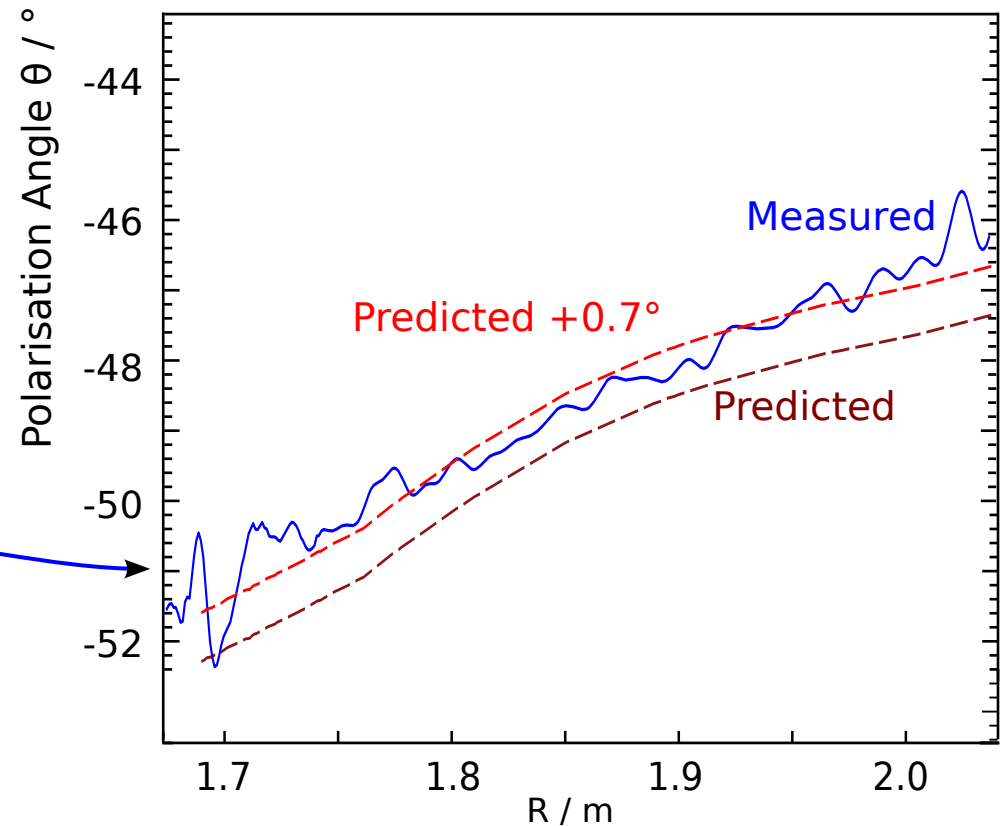
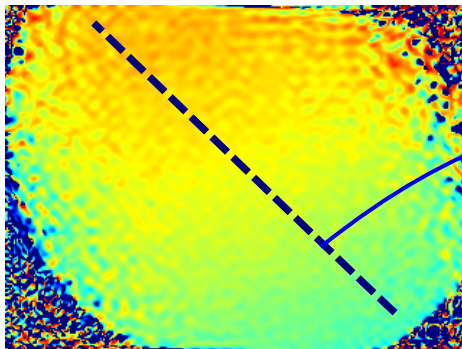
- Final prediction entirely without calibration within $\sim 0.7^\circ$ of measurement.
- Remaining uncertainties only affect offset.
- $d\theta/dr$ most important - well modelled.



Forward Model

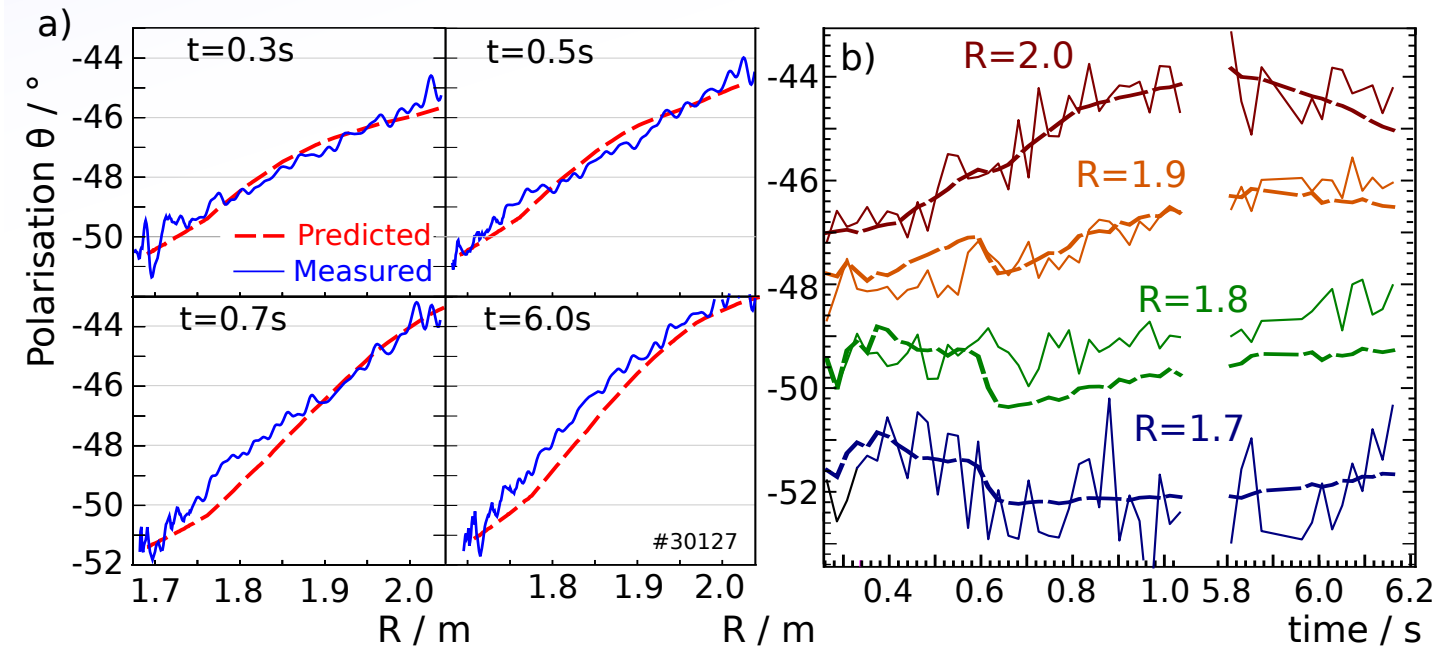


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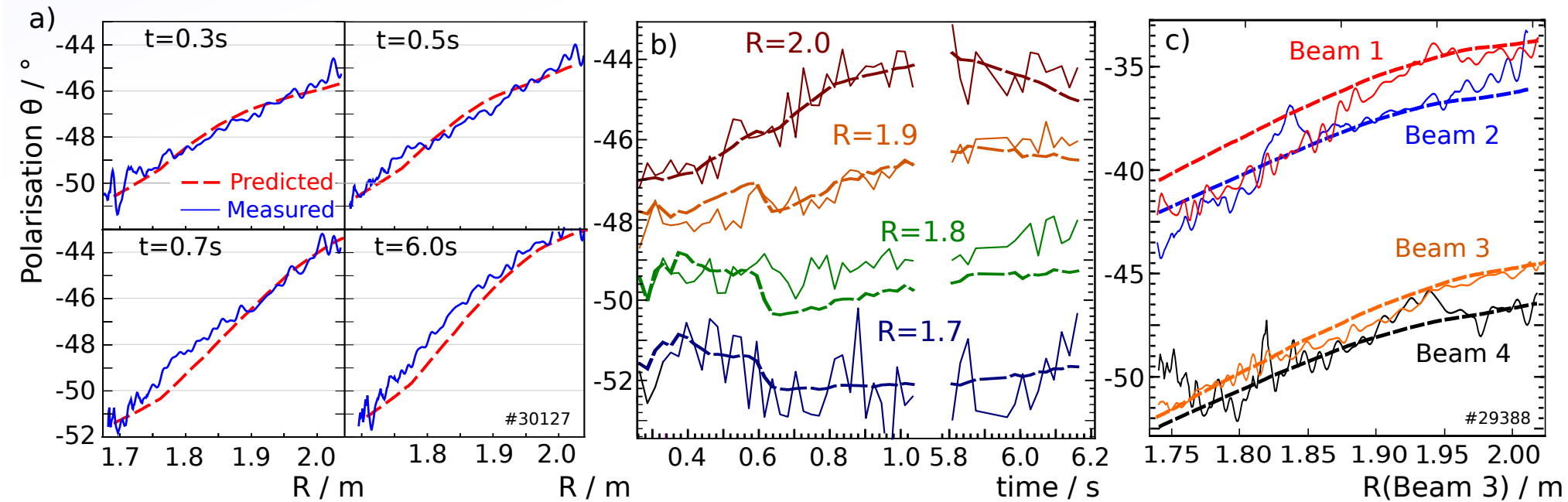
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- Remaining disagreement is largely what is unknown in equilibrium code.



