



Motional Stark Effect Coherence Imaging for ASDEX Upgrade. Design and evaluation progress.

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1: Max-Planck Institut für Plasmaphysik, Greifswald, Germany

- 2: Plasma Research Laboratory, Australian National University, Canberra
- Brief (re)introduction.
- Line integration and resolution.
- What do we gain with 2D measurements? in Theory,
 - in Practice
- Model improvements.
- Outlook



2D Current Measurements at AUG with Coherence Imaging.



Very Brief Introduction





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Neutral beam atoms injected into plasma. Excited by plasma, then emit $H\alpha/D\alpha$ radiation.



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Spectrum from a single pixel:





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Stark split by electric field in rest frame of atom:

 $\boldsymbol{E} = \boldsymbol{v} \times \boldsymbol{B}$



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Complications:

Atoms with different injection energy: different Doppler shift. Doppler broadening: Beam divergence, line integration etc. Background $D\alpha$ (not shown).



Spectrum from a single pixel:





Introduction: Spectro-Polarimetric Imaging

We want a full 2D image of polarisation of $D\alpha$ emission from beam. Needs to also be sensitive to spectrum and polarisation.





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Savart plates: Split light into 2 components and time delay one depending on incident angle (i.e. position in image/object plane).



$I = \frac{I_0}{2} \left[1 + \zeta \left(\cos 2\theta \cos(x) + \sin 2\theta \sin(x) \sin(y) \right) \right]$

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$$\begin{split} I &= \int \frac{I_0}{2} \left[1 + \zeta \left(\cos 2\theta \cos(x) + \sin 2\theta \sin(x) \sin(y) \right) \right] \, dl \\ &\neq \frac{\langle I_0 \rangle}{2} \left[1 + \langle \zeta \rangle \left(\cos \langle 2\theta \rangle \cos(x) + \sin \langle 2\theta \rangle \sin(x) \sin(y) \right) \right] \end{split}$$

Actually, this is wrong. The image is really the integral of this over the LOS. However - it seems that if we assume it is, the recovered θ is the same as the LOS average for each pixel. The other terms are not equal to their LOS averages and introduce extra phases.





Demodulation: Accuracy of θ recovery.







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The recovered θ are really < θ > over the LOS. Spatial resolution is a combination of pixel-pixel averaging due to modulation (1cm) and the LOS averaging.





























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To final objective is to measure plasma current *j*.

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Assuming toroidal symmetry, the current is:

 $-\mu_0 j_\phi = \frac{\partial B_z}{\partial R} + \frac{1}{R} \frac{\partial^2}{\partial Z^2} \int_0^R R' B_z(R', Z) \, dR'$

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However, we only see where the MSE emission is, so can only integrate from some $R = R_0$:

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This we have with 1D MSE.





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A normal MSE system has only $B_z(R)$ so cannot calculate the 3rd term. In theory, with 2D measurements, we can.





- Take CLISTE current distribution
- Predict 30x30 grid of Bz.
- Try to directly calculate jo









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Conclusion: **No**. You still cannot exactly calculate j_{ϕ} directly.

(Centre IPP



So can we directly calculate $j\phi$?



- Predict 30x30 grid of Bz.
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Conclusion: **No**. You still cannot exactly calculate j_{ϕ} directly.

However, we still might not need to go as far as equilibrium as we also gain measurements of dBz/dR at different Zs. Together with normal coil measurements, it is now part of a complex tomography problem that we have done before.





AUG PF coils and pickups model now in Minerva, so we can do Current Tomorgraphy and Bayesian Equilibrium for AUG. Try simple tomography from:







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All sigmaBr = sigmaBz =10mT

By current tomography II 2) Normal MSE (line) R / m 1.4 1.6 1.8 2.0 3) IMSE Bz (grid) R / m 1.4 1.6 1.2 1.8 2.0



The IMSE still has a large uncertainty in $j\phi$ offset. The unknown term it is not entirely pinned down by the magnetics.



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Off axis and near the core, the AUG IMSE system will see Br with reasonable strength: —



Relative stength of Br: MSE Intensity weighted LOS integral Br/Bz



i / MA

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/ MA

-2

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1.8

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4) IMSE Br and Bz

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Even here, the LOS average polarisation angle, in terms of the field is:

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At 5 - 10%, it will have an effect, but we do not expect to see the full current recovery from 2D tomography.







From this week, I can now do the full inversion from polarisation angle to plasma current $\theta(x,y) \rightarrow j_{\phi}(R, Z)$, (without equilibrium) thanks to some new non-parametric (Gaussian process) priors (J. Svensson) and getting access to an unloaded linux cluster (on wednesday).





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Initial results indicate that it is possible to recover the $j_{\phi}(R, Z)$ to at least a good resolution for studying the bulk plasma (e.g. testing different equilibrium models etc). This is MUCH better than is currently possible. Resolution is processing limited - Higher resolution may be possible, but computation cost rises with resolution as $\sim n^4$.







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Camera will be subject to magnetic field, which Minerva can predict from the PF coils. For the highest plasma current ($I_p = 1.2MA$), |B| < 50mT:

















- The camera we have (12bit 1376x1040 Imager QE) was used next to the coils in Pilot (PSI) last year, so may survive this. Apart from a very slow frame rate (10Hz), it is otherwise perfectly suited, so could be used for a first attempt.






Other progress (Hardware)



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- Faraday rotation due the field in the Savart plates will not be a problem, but the main delay plate might be. (I'm assuming Lithium Niobate, but I can't find a Verdet constant for it in the Literature. Any suggestions?)





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Things still to add:

- Background D-Alpha and FIDA. (These will only reduce S/N).
- CCD noise (other than photon statistics).
- Viewing optics.