Model agreement

- Remaining disagreement is largely what is unknown in equilibrium code.
- Different beam geometries also approximately predicted
 - > Confirmation of geometric effects, variation over image etc.



FusionOptics Ray Tracer

- Ray tracing core is a relatively simple to use Java library.

```
/** Shortest possible code to produce a nice imaging SVG
 * @author oliford */
public class SuccinctImagingSVGExample {
    final static String outputPath = MinervaOpticsSettings.getAppOutputPath() + "/rayTracing/succinctImaging";
    final static int nRays = 500;
    final static double z[] = OneLiners.linspace(-0.2, 0.2, 6);

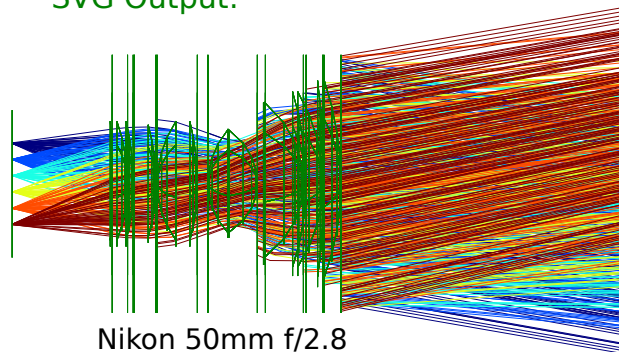
    public static void main(String[] args) {
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        Optic all = new Optic("all", new Element[]{ lens, imgPlane });

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        SVGRayDrawing svgOut = new SVGRayDrawing(outputPath + "/imgTest", new double[]{ 0, -1, -1, 2, 1, 1 }, true );
        svgOut.generateLineStyles(col, 0.0002);

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                Tracer.trace(all, ray, 30, 0.01, true);
                svgOut.drawRay(ray, iZ);
                Pol.recoverAll();
            }
        }

        svgOut.drawElement(all);
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SVG Output:



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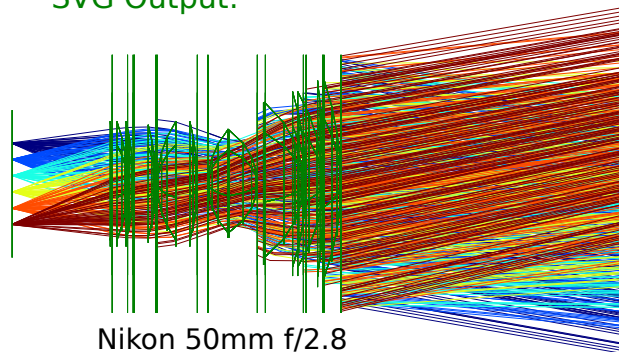
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Optics definition

SVG Output:



Nikon 50mm f/2.8

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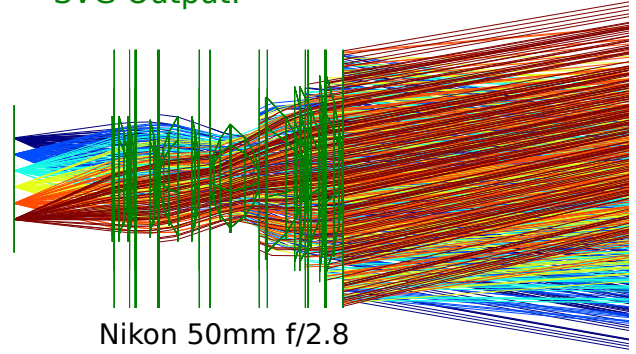
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```

Optics definition

Ray tracing

SVG Output:



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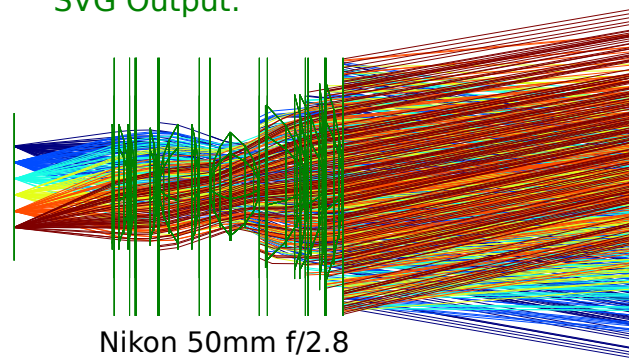
```

Optics definition

SVG Output:

Ray tracing

SVG Output:



Nikon 50mm f/2.8

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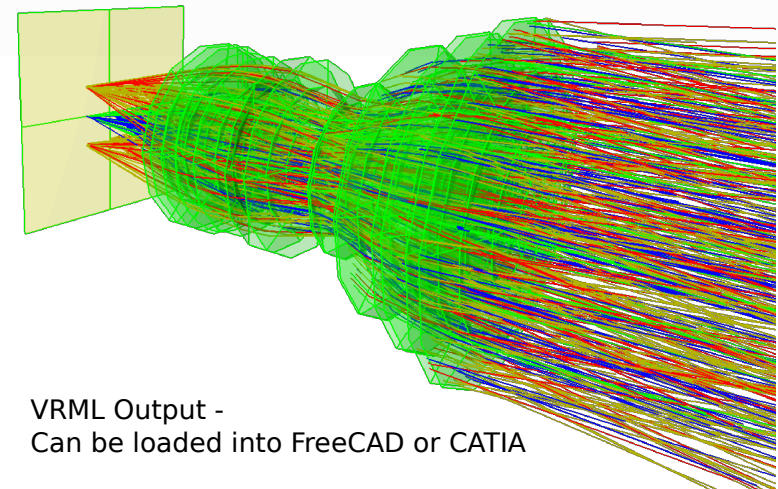
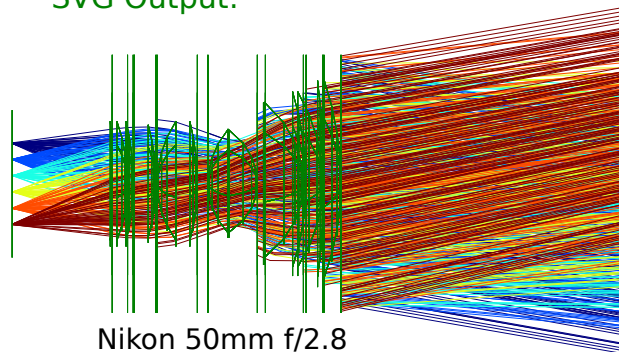
```

Optics definition

SVG Output:

Ray tracing

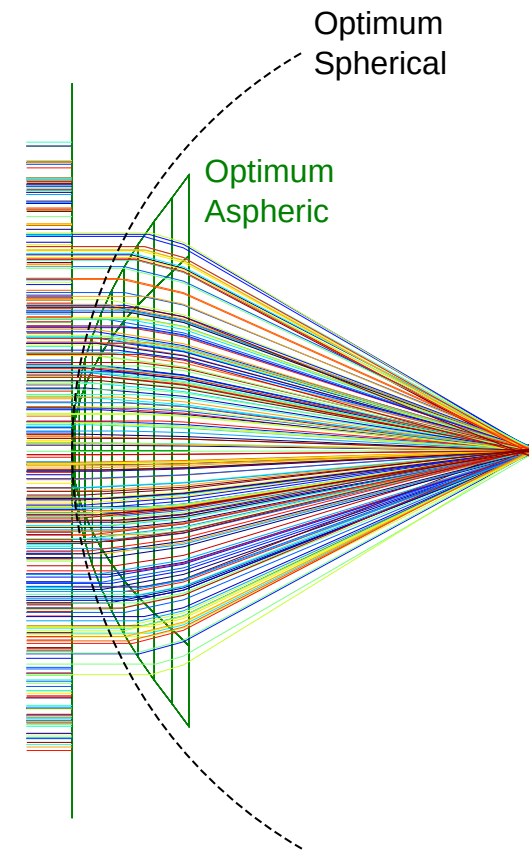
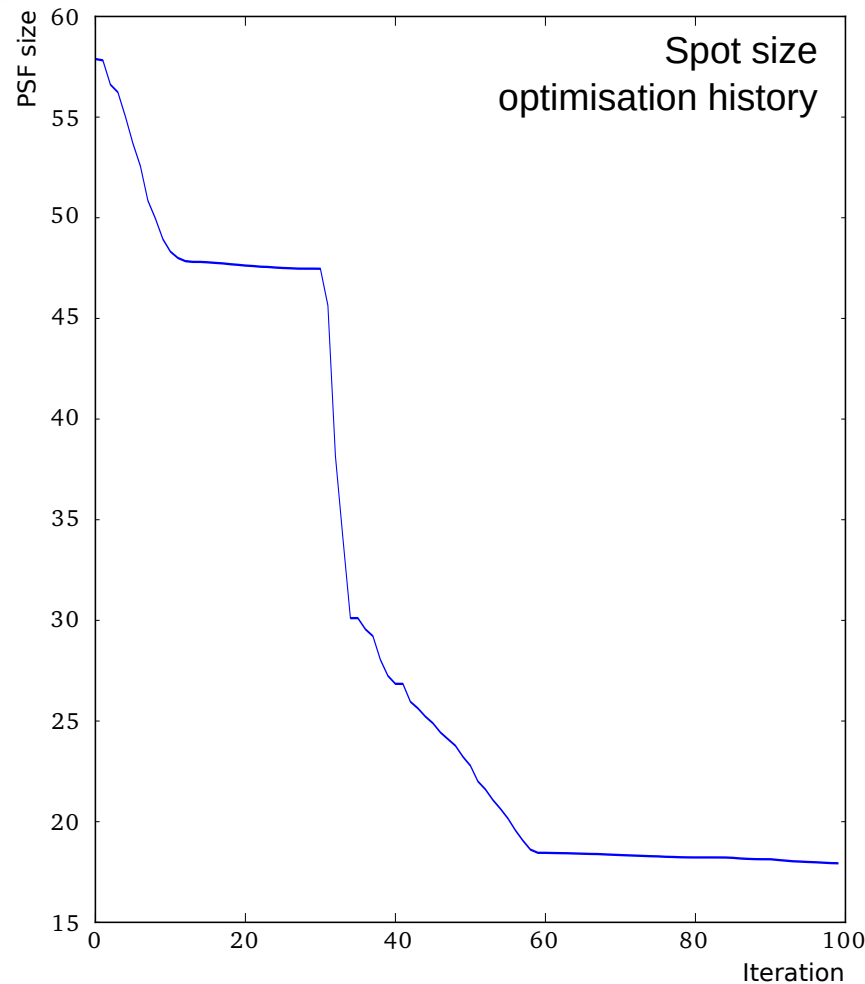
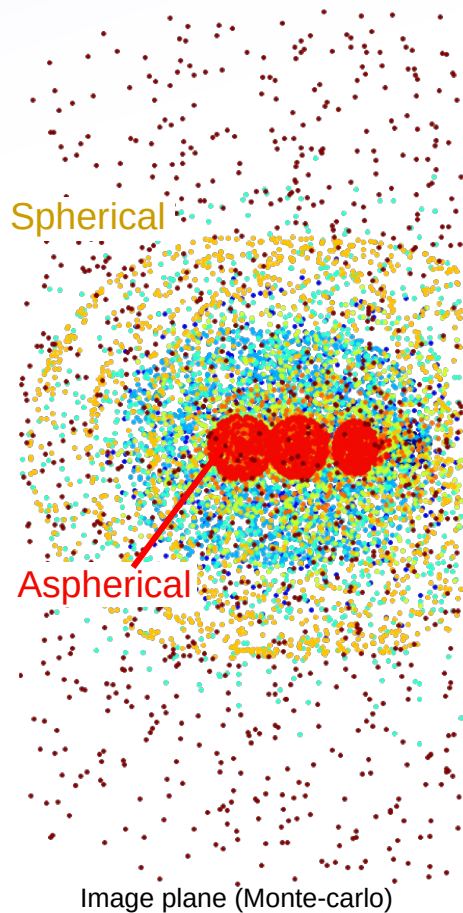
SVG Output:



FusionOptics Ray Tracer - Aspherics

Many optimisation algorithms available (Hooke & Jeeves, Genetic Algorithms, ...), so easy to optimise any parameters to any cost function. e.g:

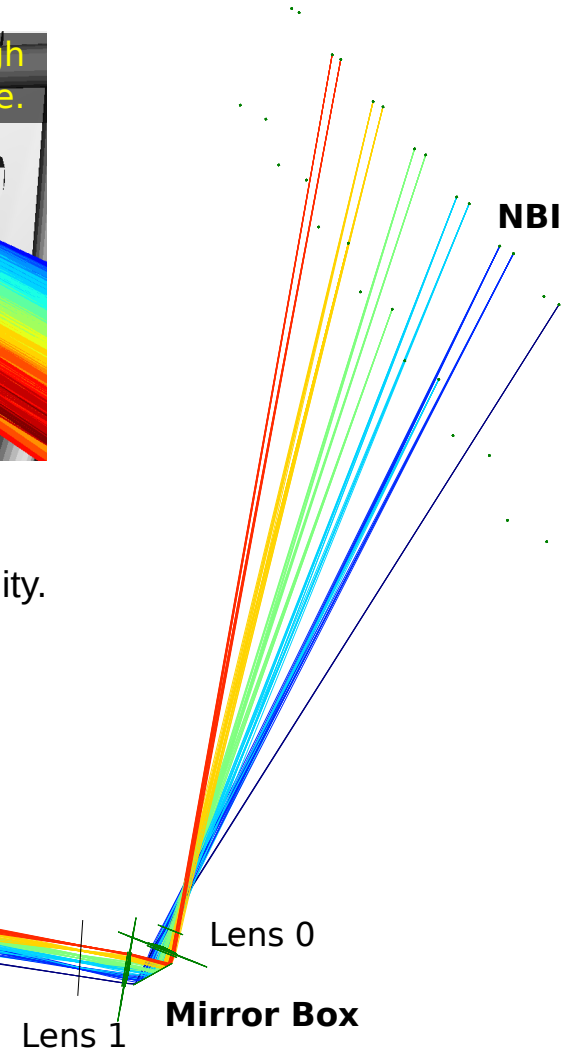
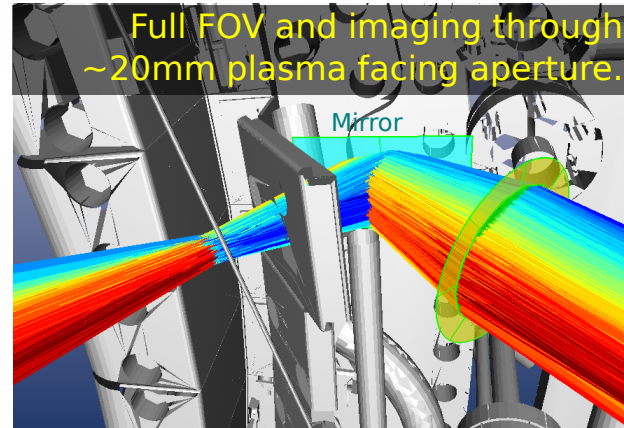
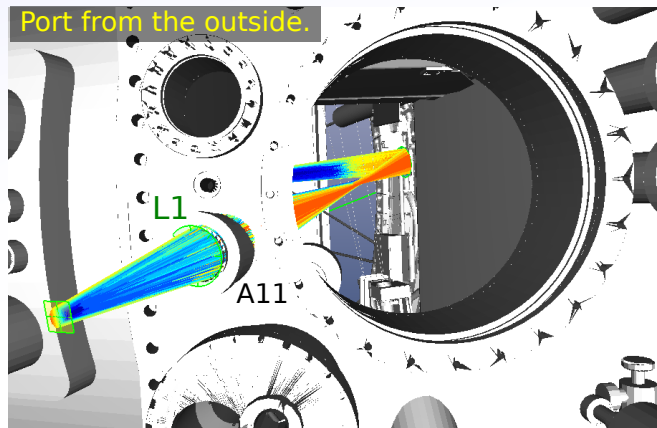
- Auto-focus (moving elements).
- Determining unknown lens properties (e.g. refractive indices) by fitting measured image.
- Aspheric surface optimisation for aberration control.



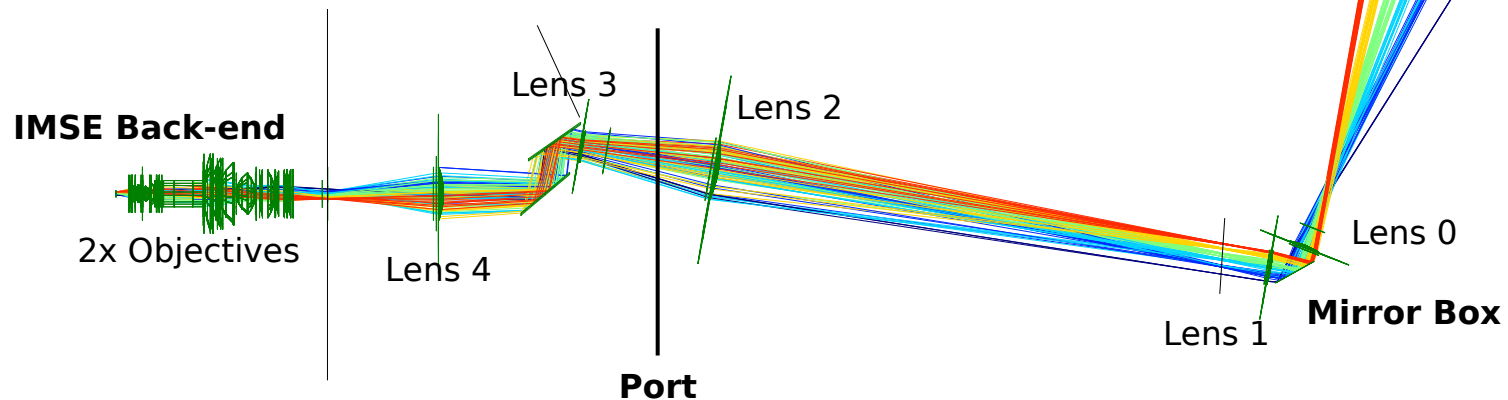
FusionOptics Ray Tracer - In place design

Has now been used for optical design/analysis of various systems at IPP:

- Permanent IMSE at ASDEX Upgrade:



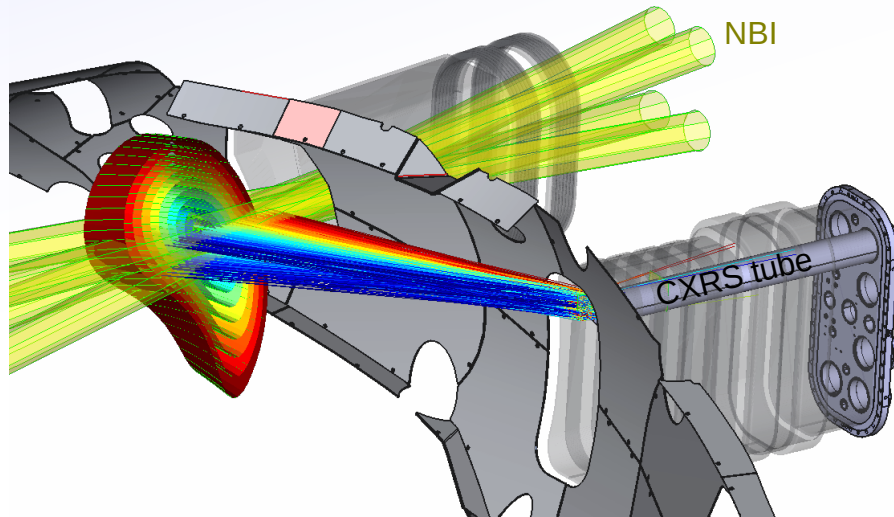
- Complex multi-component system, fully maintaining polarisation and image quality.
- 3 Spheric lenses, 2 Aspheric, 2 compound objectives.
- 3 dielectric mirrors



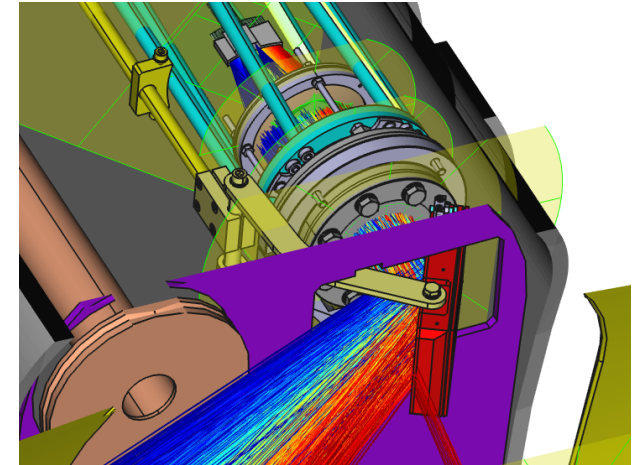
FusionOptics Ray Tracer - In place design

Has now been used for optical design/analysis of various systems at IPP:

- CXRS at W7-X: Full optical system design.



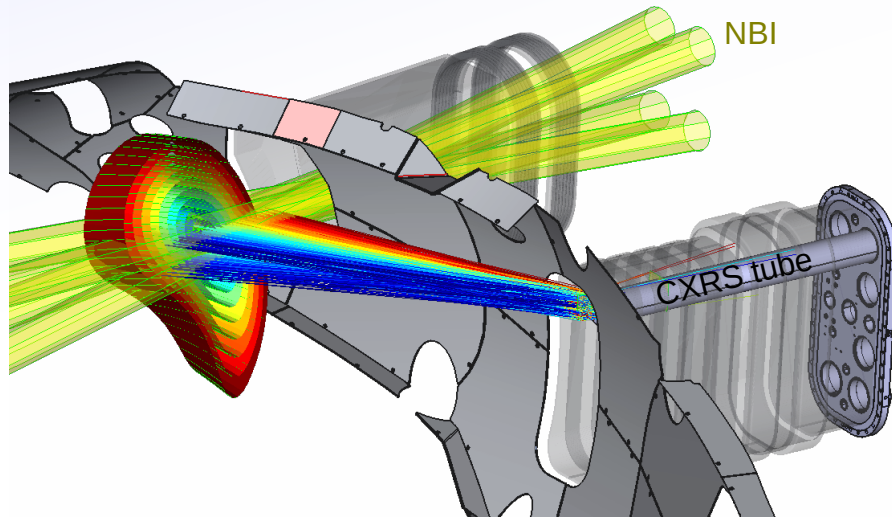
Minimal window exposure:



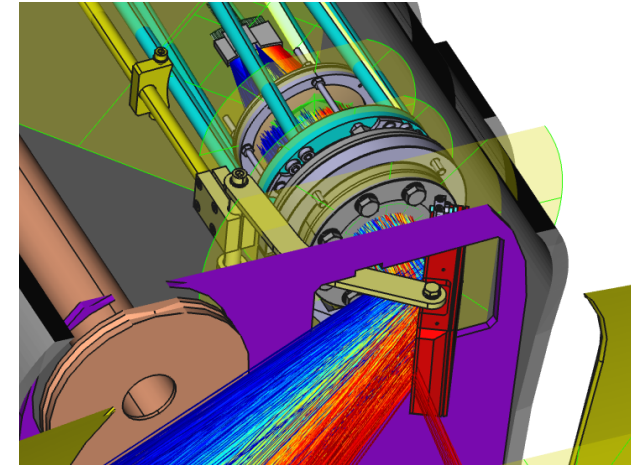
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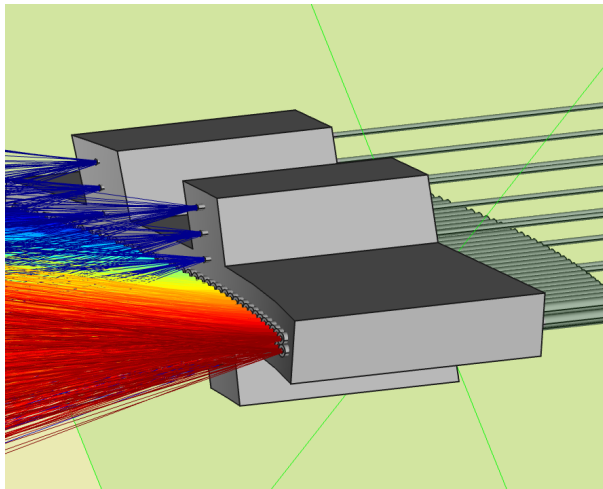
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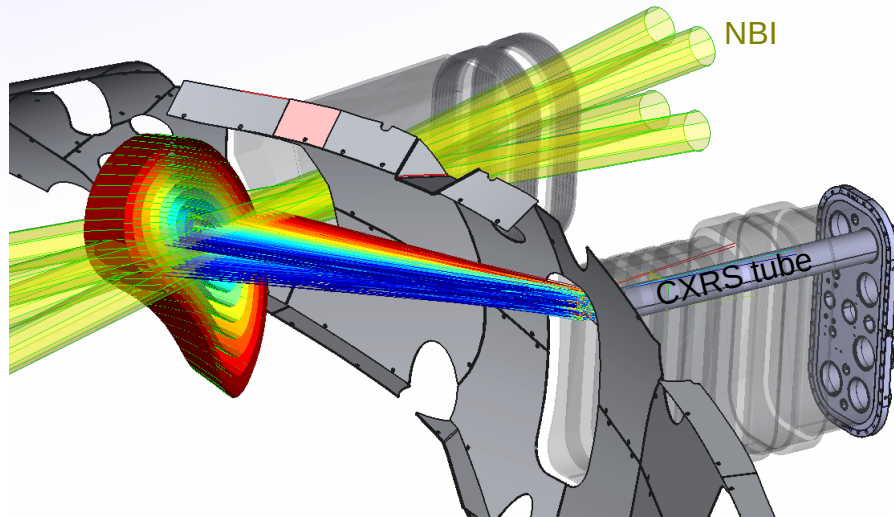
Fibre head design for optimal focus:



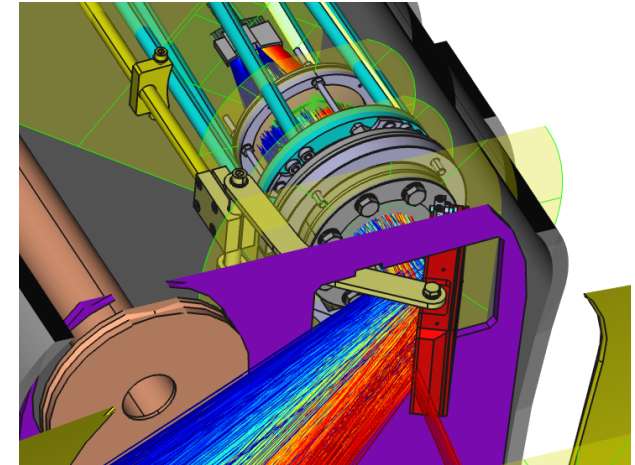
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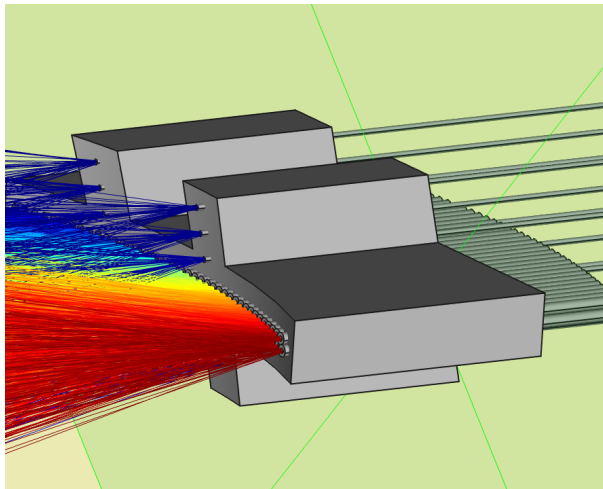
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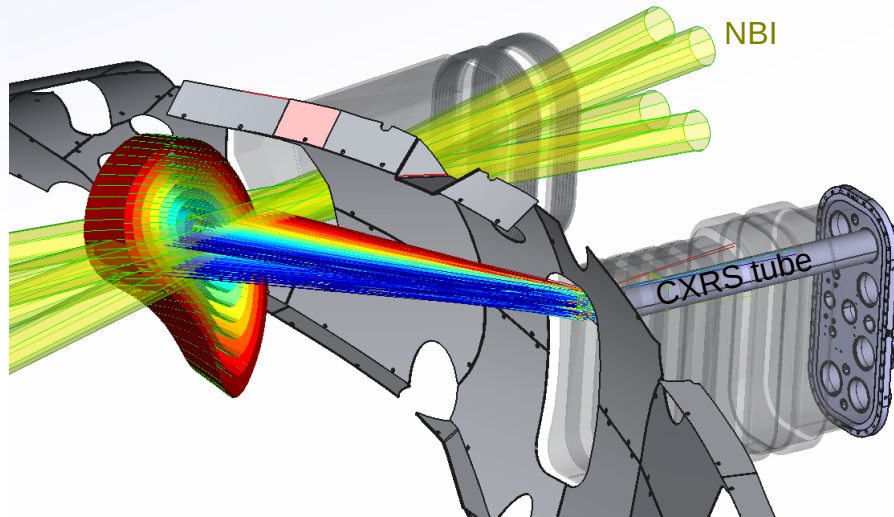


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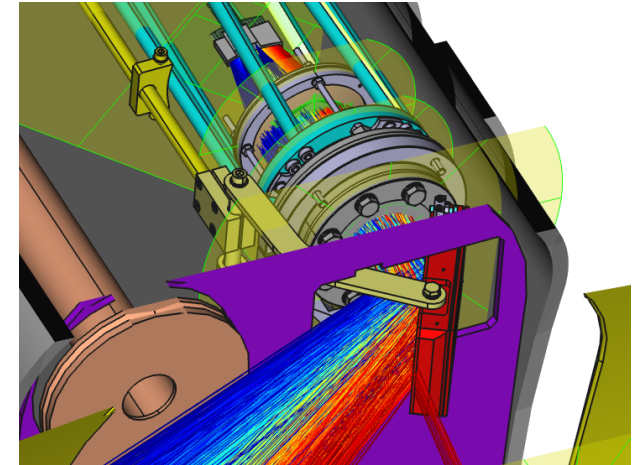


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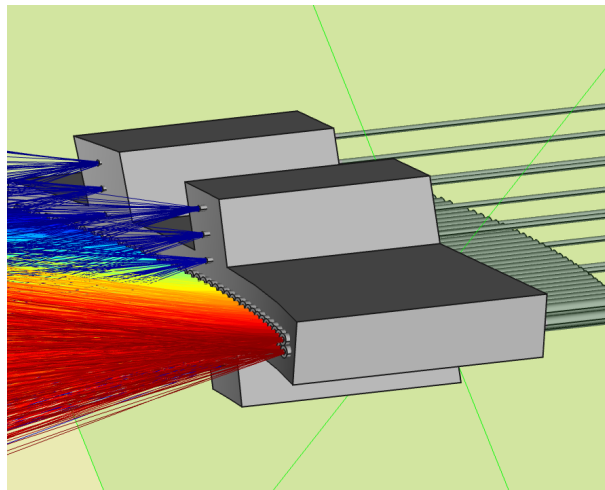
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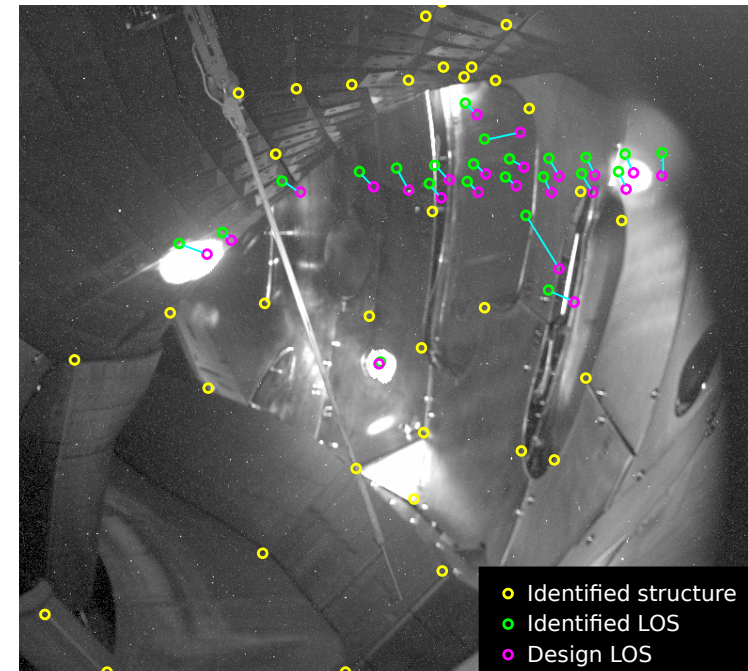
Minimal window exposure:



Fibre head design for optimal focus:



Fit model alignment from backlighting:

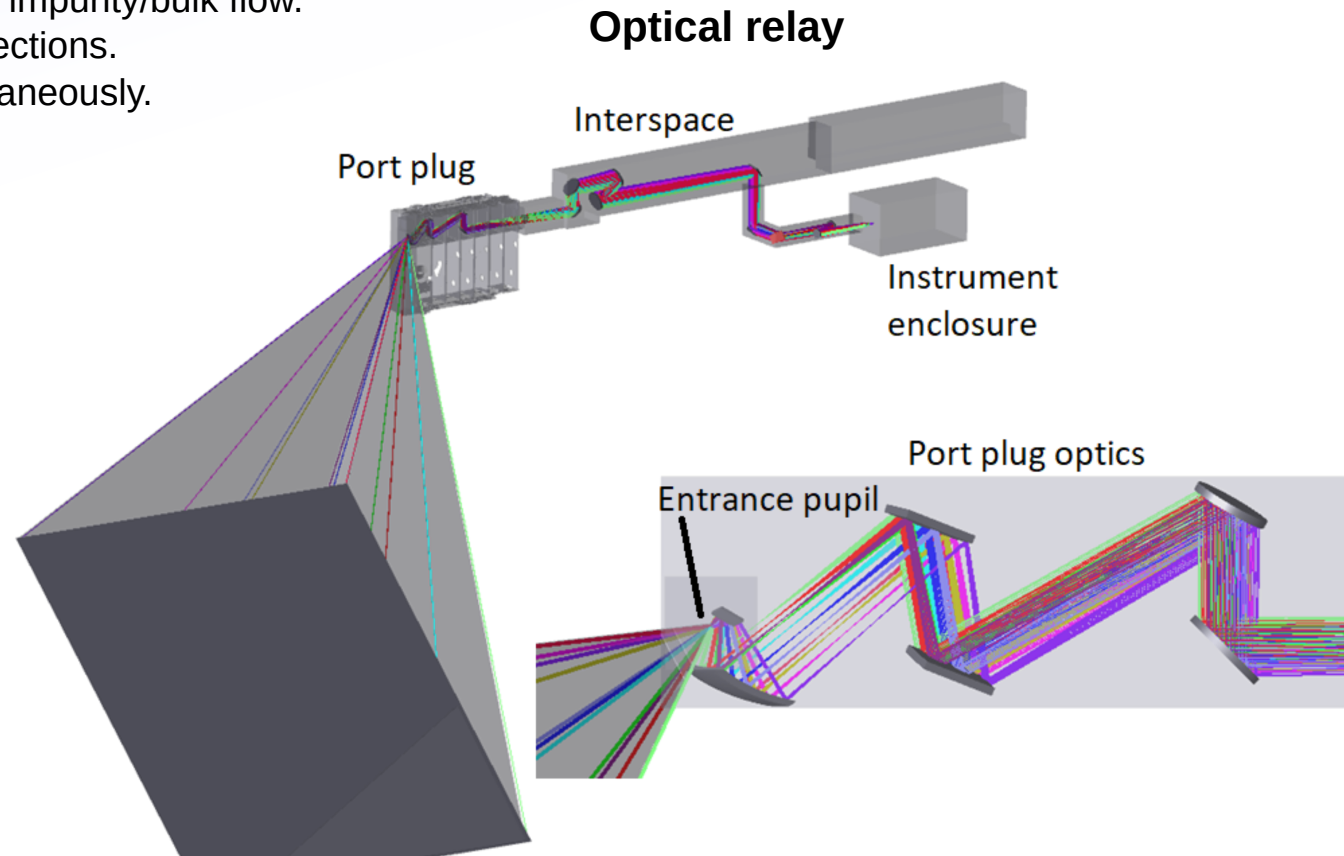


- Identified structure
- Identified LOS
- Design LOS

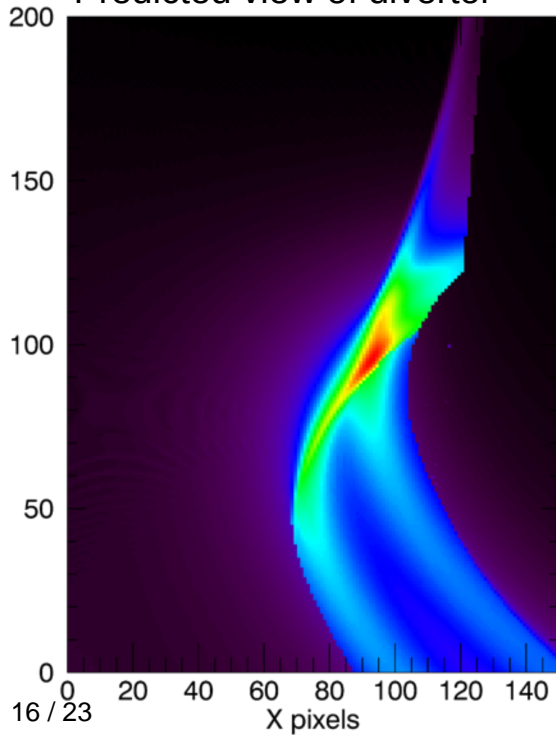
ITER Flow Monitor

ITER 'Flow Monitor'

- Coherence imaging system for SOL impurity/bulk flow.
- Use polarisation to discriminate reflections.
- Several other measurements simultaneously.



Predicted view of divertor





Summary

FusionOptics:

- 3D general ray-tracer developed for design/analysis of optical diagnostics.
- Intended for coupling into diagnostics forward models.
- Simple modular object-oriented structure.
- Detailed treatment of many realistic components (mirror, lenses, glasses, filters etc)
- Good coupling to CAD programs.
- Full 3D treatment of polarisation states, easy to understand and visualise.
- Now used for several diagnostics at AUG and W7-X.

Summary

FusionOptics:

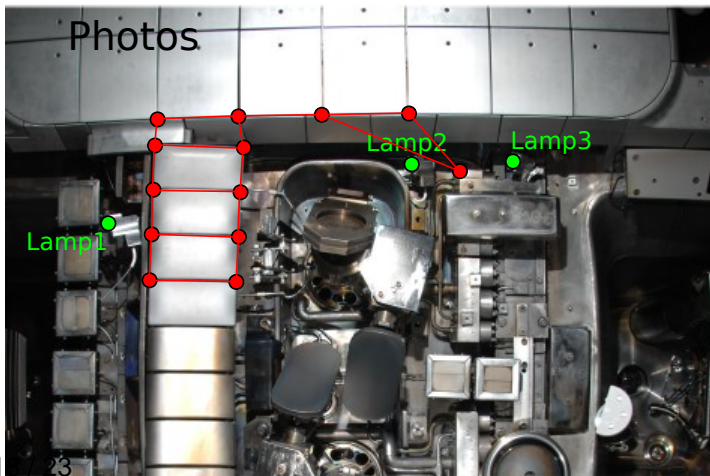
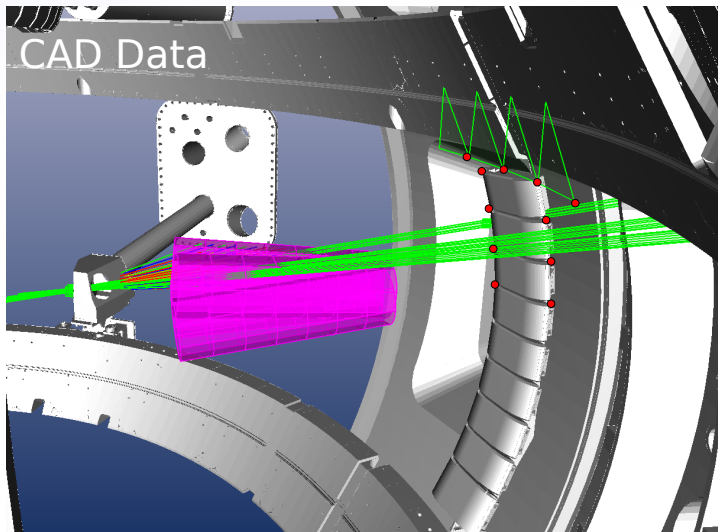
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General:

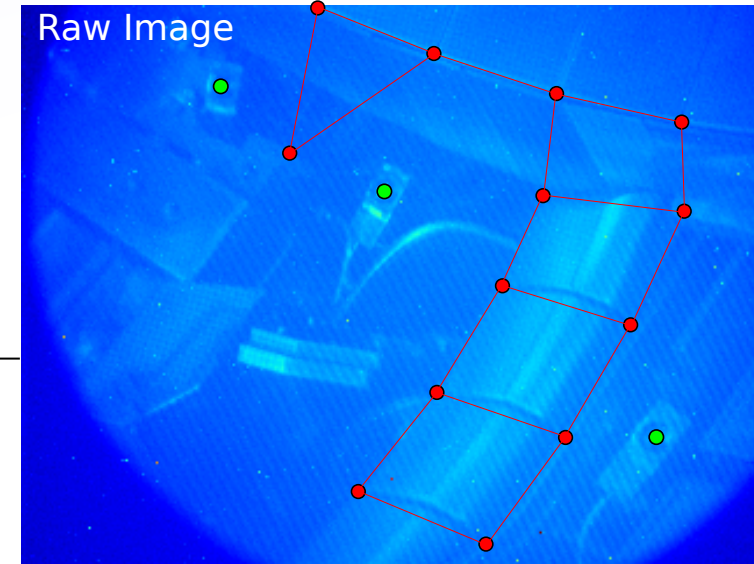
- Fitting of known image points and vignetting/limit circles constrains many unknowns such that polarisation state is well predicted.
- Coupling of 3D ray-tracing and CAD allows easy simultaneous convergence of optic and mechanical design.
- Very complex optical chains can be handled without too much difficulty - (e.g. most optical ITER diagnostics)
- Small polarisation effects ($\sim 0.1^\circ$) are numerous, but can be modelled.
- Particular relevance for ITER Flow Monitor (coherence imaging / divertor viewing).

Image Transform

- Points with known 3D positions (CAD)
- Define affine/cubic transform directly $(x,y) \rightarrow (\varphi, \theta) \rightarrow (R, Z)$
- Fit unknown optics model parameters so ray-tracing matches:
 - a) Camera position $\pm 6\mu\text{m}$
 - b) Mirror angles $\pm 0.1^\circ$



Project in (R,Z)



Z / m

0.20

0.15

0.10

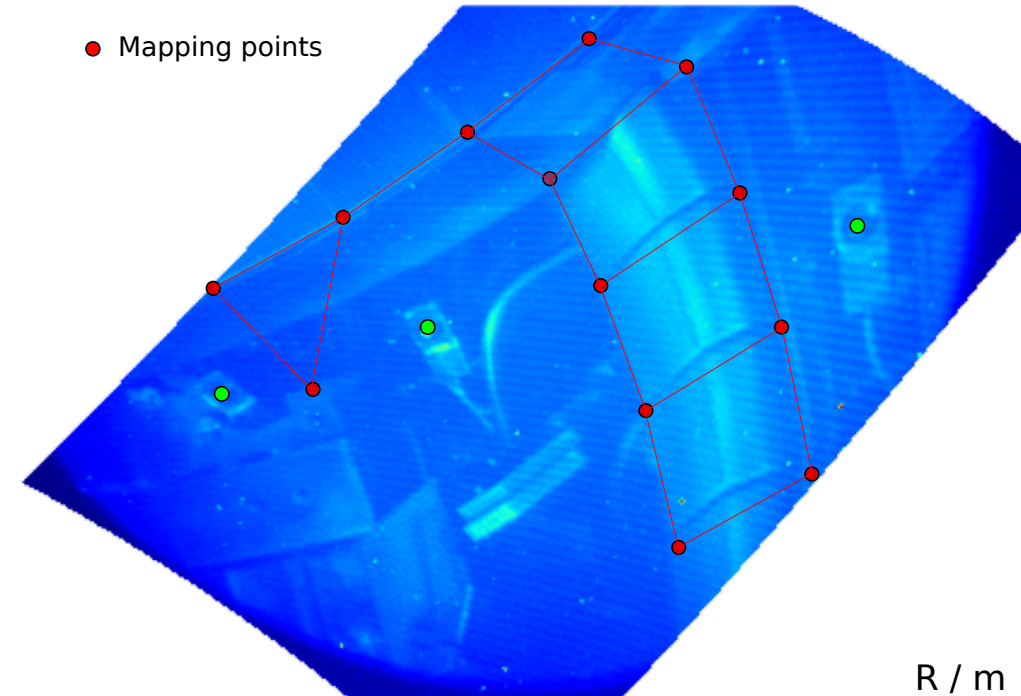
0.05

0.00

-0.05

-0.10

● Mapping points



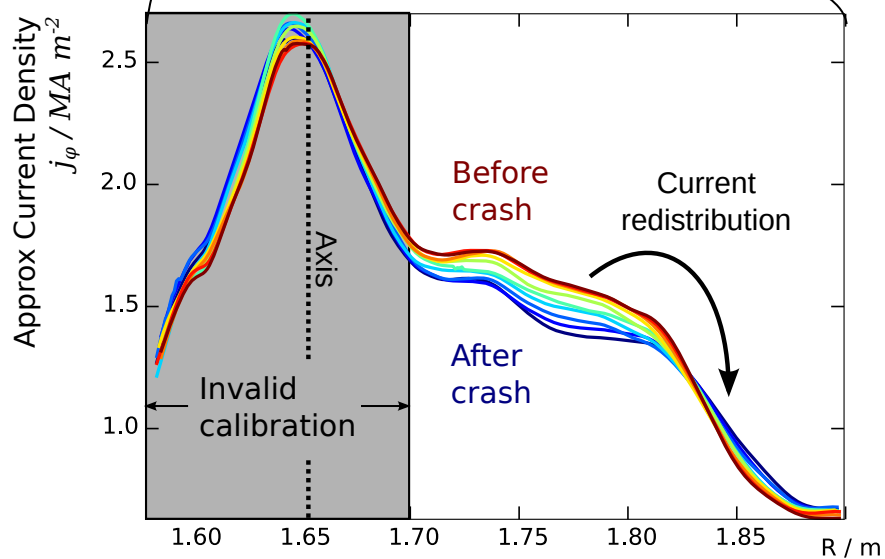
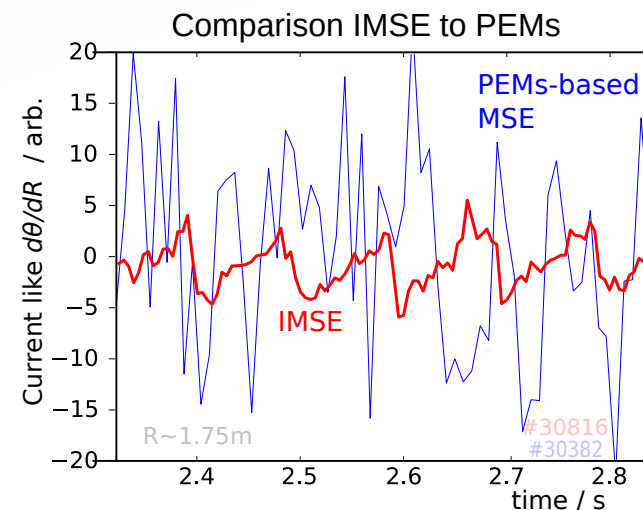
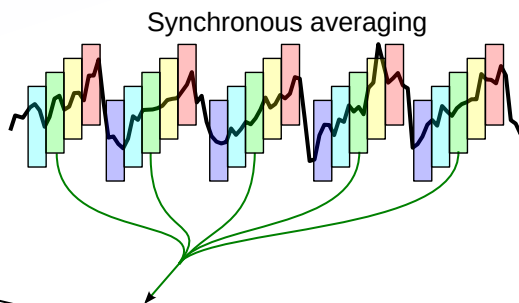
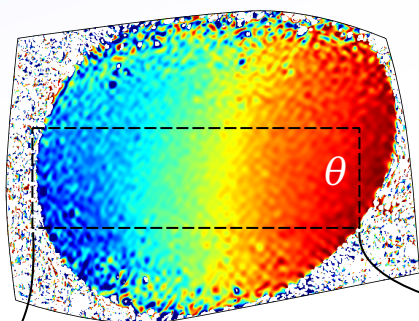
R / m

1.6 1.7 1.8 1.9 2.0

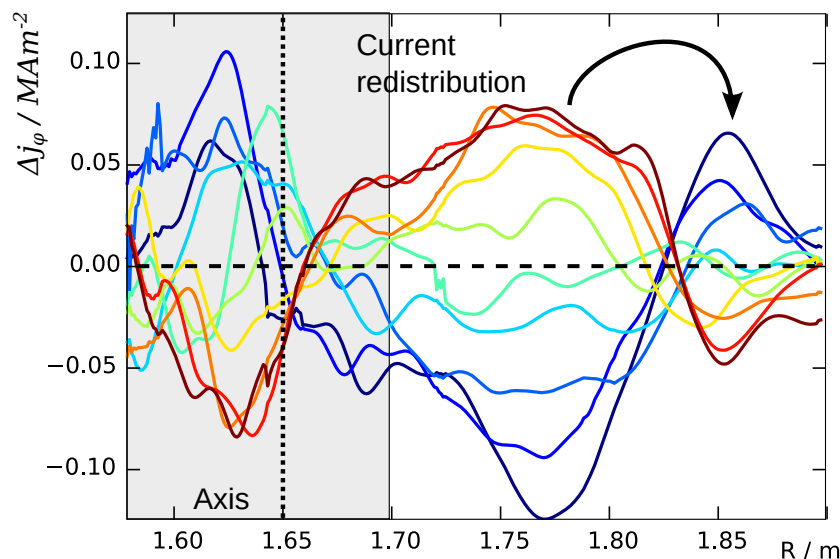
Sawteeth - Magnetic Reconnection

What do we see in the IMSE data?

- Sawtooth changes are **very** small - need good statistics.
- Average over Z near axis
- Synchronous average over many sawteeth in time.



Difference from average profile:



Current redistribution: $\Delta j \sim 0.050 \text{ MA m}^{-2}$

Measurements every ~3cm (resolution): $\Delta(d\theta/dR) \sim 0.7^\circ \text{ m}^{-1}$

--> $\Delta\theta \pm 0.02^\circ$ required for $\Delta R = 3\text{cm}$

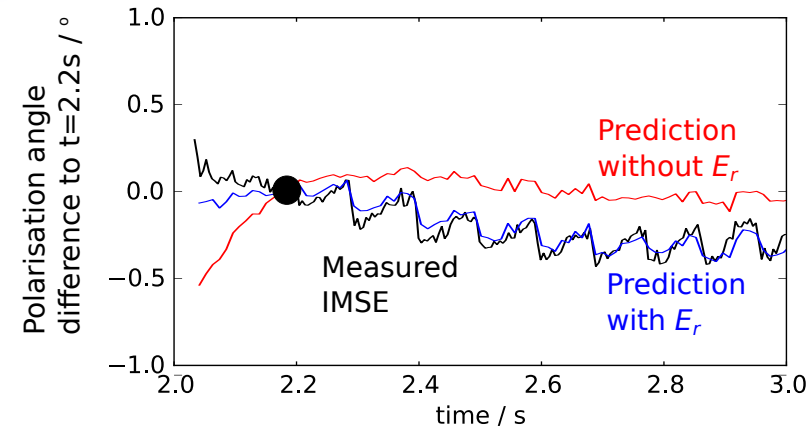
Integrated Equilibrium vs IMSE - Sawteeth

Required precision is so high, many other factors become important:

Plasma radial electric field:

$$E = v \times B + E_r$$

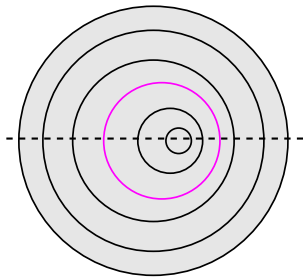
At some locations, ΔE_r during sawtooth dominates measurement:



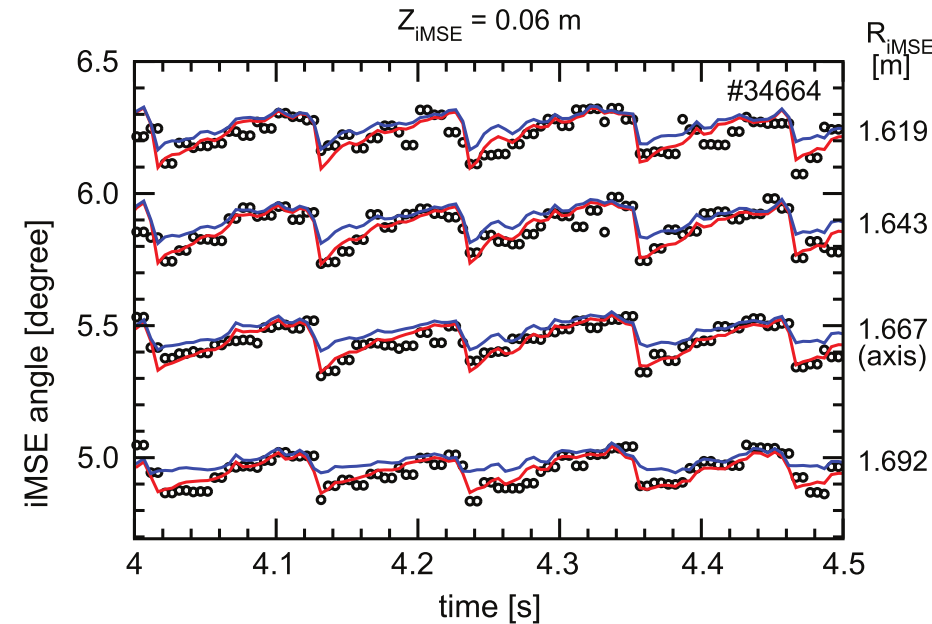
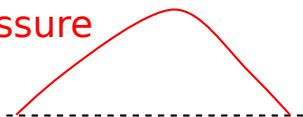
Shafranov shift:

Movement of plasma axis with pressure.

(including redistribution of fast-ions from neutral beam)



Pressure

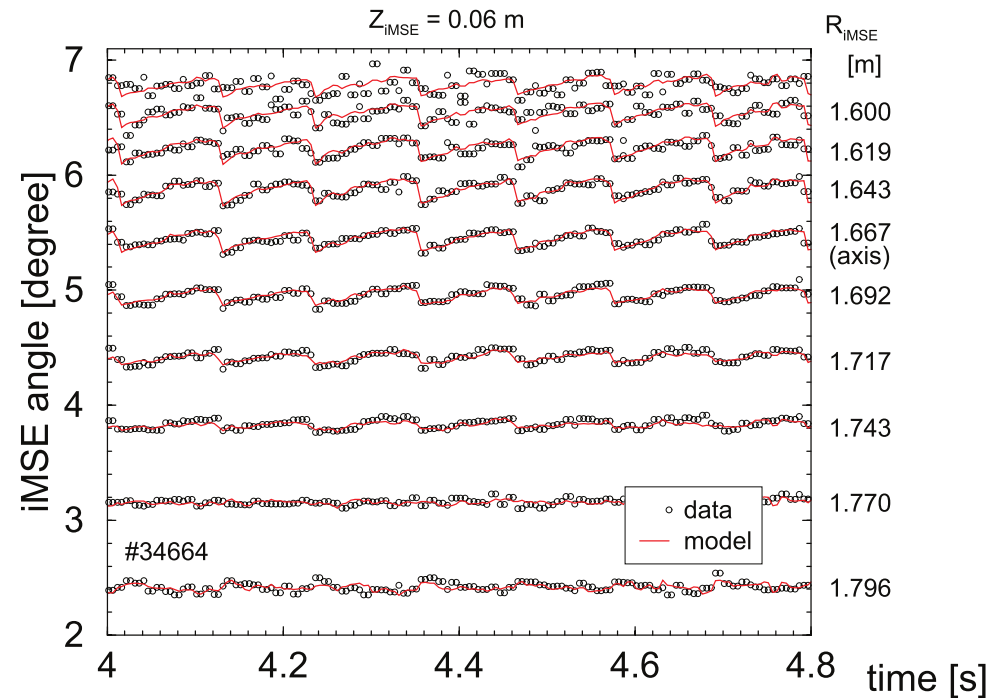
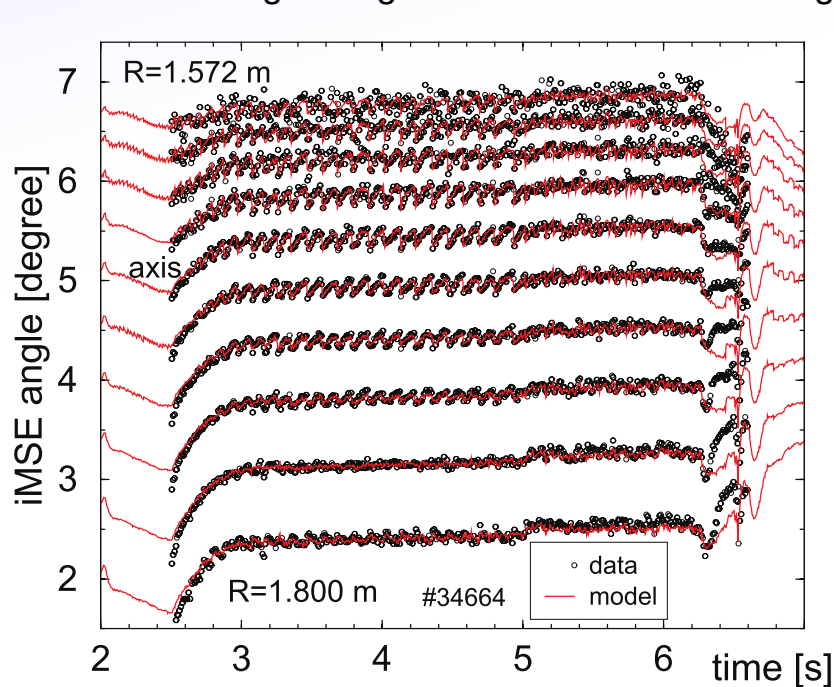


Integrated Equilibrium vs IMSE - Sawteeth

Required precision is so high, many other factors become important:

but...

we now have good agreement between full integrated model and IMSE measurements for sawtooth evolution in θ .



- This is where we are - 'the state of the art ... science'
What next?

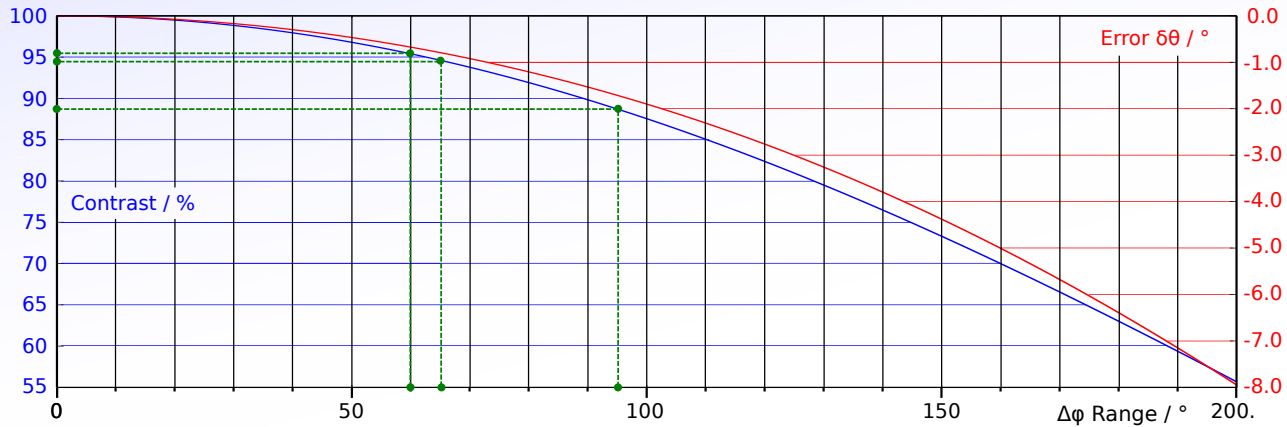
IMSE:
- Improve calibration
systematics,

Converge

IDE:
- Modeling of effects.
- Tolerance to calibration
systematics.

The return of the Magic Number

The crystal parallelism isn't enough to explain all of the magic number. E.g. United Crystals plate A has $< 60^\circ$ and is very flat in the middle ($< 5^\circ$ variation). That should give a contrast of $> 98\%$, but the measured contrast is always below 90%.



So, there is more to the story....

Using a big sphere to light all of the CCD/lens and looking at the full 16mm CCD shows a consistent pattern:

United Crystals A

United Crystals B

CLaser Displacer



Linked
image
not found